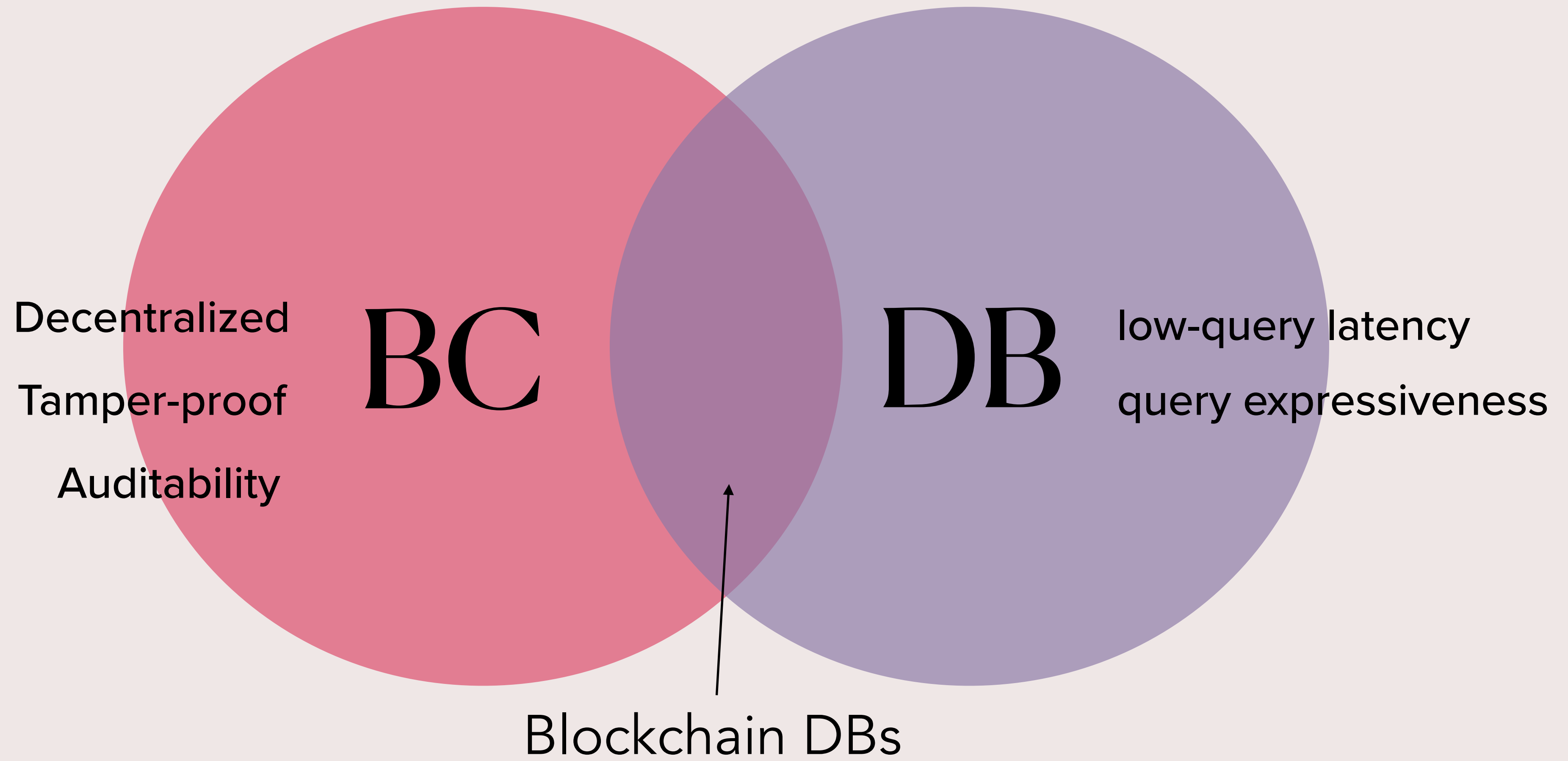


Encrypted Blockchain Databases

Daniel Adkins, **Archita Agarwal**, Seny Kamara, Tarik Moataz



Blockchain DBs

Blockchain DBs

BIGCHAIN 

 **bluzelle**

Blockchain DBs

BIGCHAIN 



- electronic healthcare records
- financial records
- legal documents
- customer data

Blockchain DBs

BIGCHAIN 



CONFIDENTIALITY ?

- electronic healthcare records
- financial records
- legal documents
- customer data

Blockchain DBs

BIGCHAIN 



CONFIDENTIALITY ?



- electronic healthcare records
- financial records
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- customer data

In this work ...

**How to store Encrypted
Multi-Maps on BCs**

In this work ...

How to store Encrypted Multi-Maps on BCs

a kind of NoSQL Databases, like Key-Value Stores

What are Multimaps?

Set of label/value tuples

ℓ_1	(v_1, v_2)
ℓ_2	(v_1, v_2, v_3)
ℓ_3	(v_3)
ℓ_4	(v_4, v_5)
ℓ_5	(v_2, v_5, v_7, v_8)

Varying lengths

Encrypted

What are Multimaps?

Set of label/value tuples

ℓ_1	(v_1, v_2)
ℓ_2	(v_1, v_2, v_3)
ℓ_3	(v_3)
ℓ_4	(v_4, v_5)
ℓ_5	(v_2, v_5, v_7, v_8)

Encrypted What are Multimaps?

Set of label/value tuples

Encrypted

ℓ_1	(v_1, v_2)
ℓ_2	(v_1, v_2, v_3)
ℓ_3	(v_3)
ℓ_4	(v_4, v_5)
ℓ_5	(v_2, v_5, v_7, v_8)

What are ^{Encrypted} Multimaps?

Set of label/value tuples

Encrypted

$t \leftarrow \text{Query}(\ell)$

ℓ_1	(v_1, v_2)
ℓ_2	(v_1, v_2, v_3)
ℓ_3	(v_3)
ℓ_4	(v_4, v_5)
ℓ_5	(v_2, v_5, v_7, v_8)

What are ^{Encrypted} Multimaps?

Set of label/value tuples

Encrypted

	ℓ_1	(v_1, v_2)
$t \leftarrow \text{Query}(\ell)$	ℓ_2	(v_1, v_2, v_3)
$\text{EMM}' \leftarrow \text{Add}(\ell, t')$	ℓ_3	(v_3)
	ℓ_4	(v_4, v_5)
	ℓ_5	(v_2, v_5, v_7, v_8)

What are ^{Encrypted} Multimaps?

Set of label/value tuples

Encrypted

	ℓ_1	(v_1, v_2)
$t \leftarrow \text{Query}(\ell)$	ℓ_2	(v_1, v_2, v_3)
$\text{EMM}' \leftarrow \text{Add}(\ell, t)$	ℓ_3	$(v_3) (v_4)$
	ℓ_4	(v_4, v_5)
	ℓ_5	(v_2, v_5, v_7, v_8)

What are ^{Encrypted} Multimaps?

Set of label/value tuples

Encrypted		
	ℓ_1	(v_1, v_2)
$t \leftarrow \text{Query}(\ell)$	ℓ_2	(v_1, v_2, v_3)
$\text{EMM}' \leftarrow \text{Add}(\ell, t)$	ℓ_3	$(v_3) (v_4)$
$\text{EMM}' \leftarrow \text{Delete}(\ell, t')$	ℓ_4	(v_4, v_5)
	ℓ_5	(v_2, v_5, v_7, v_8)

In our work

LSX

List-Based

TRX

Tree-Based

PAX

Patch-Based



In our work

LSX

List-Based

TRX

Tree-Based

PAX

Patch-Based



In our work

LSX

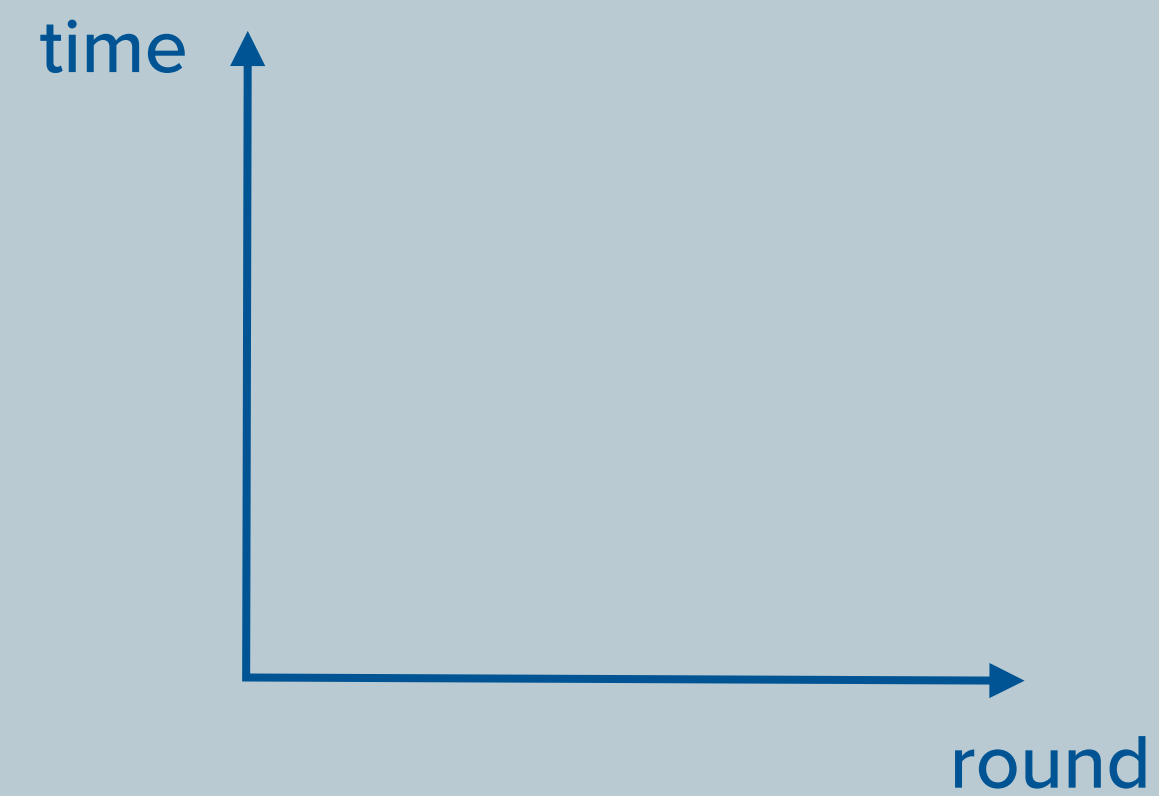
List-Based

TRX

Tree-Based

PAX

Patch-Based



In our work

LSX

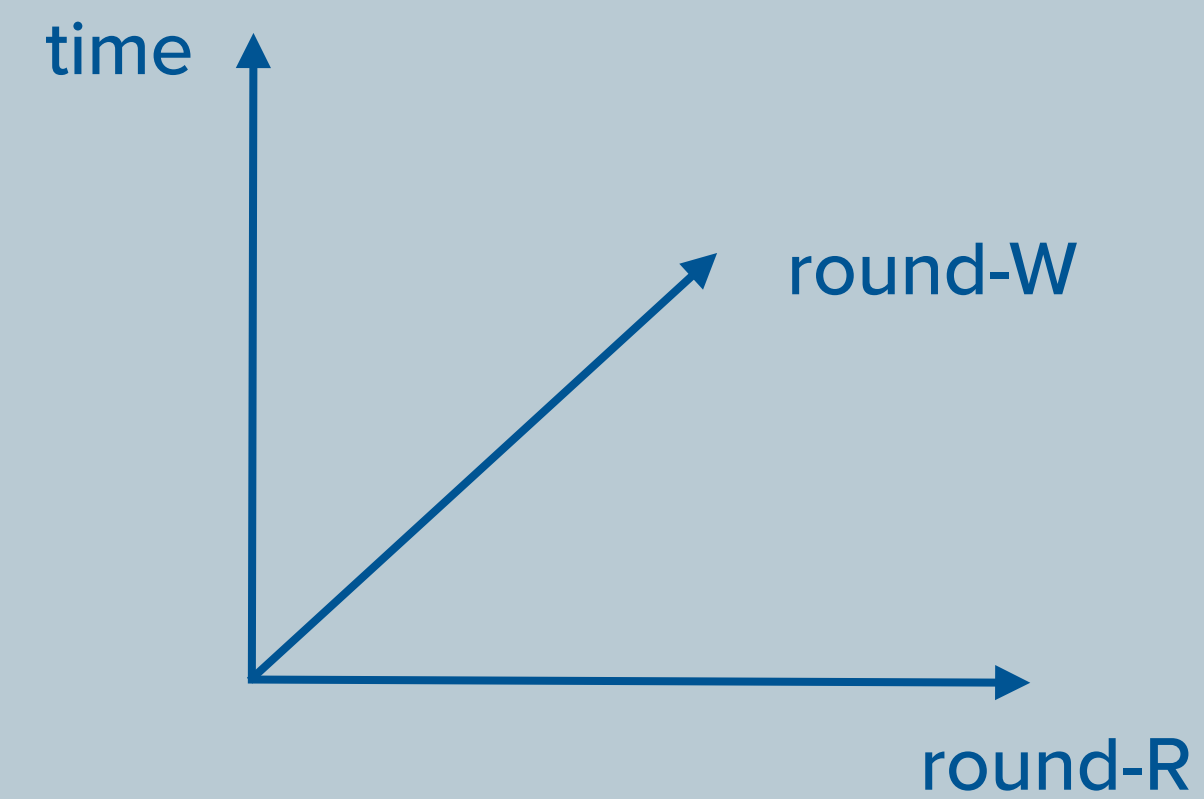
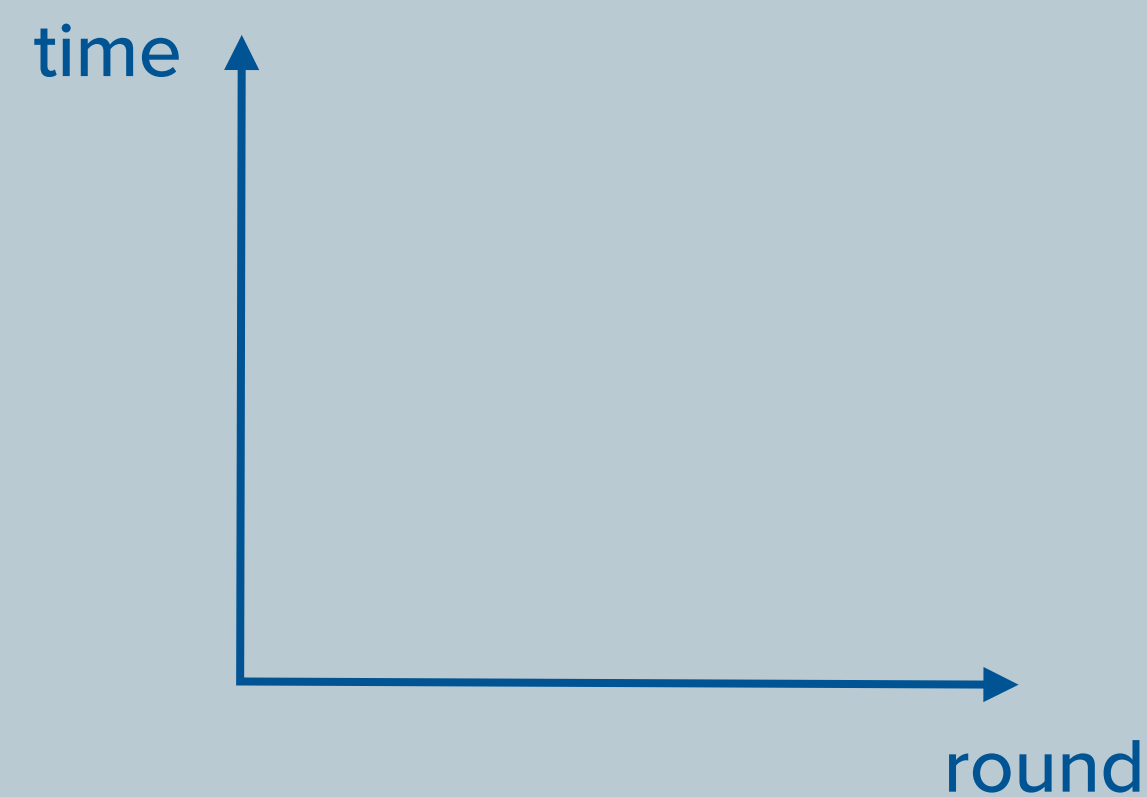
List-Based

TRX

Tree-Based

PAX

Patch-Based



In our work

LSX

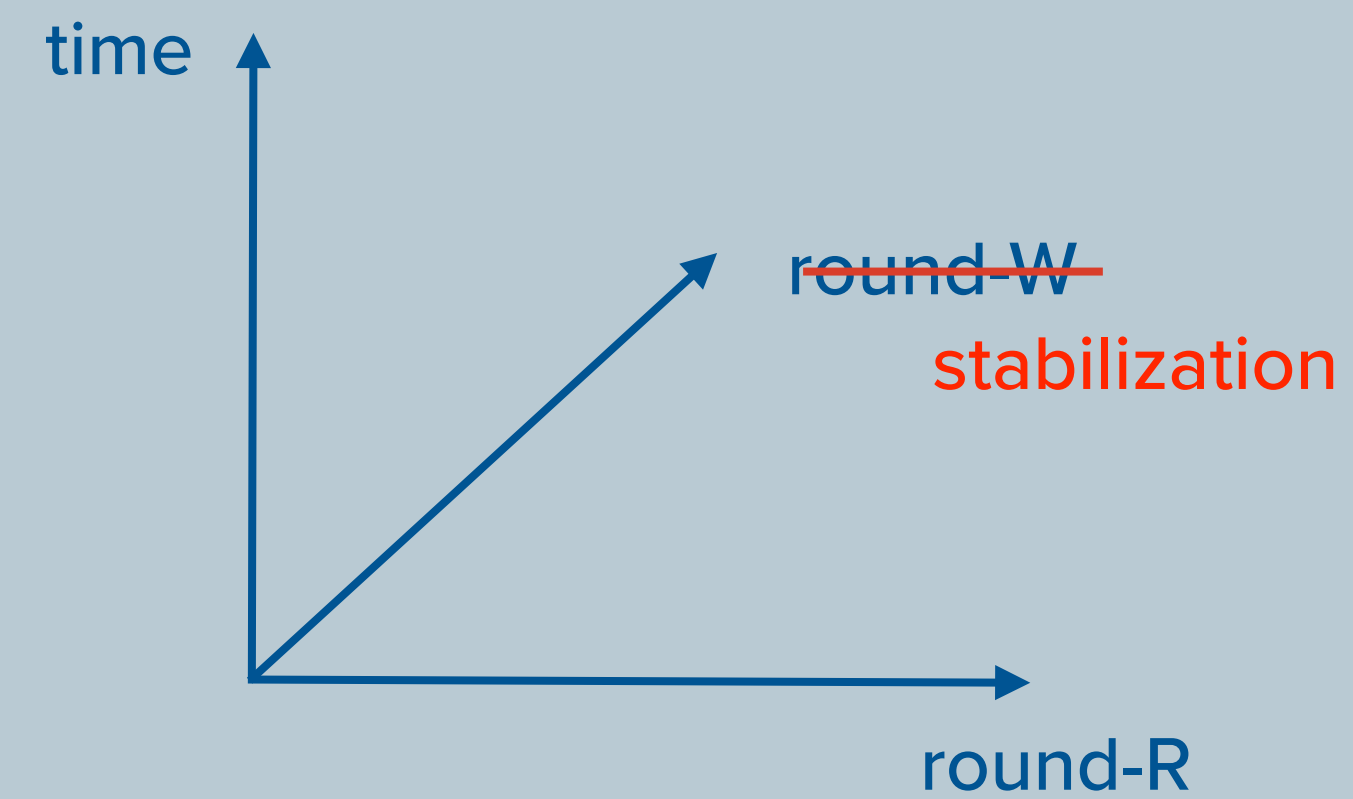
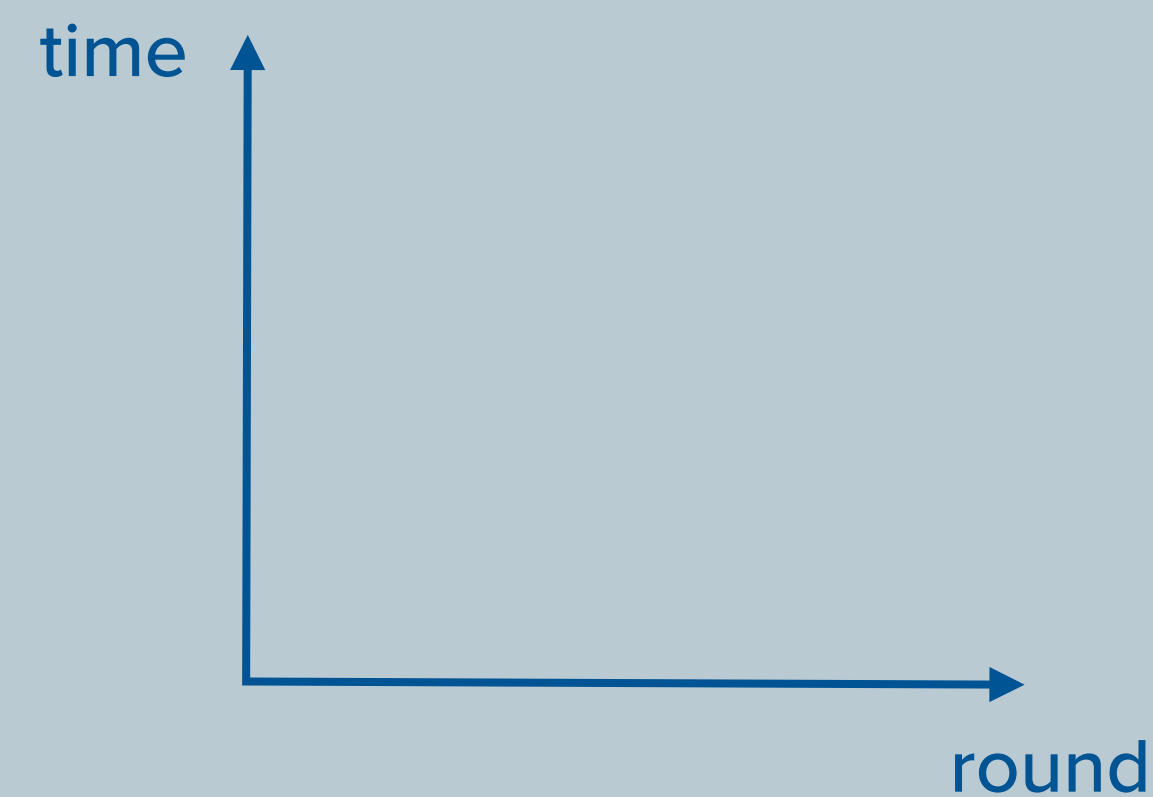
List-Based

TRX

Tree-Based

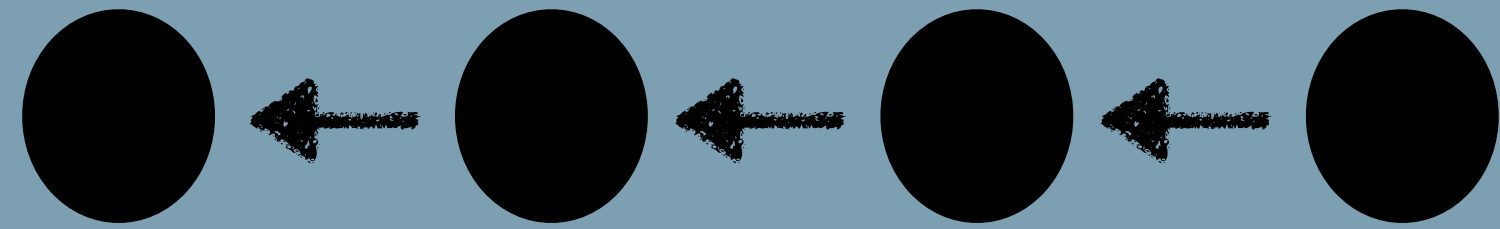
PAX

Patch-Based

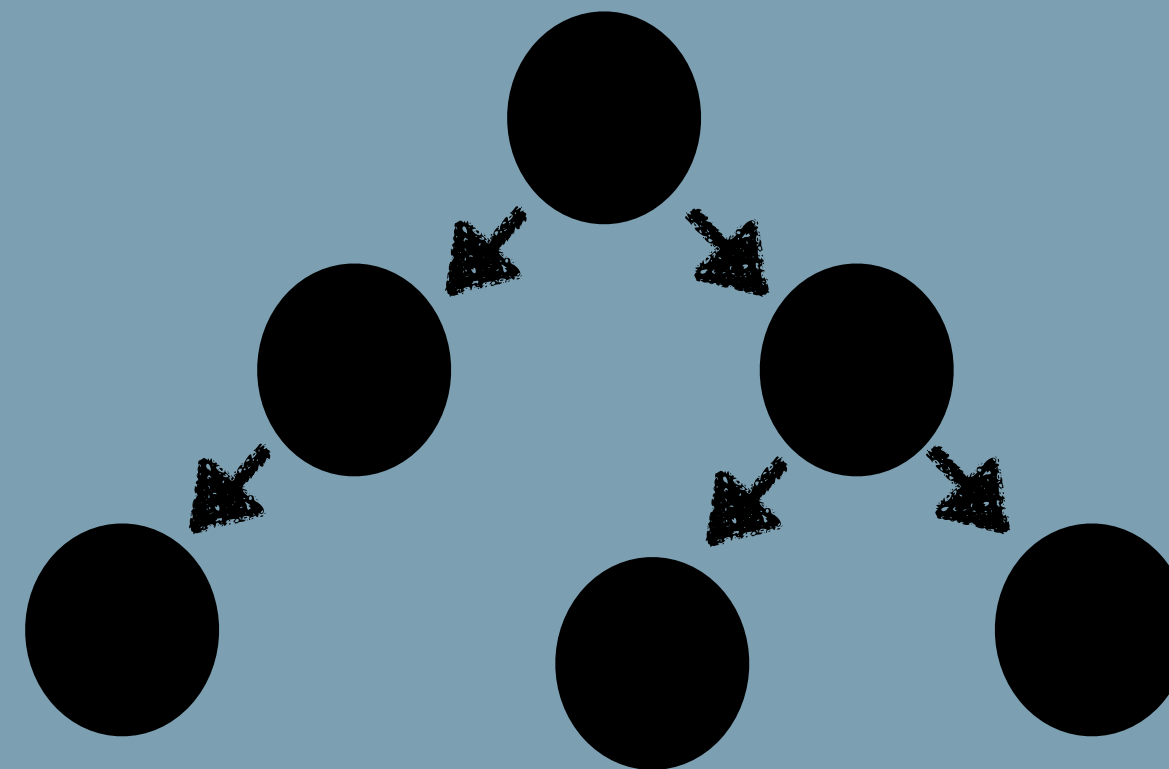
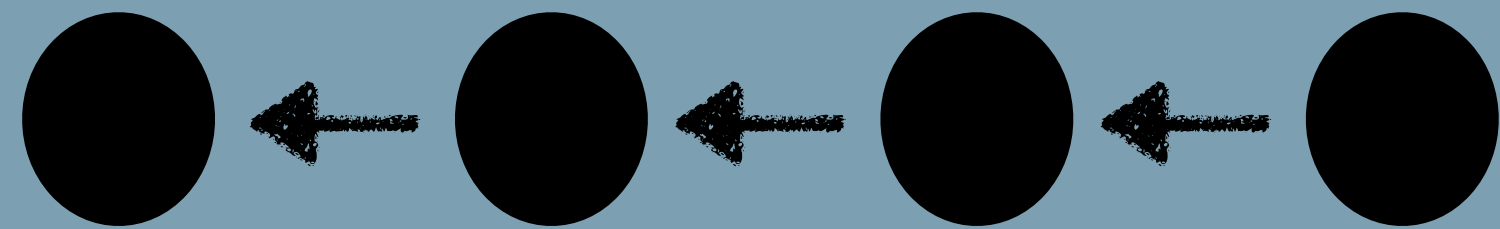


Storing data structures on BCs

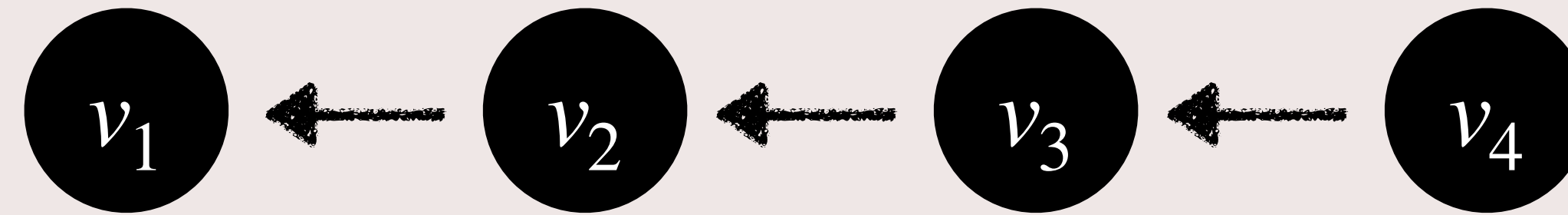
Storing data structures on BCs



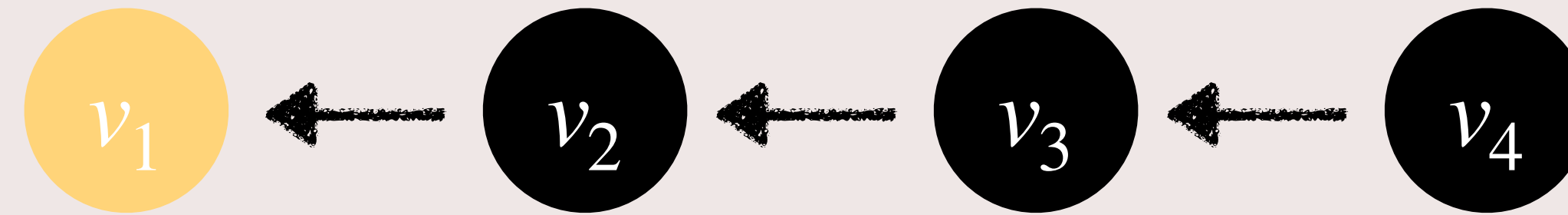
Storing data structures on BCs



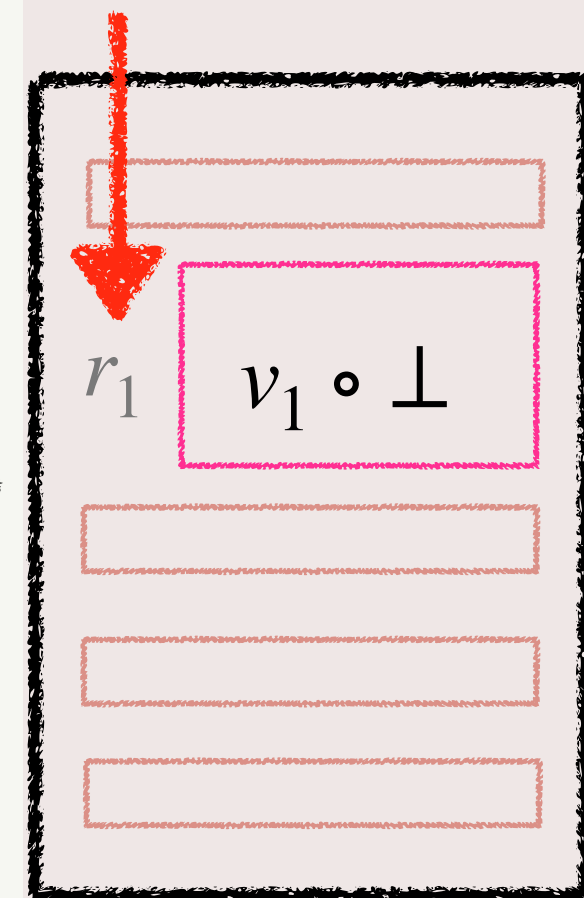
Storing linked-list on BCs



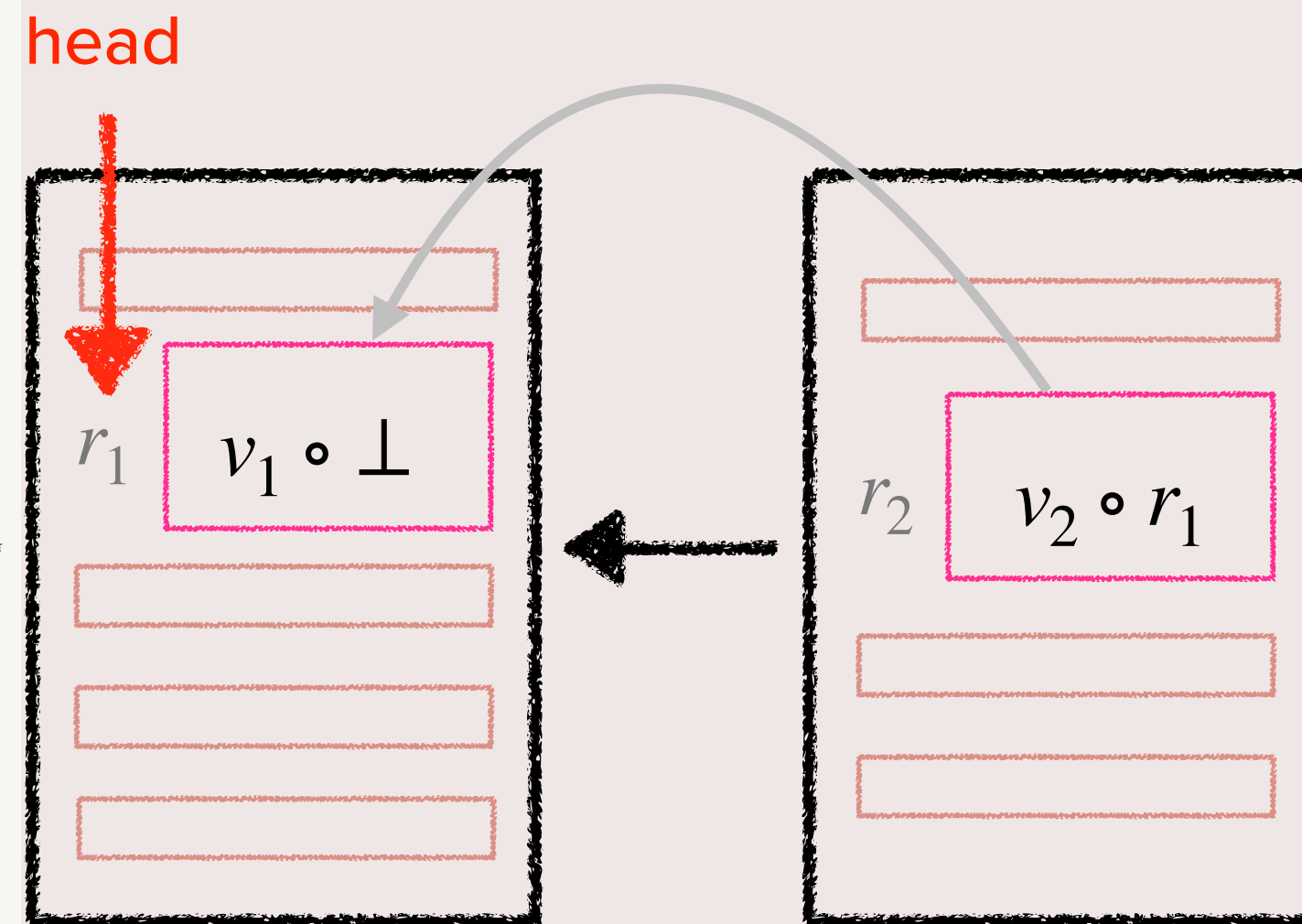
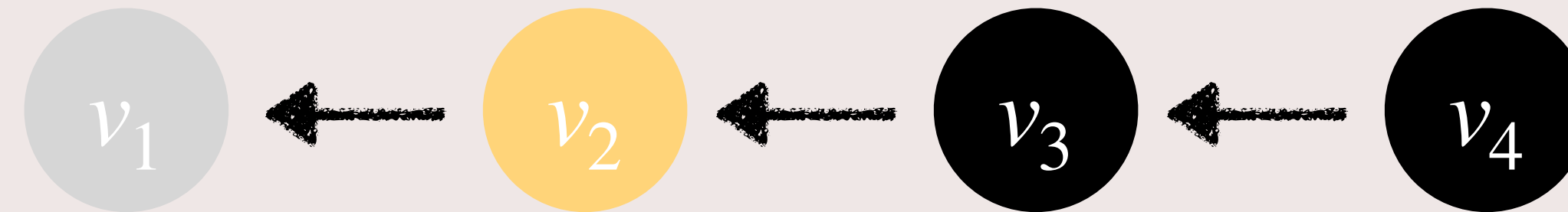
Storing linked-list on BCs



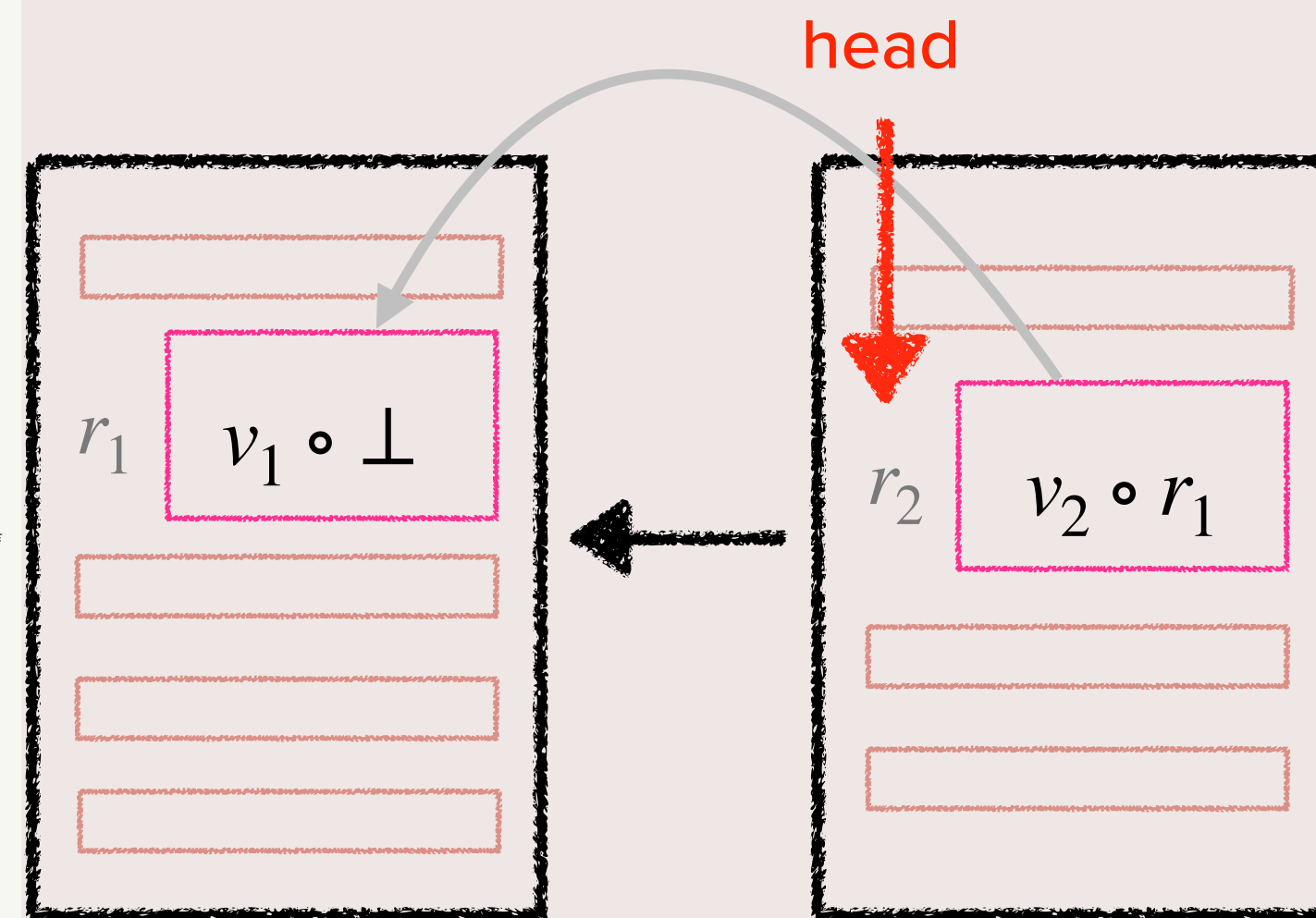
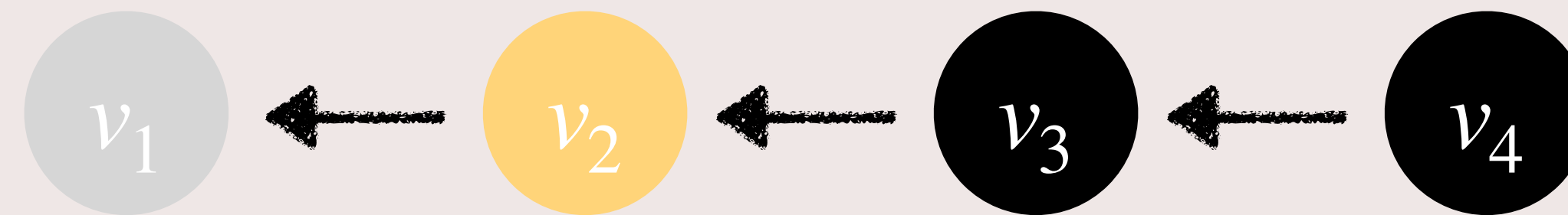
head



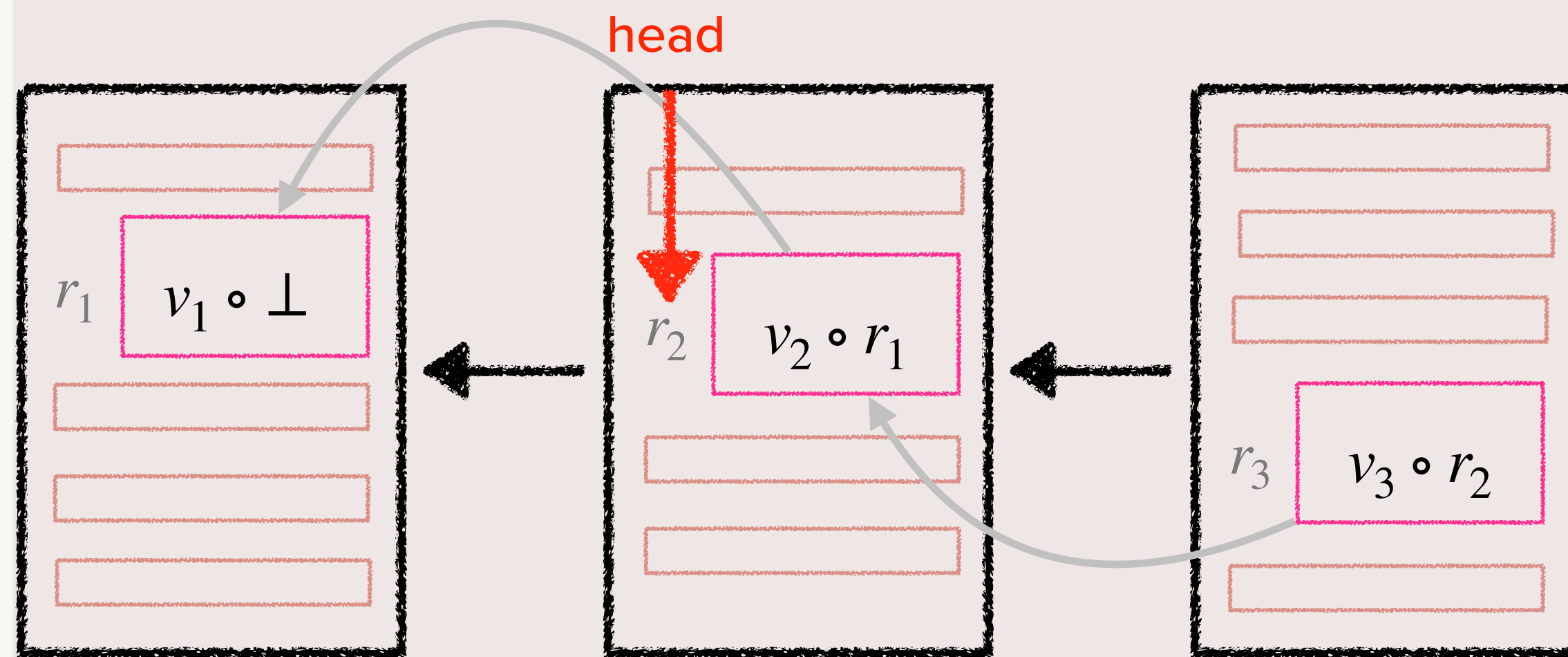
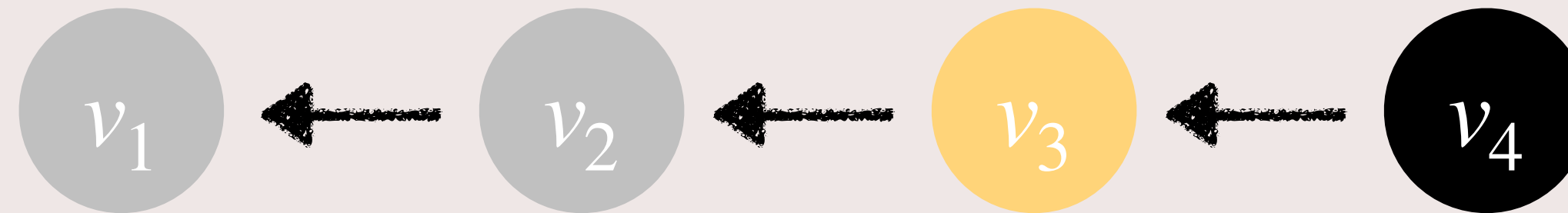
Storing linked-list on BCs



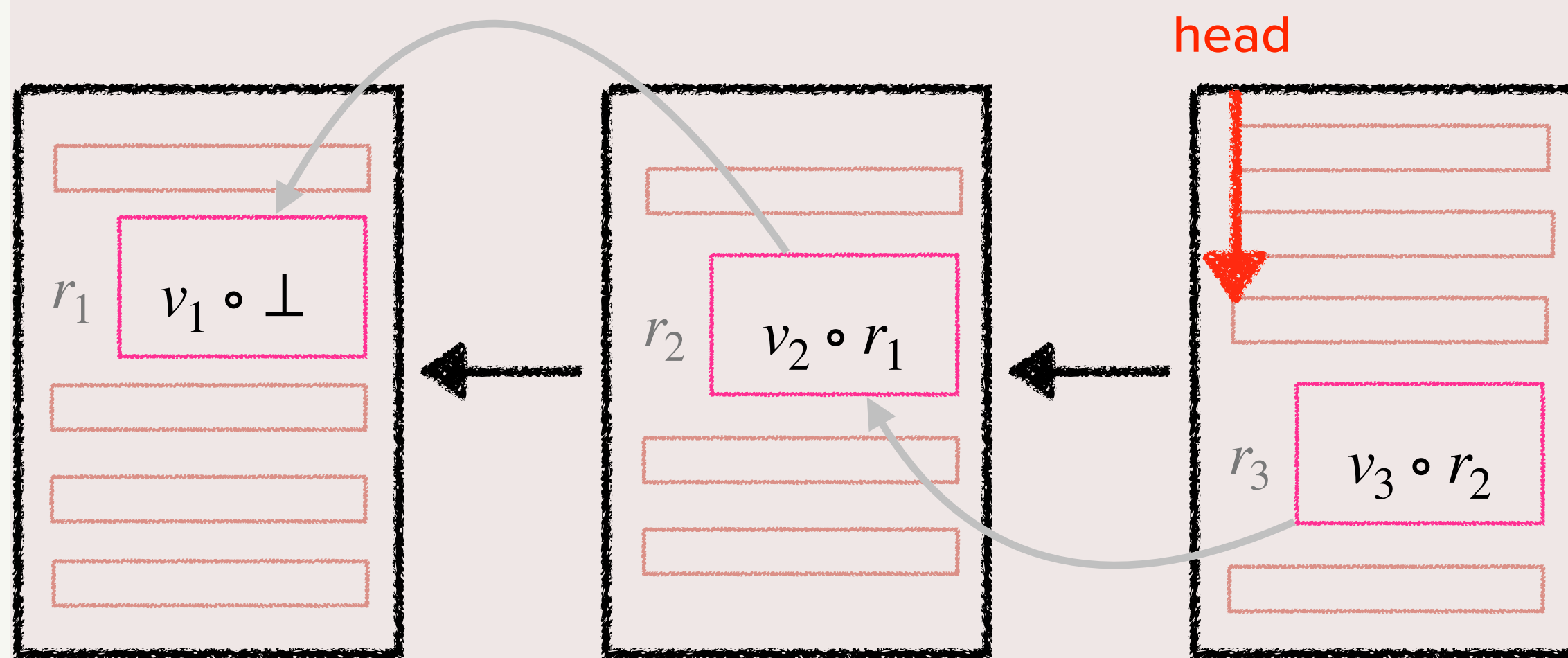
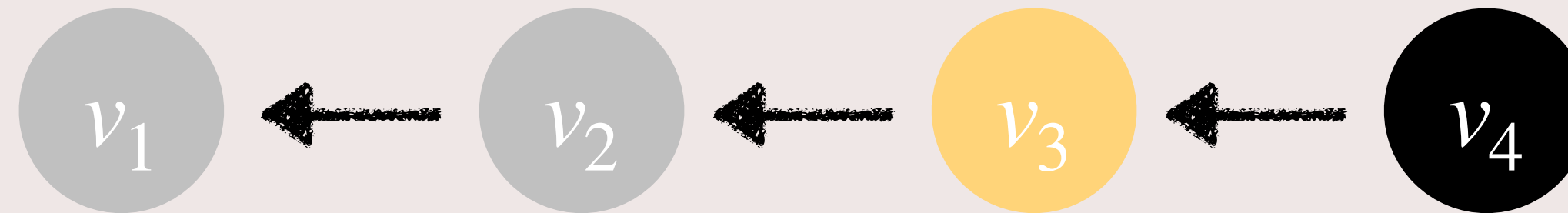
Storing linked-list on BCs



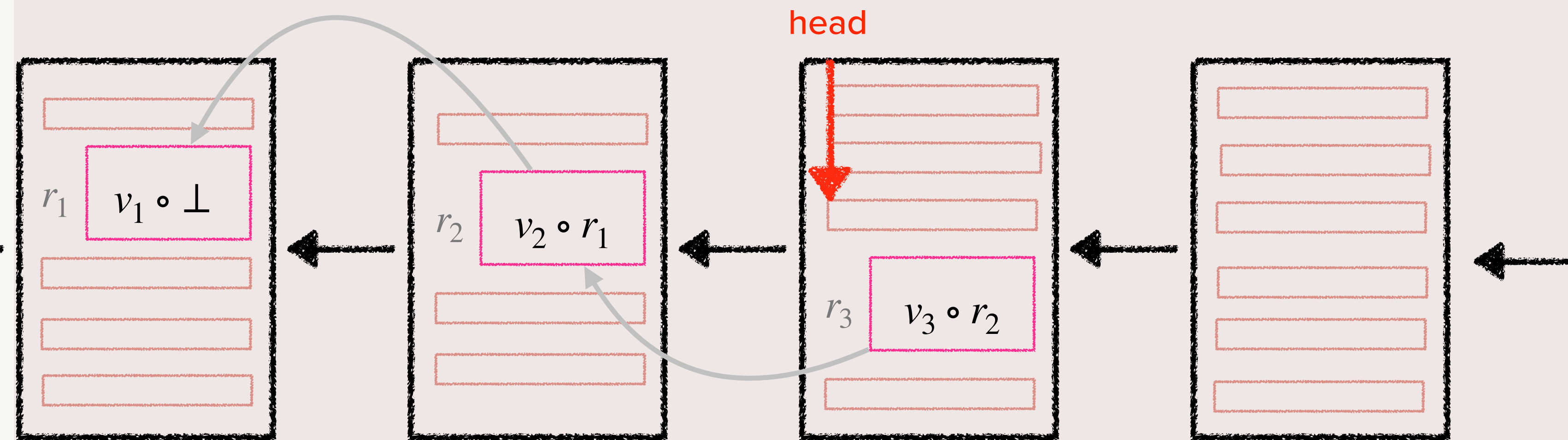
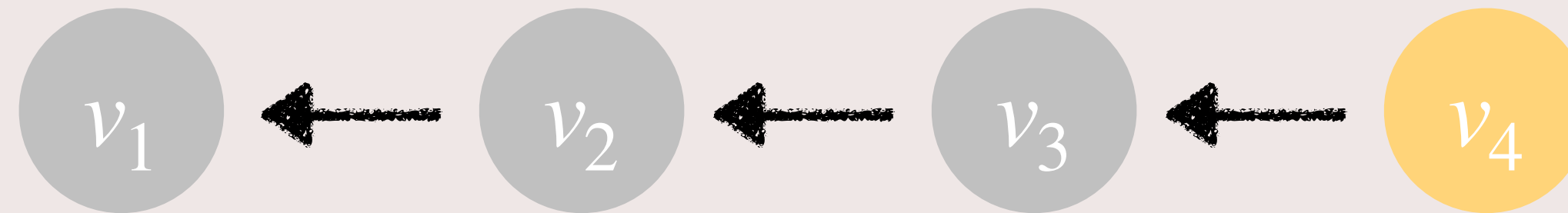
Storing linked-list on BCs



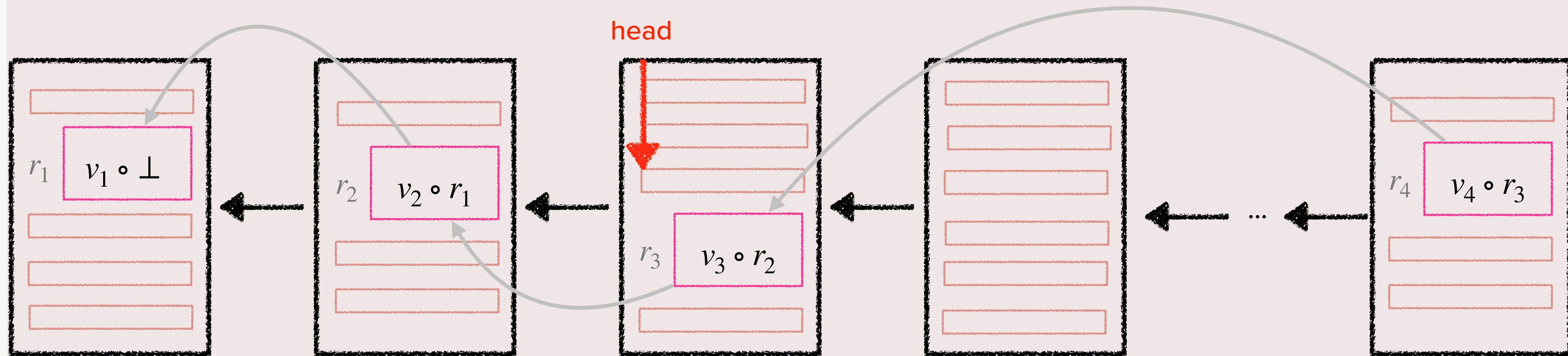
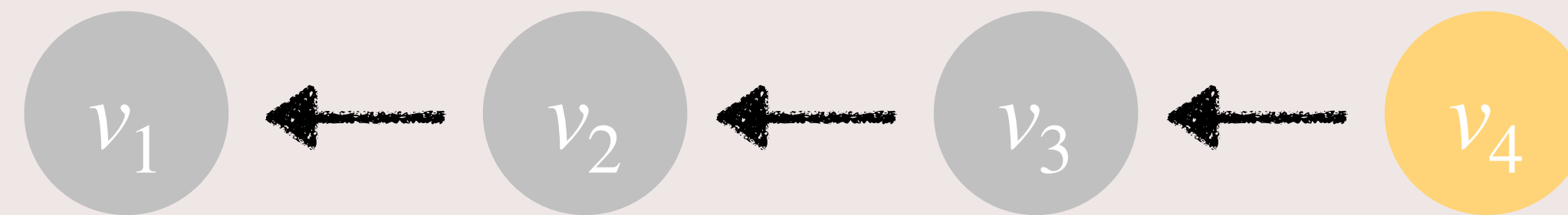
Storing linked-list on BCs



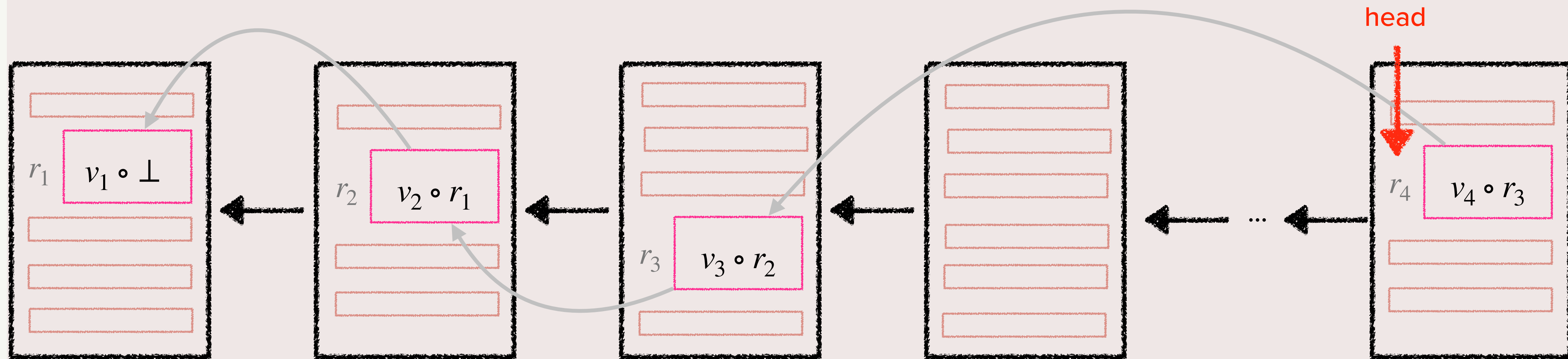
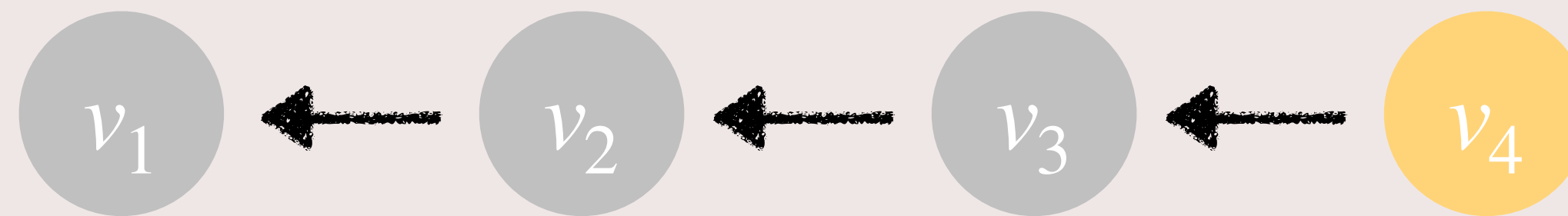
Storing linked-list on BCs



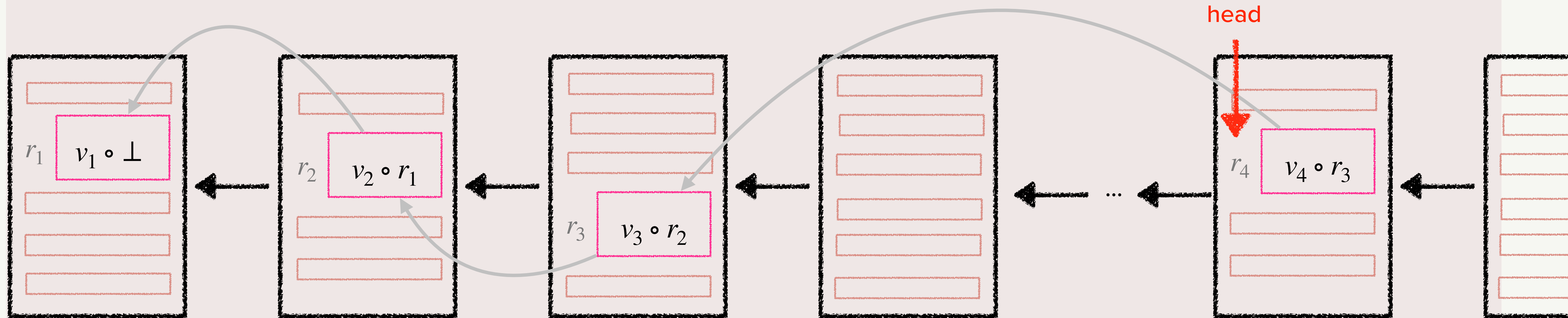
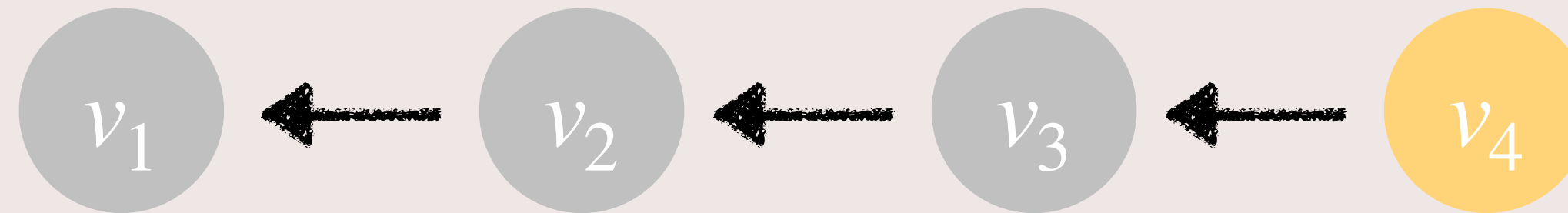
Storing linked-list on BCs



Storing linked-list on BCs



Storing linked-list on BCs



Stabilization Complexity

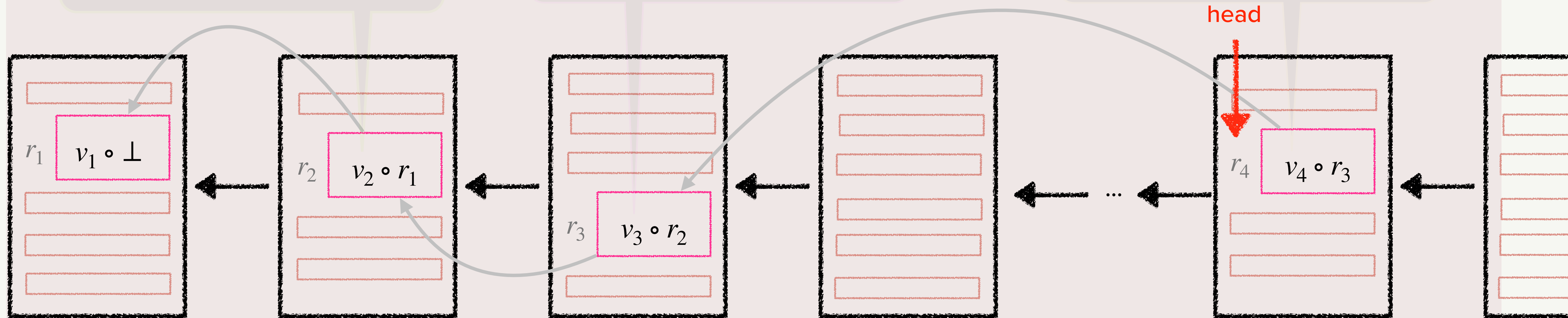
(aka number of write rounds)

number of values in linked-list

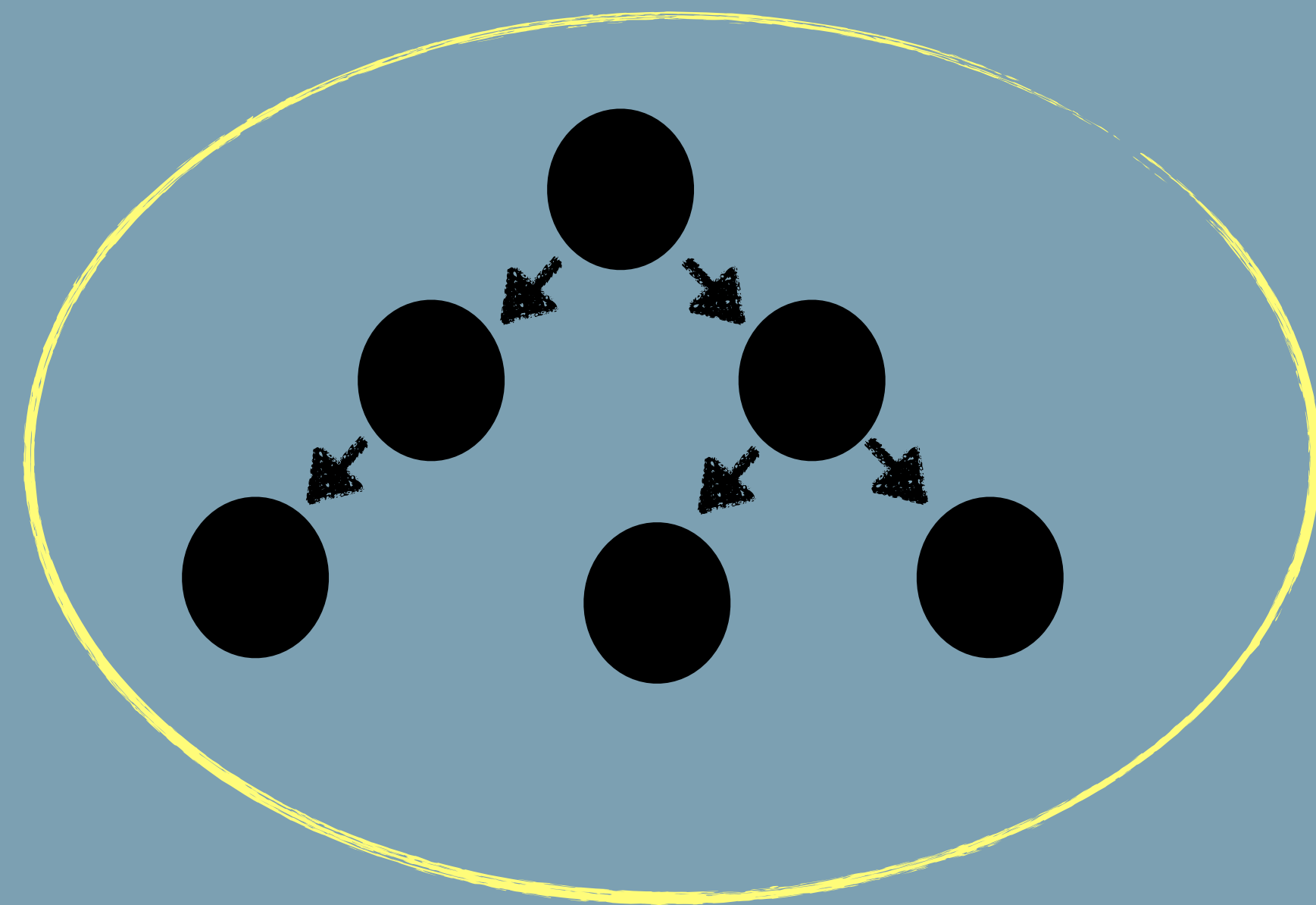
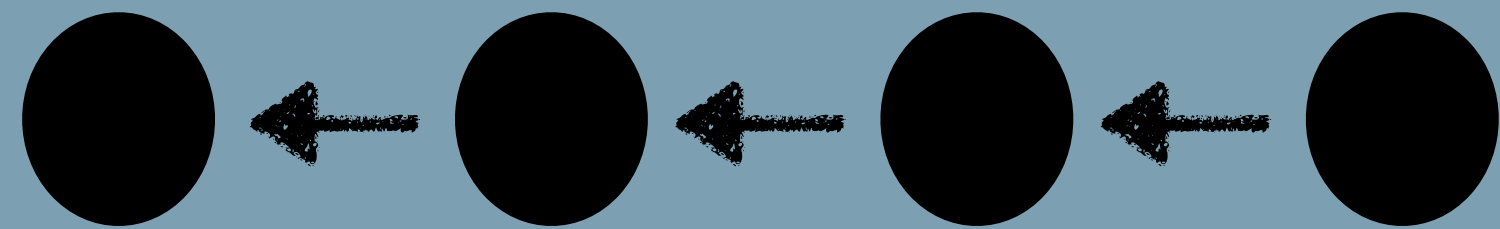
v_2 can't be stored until address of v_1 is known

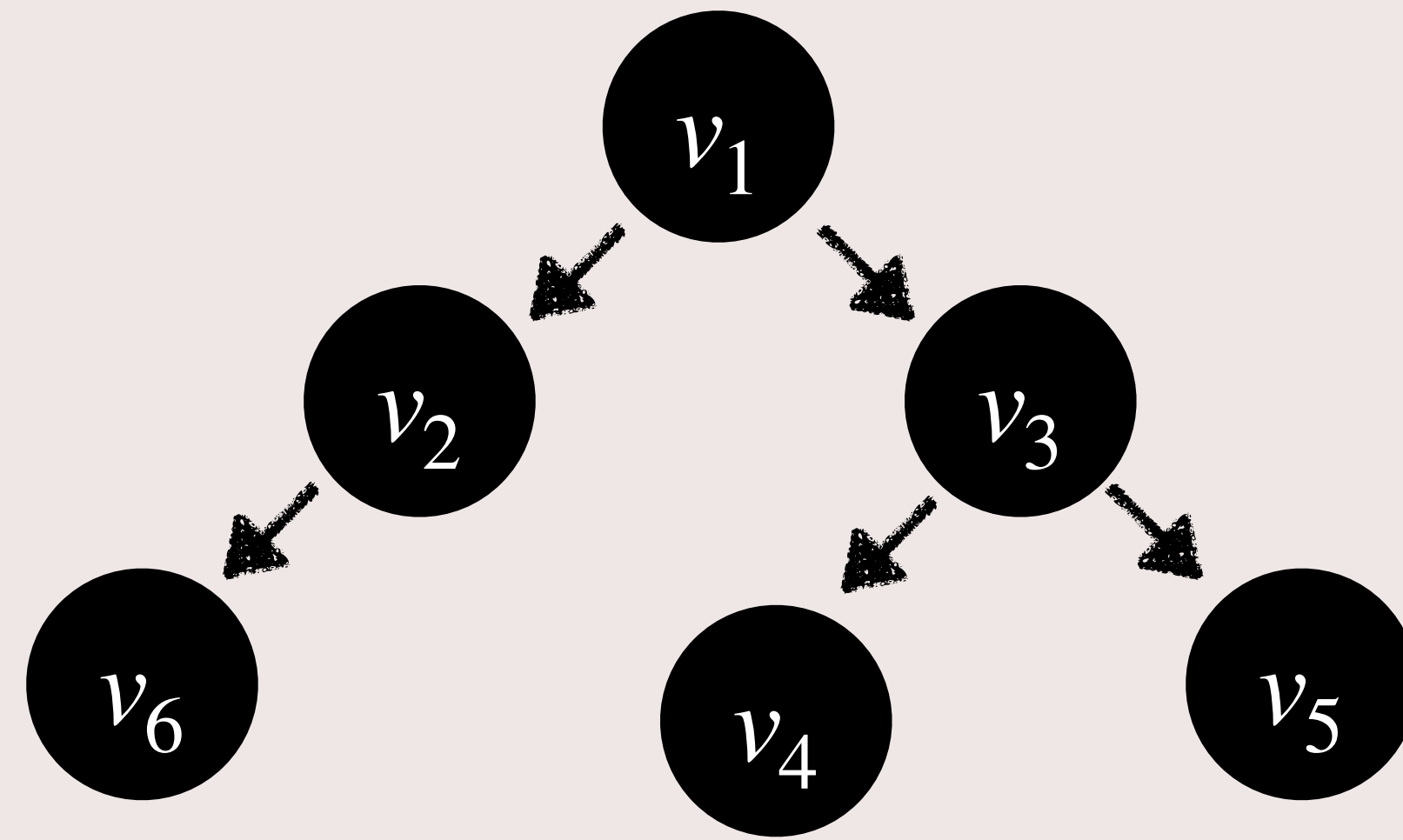
the start address of v_2 is known

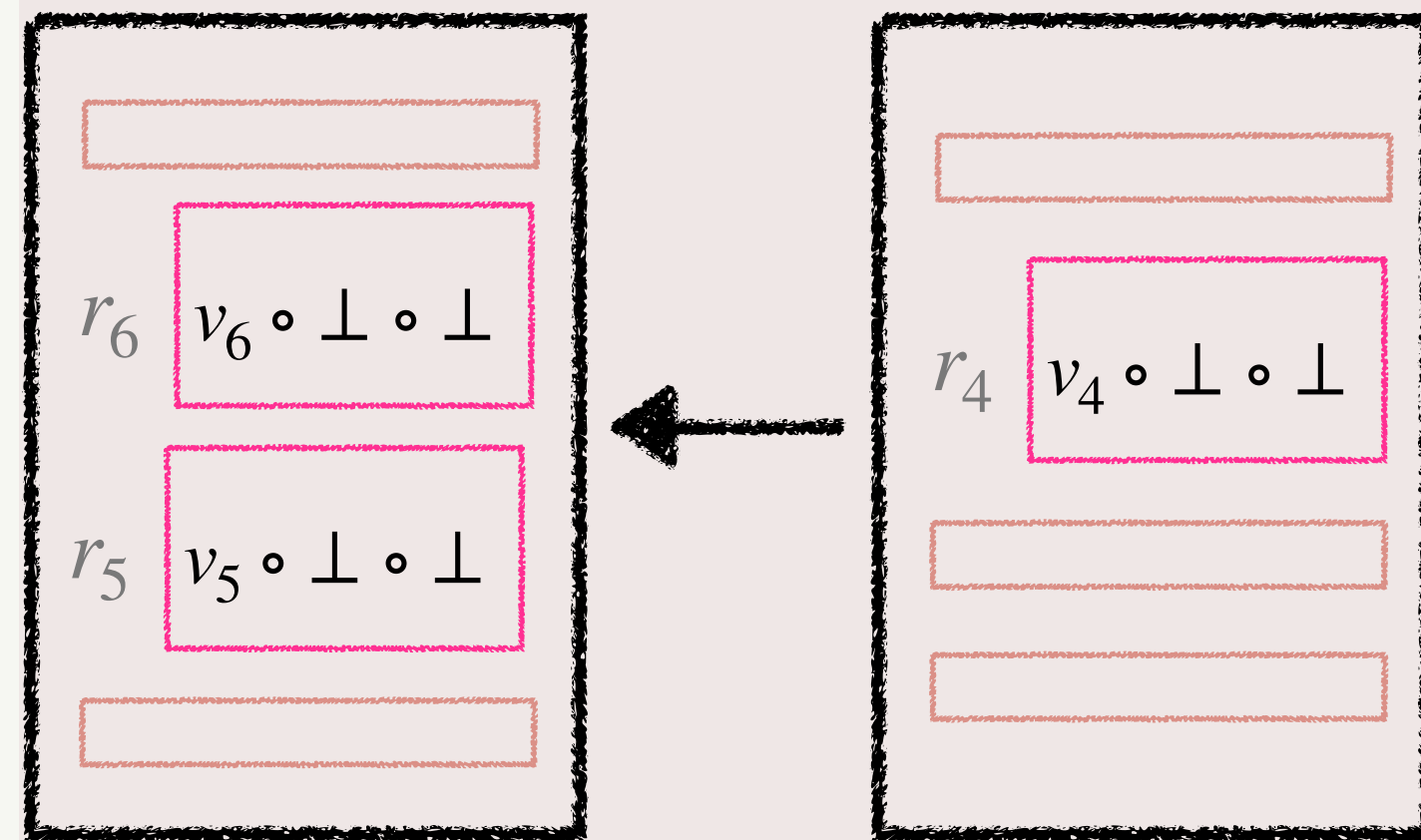
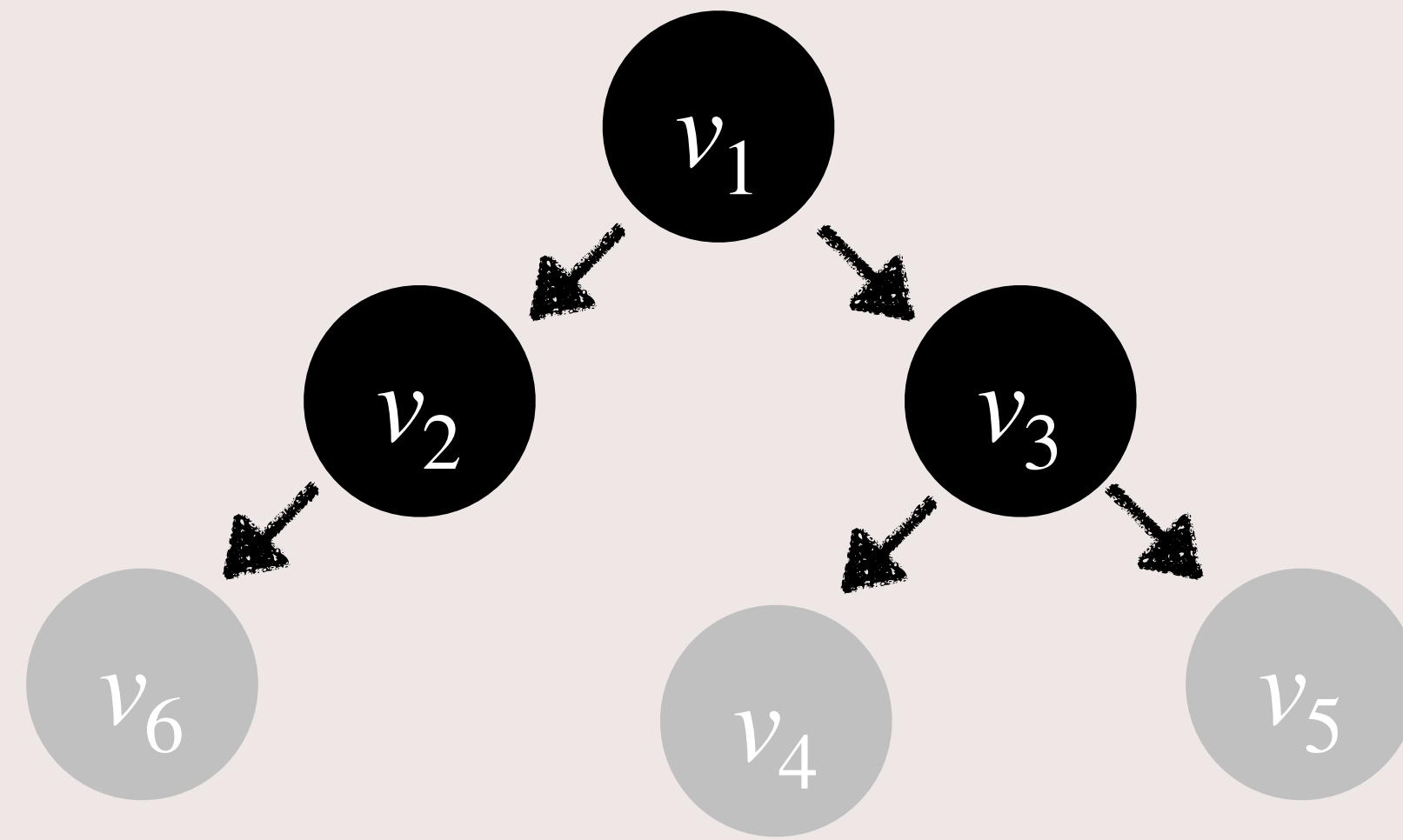
be stored until address of v_3 is known

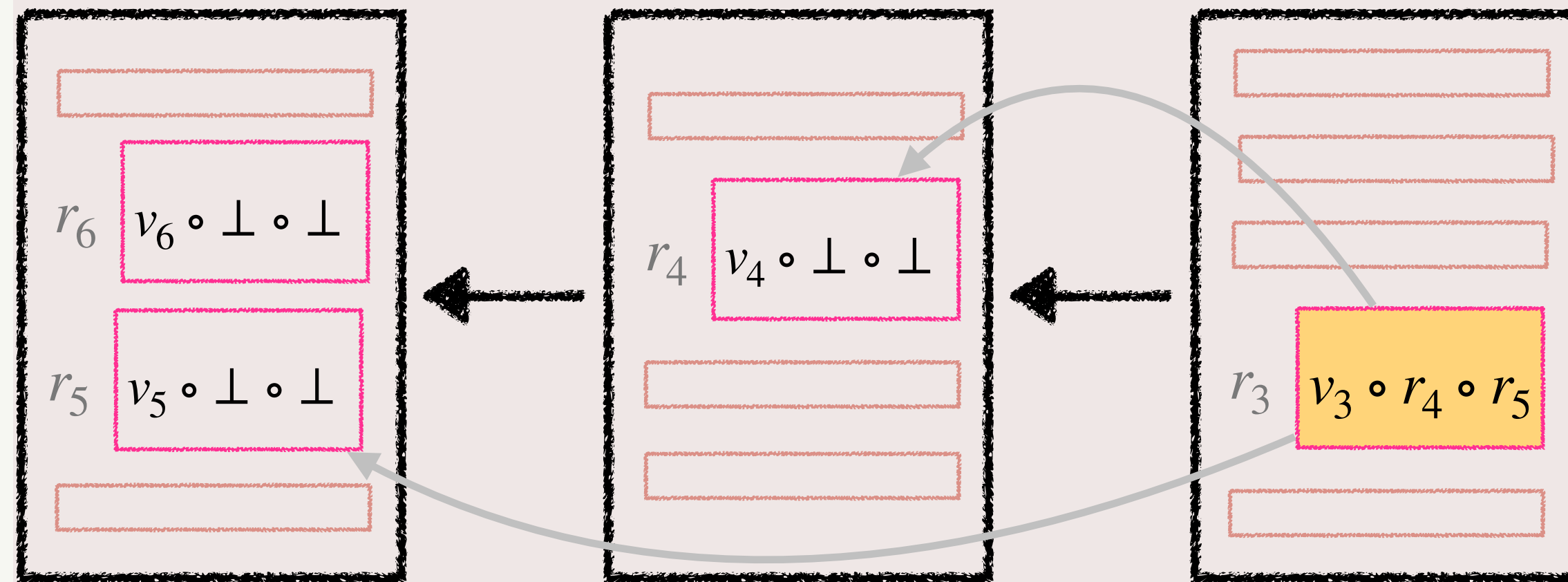
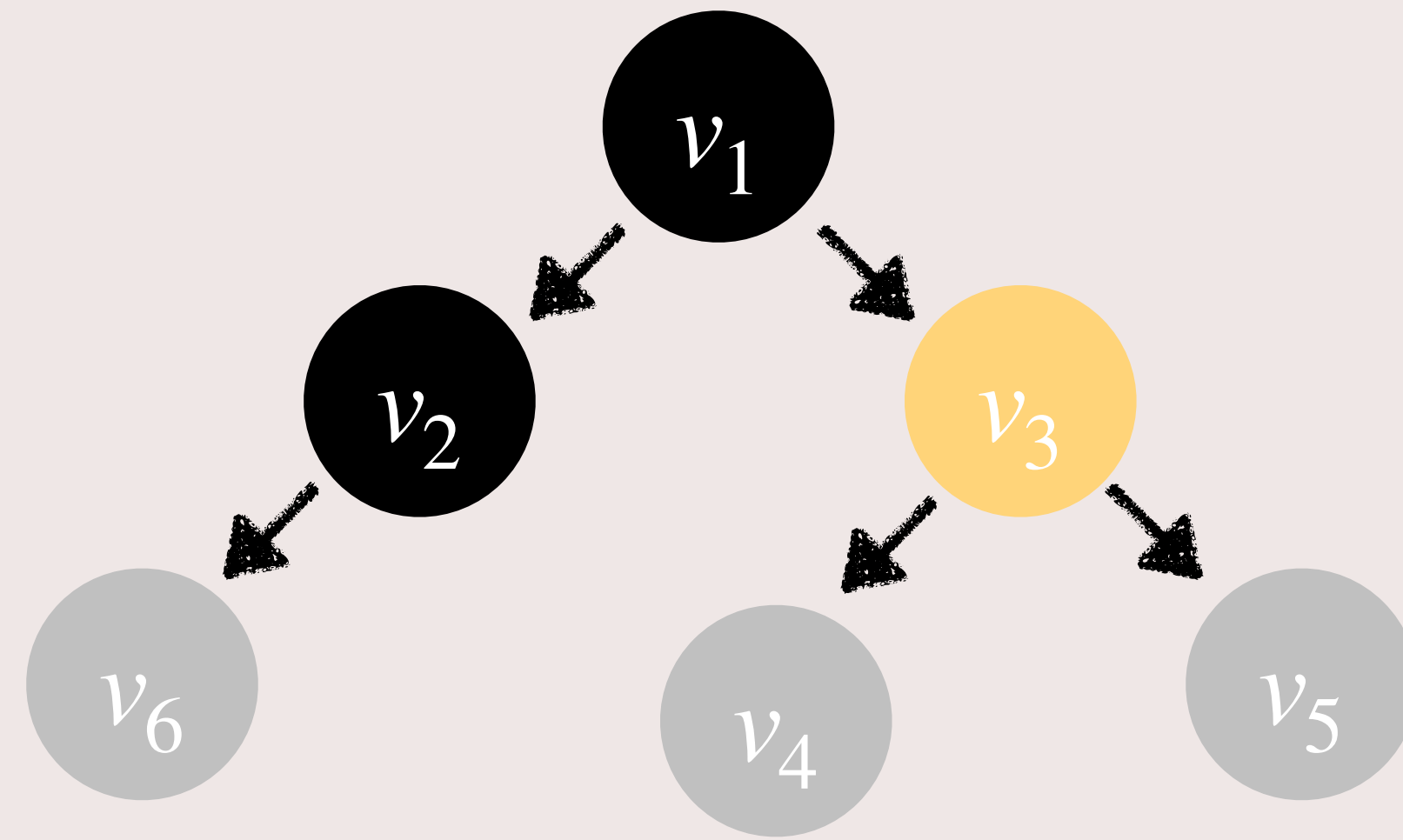


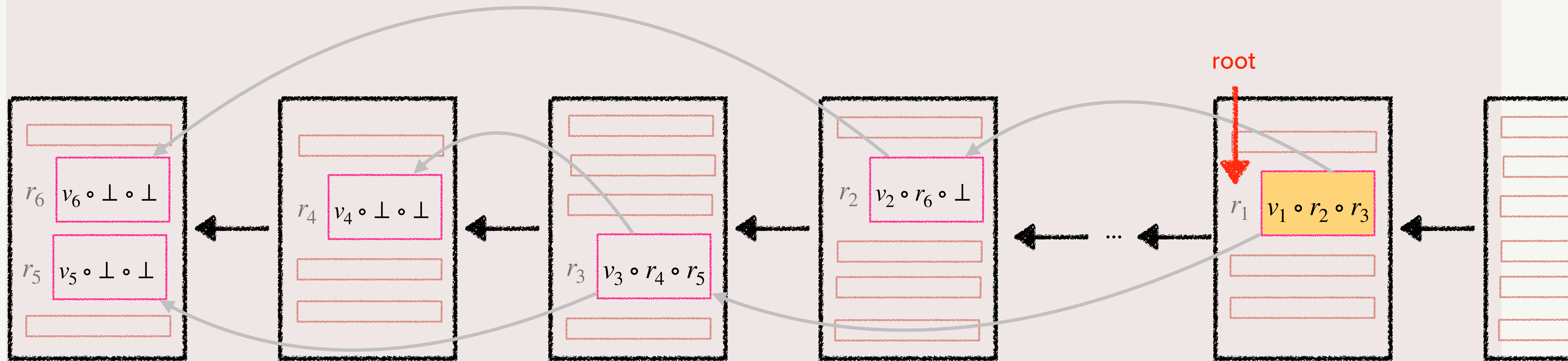
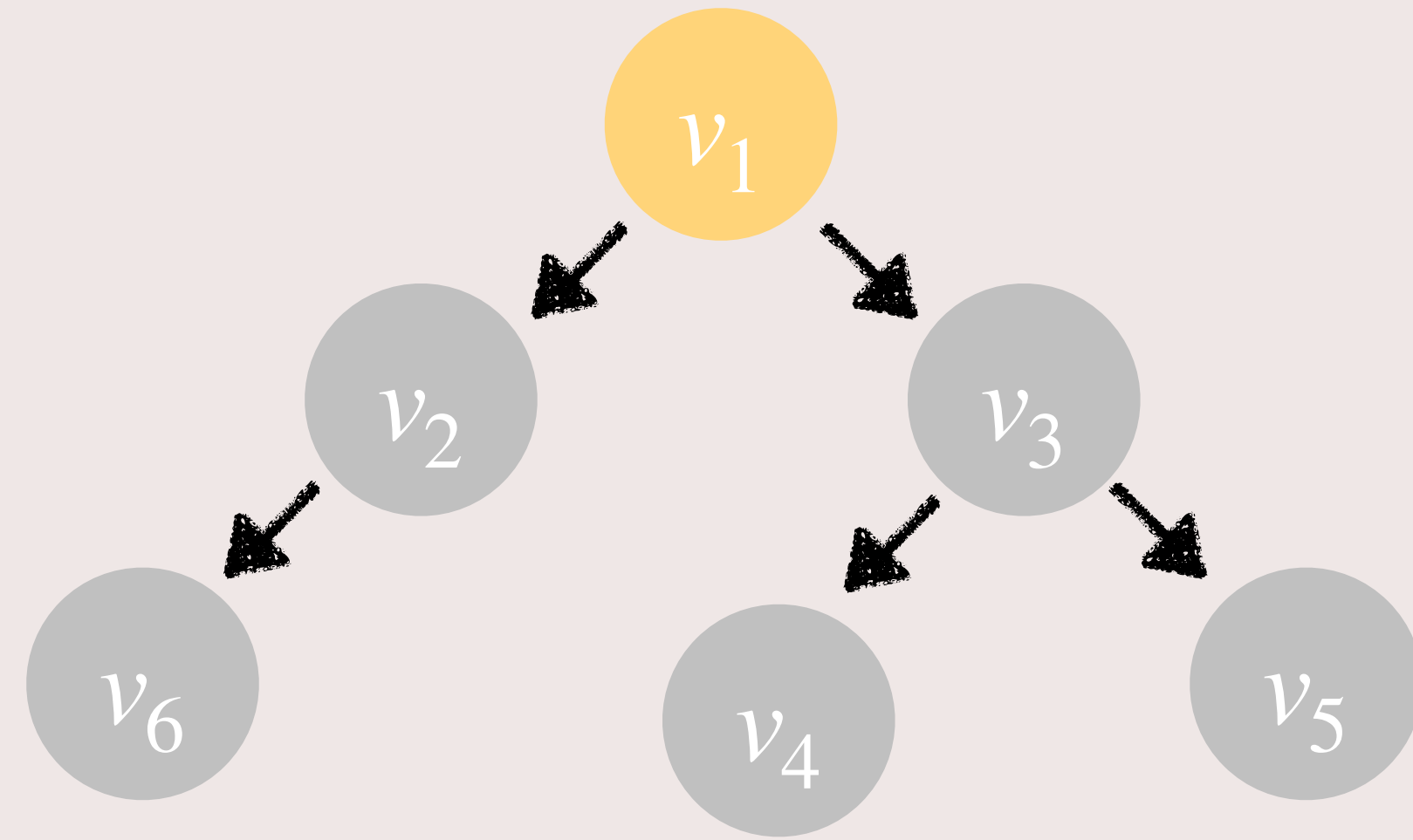
Storing data structures on BCs

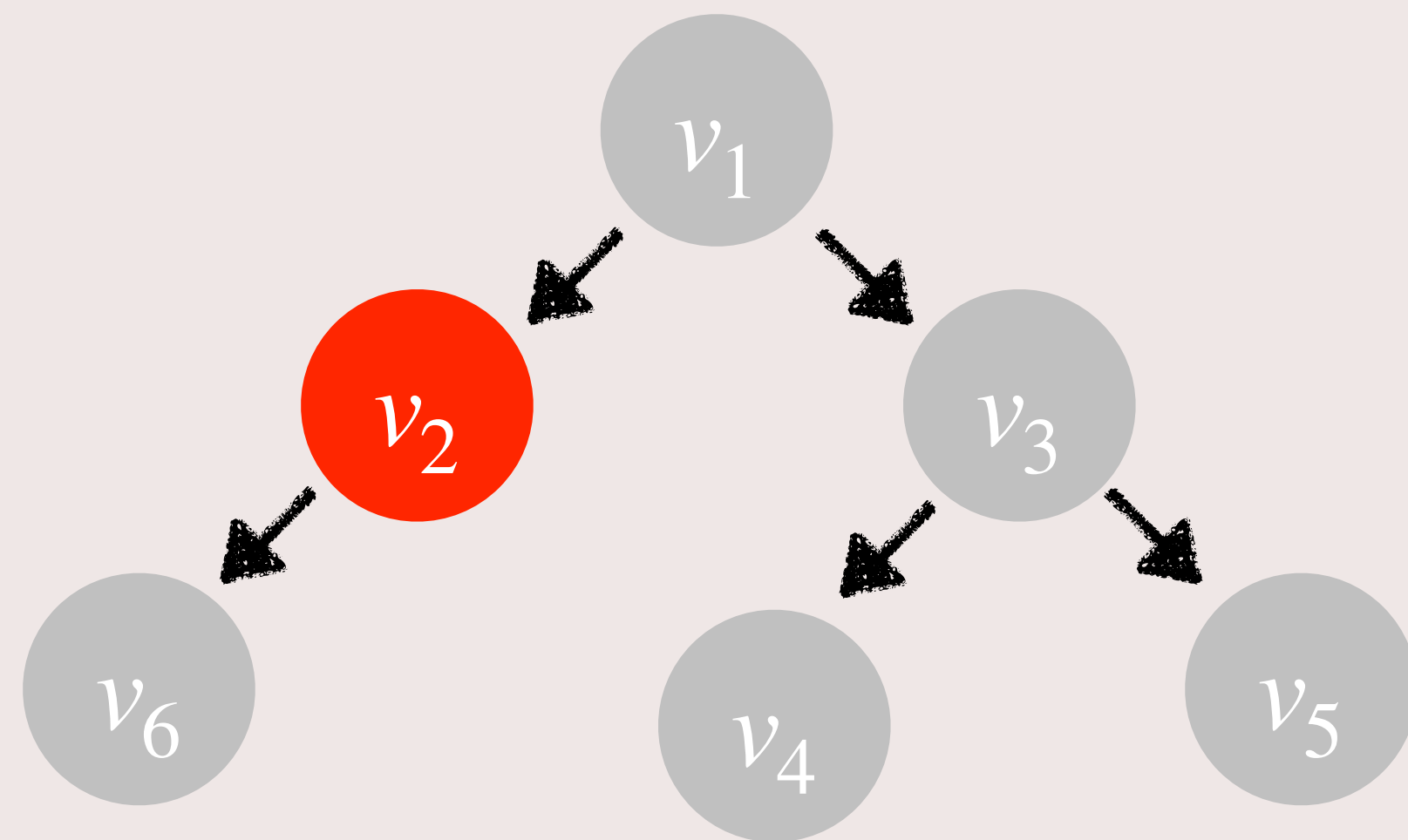




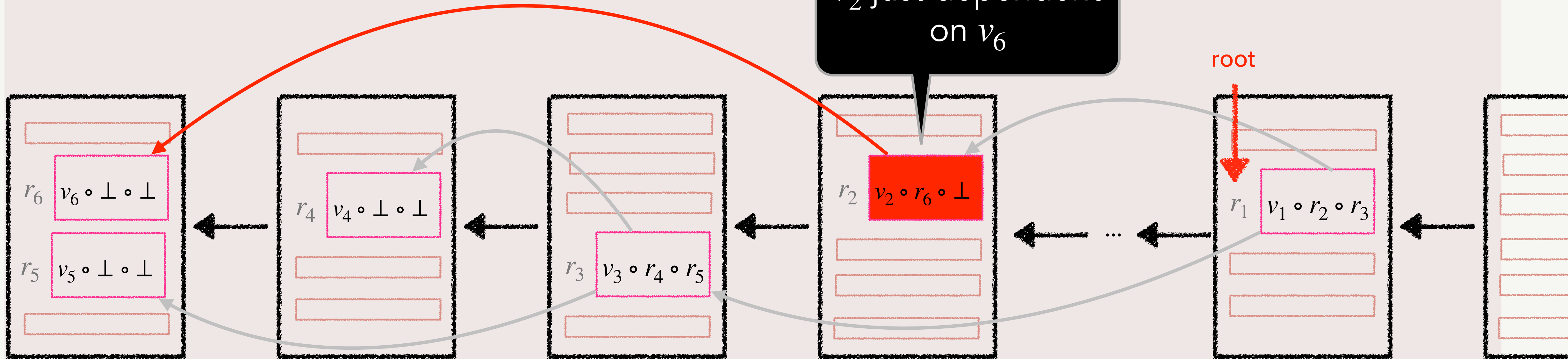




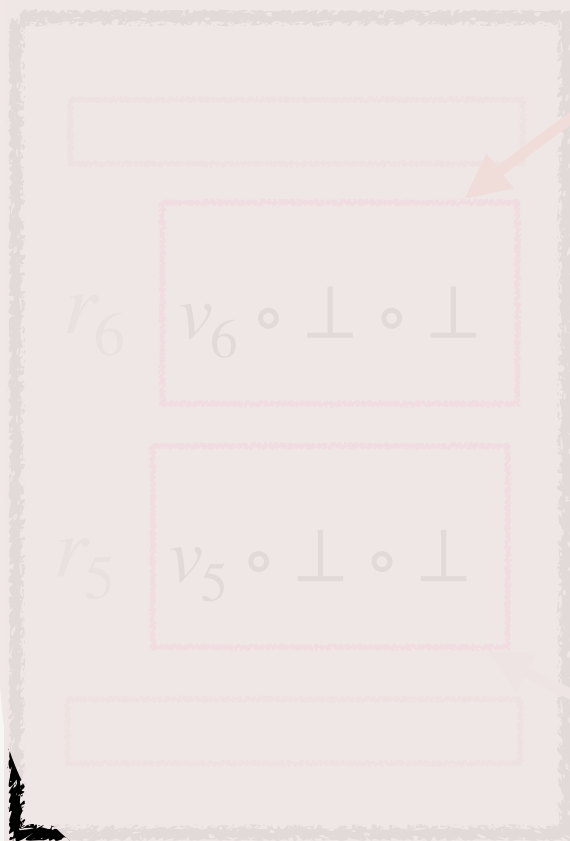
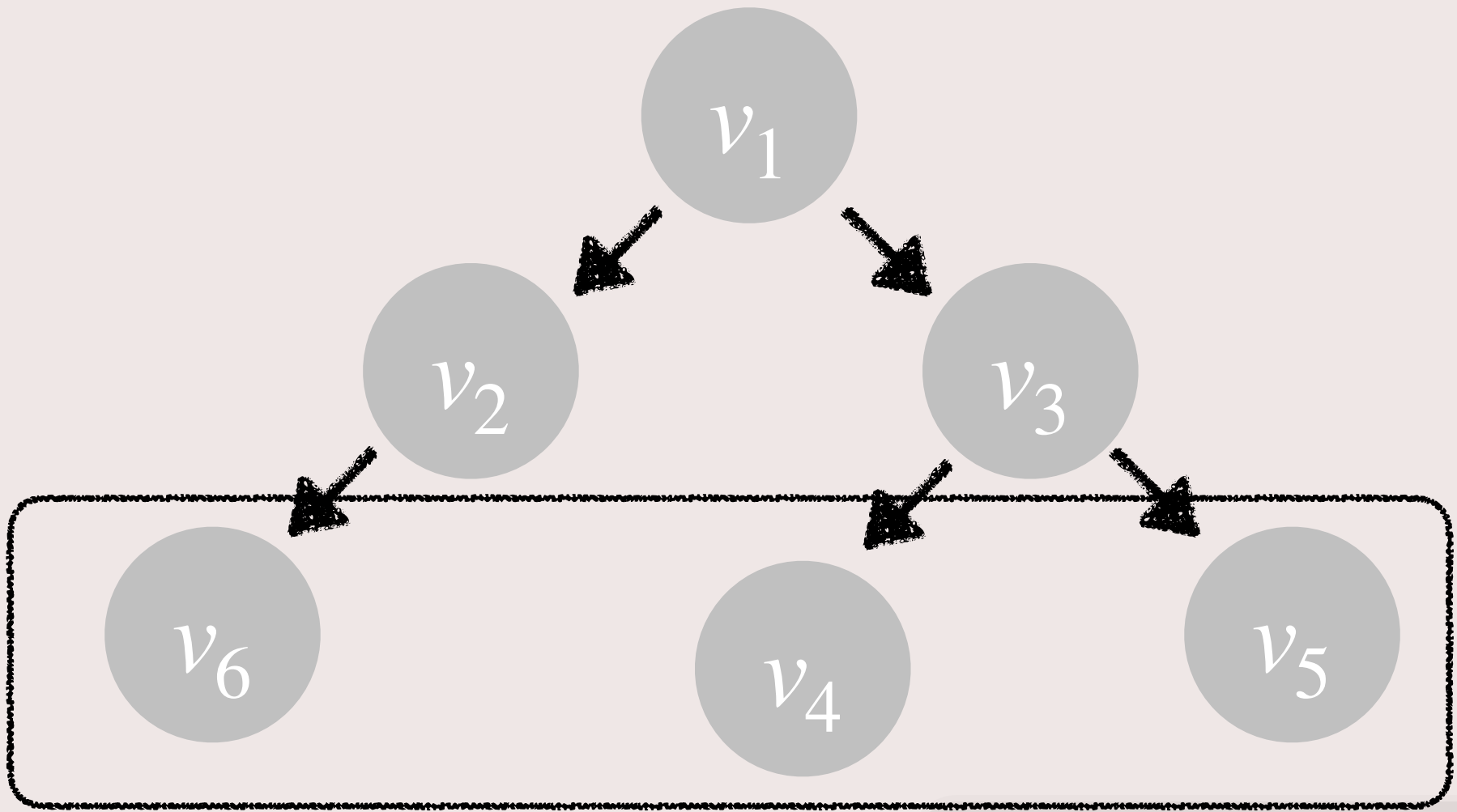




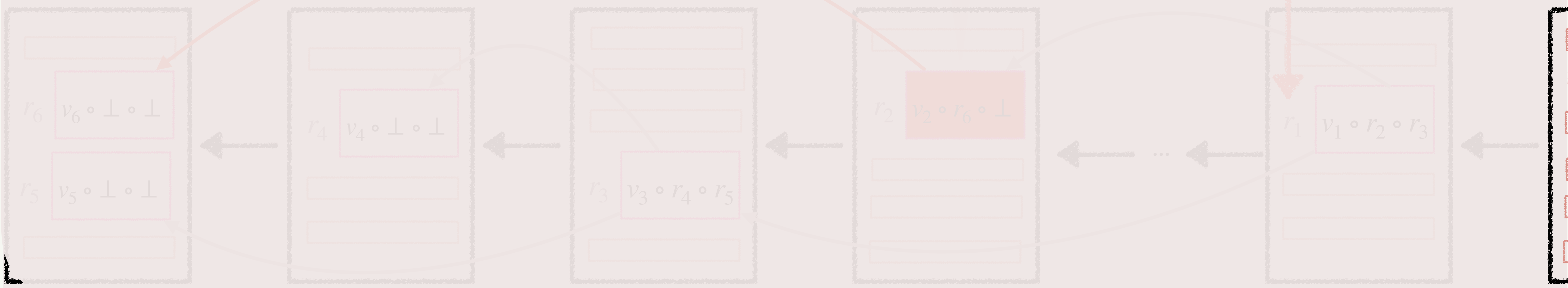
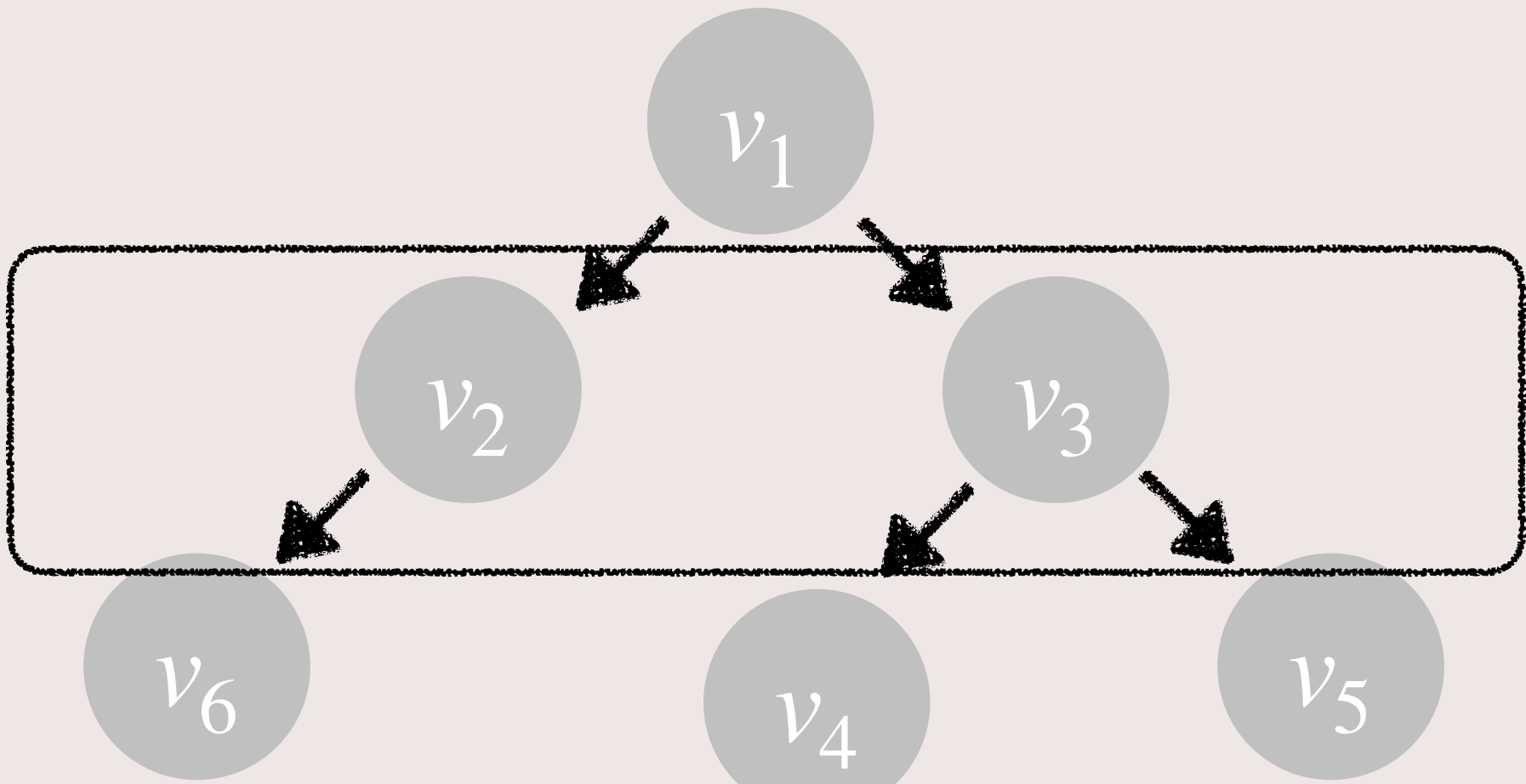
v_2 just dependent on v_6



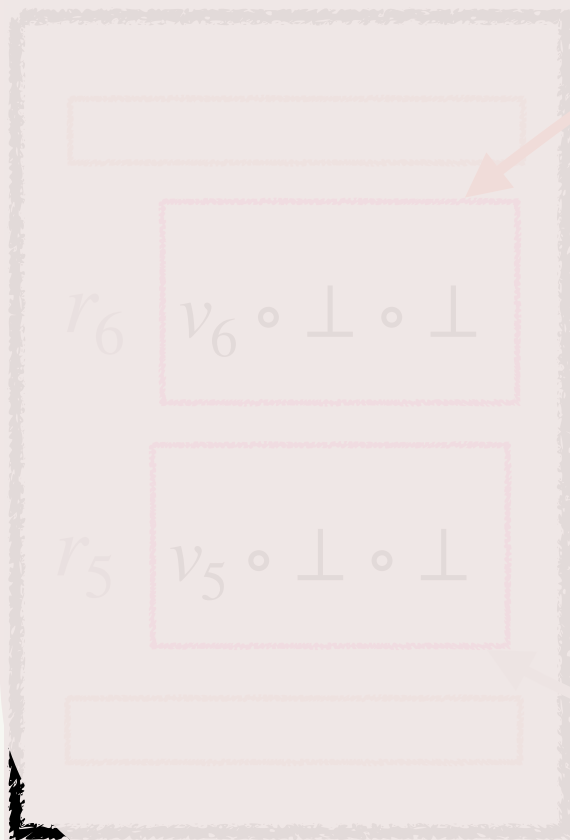
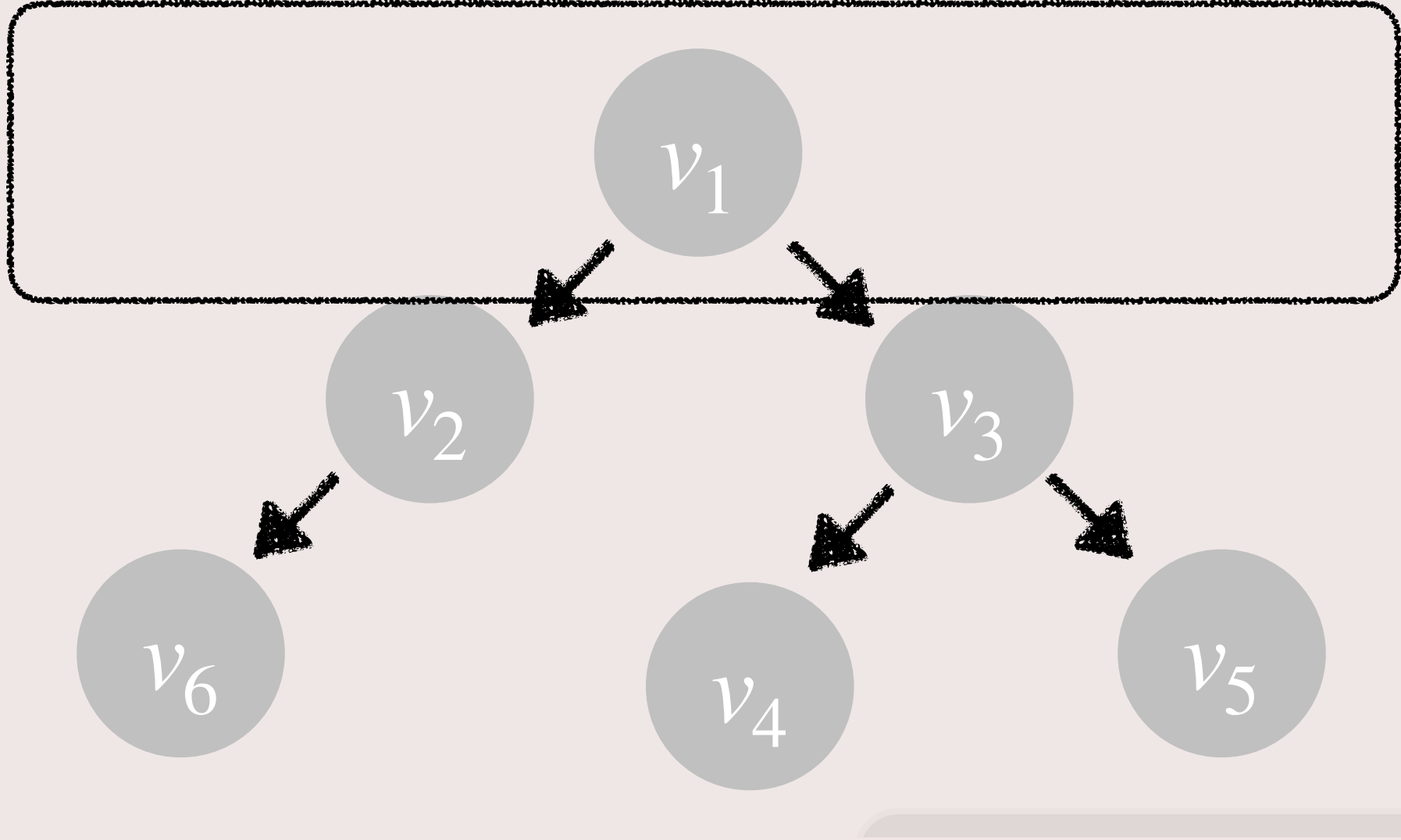
Written in parallel



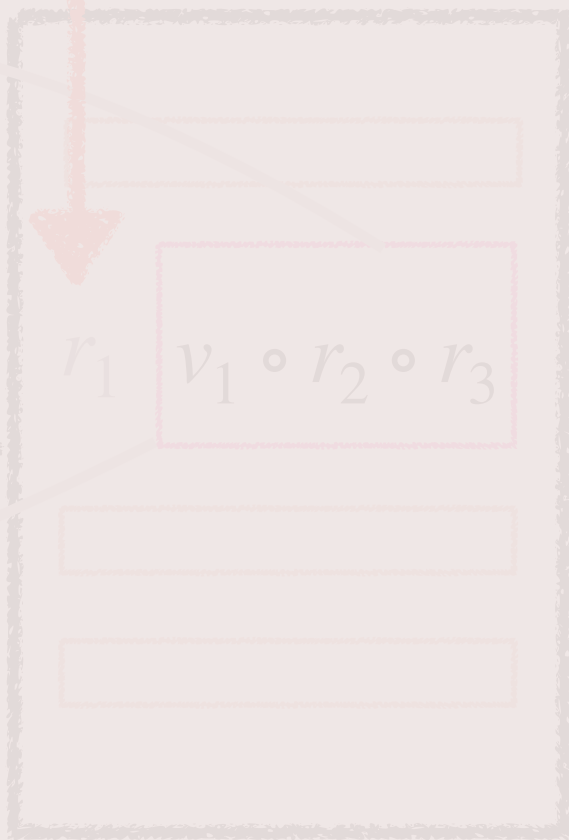
Written in parallel

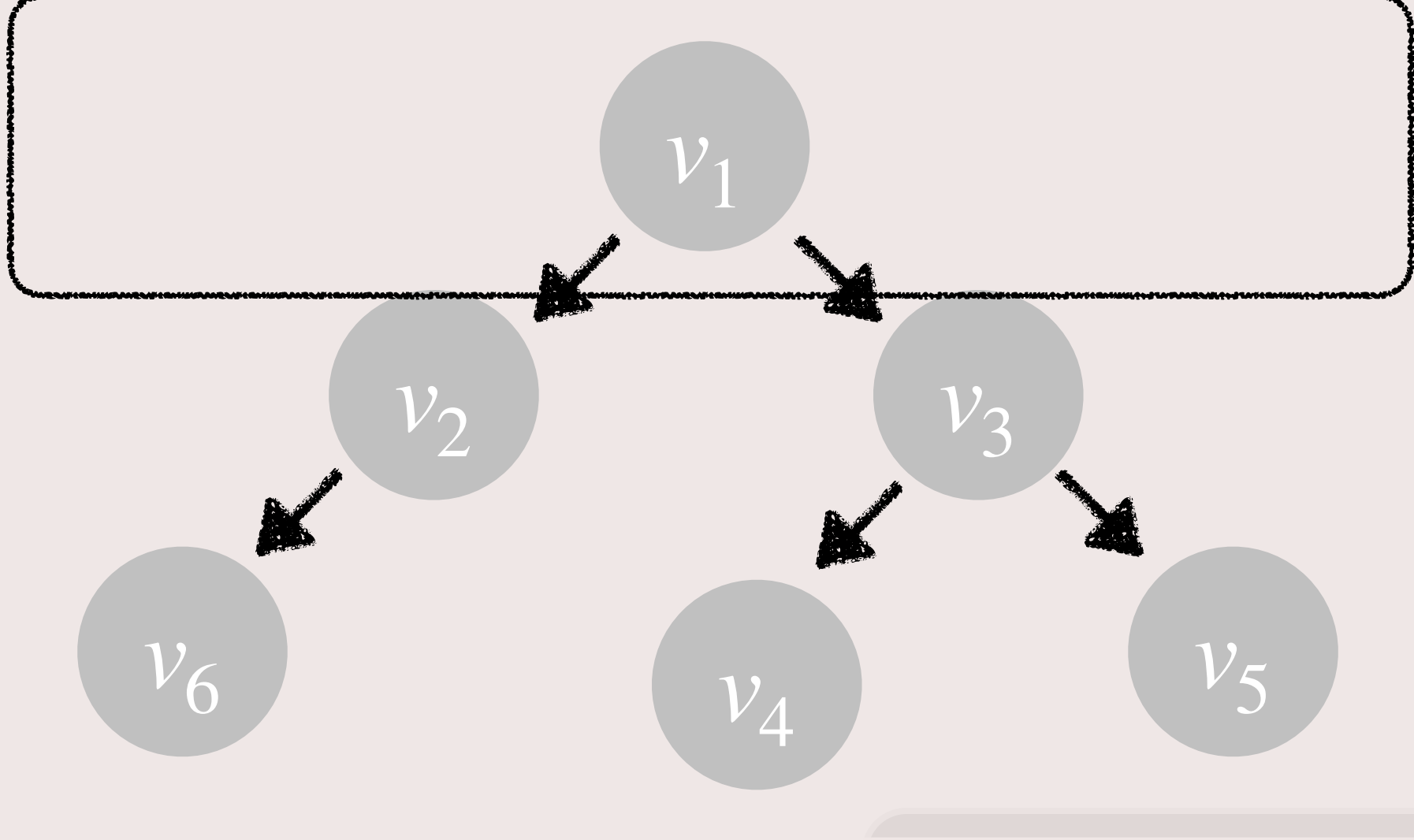


Written in parallel



root

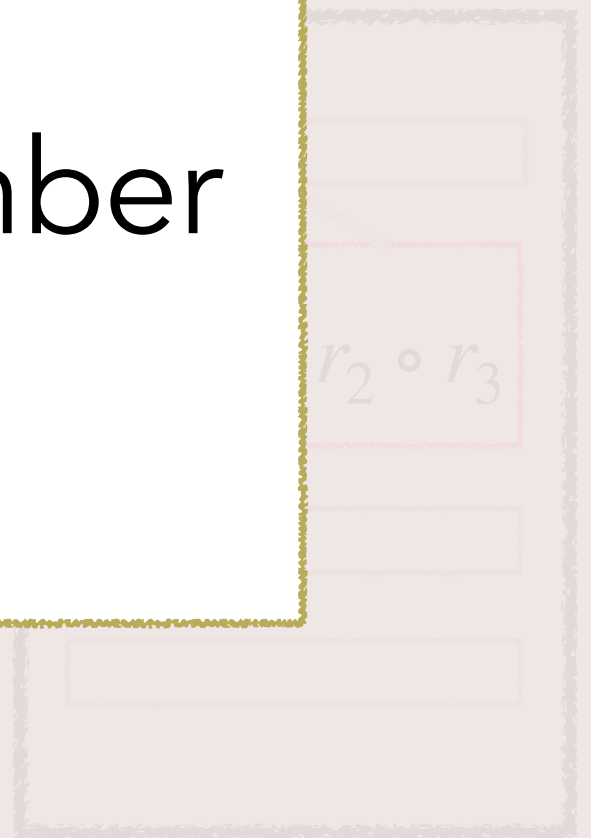
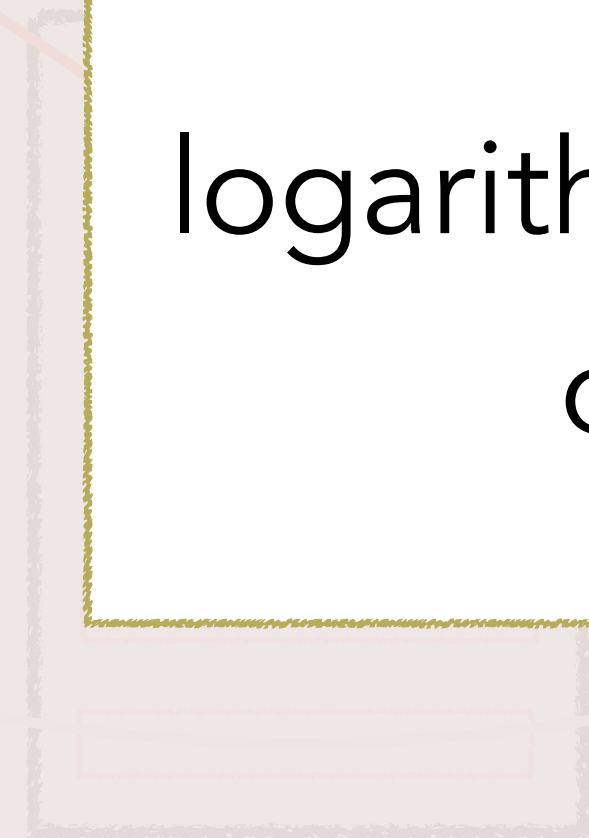
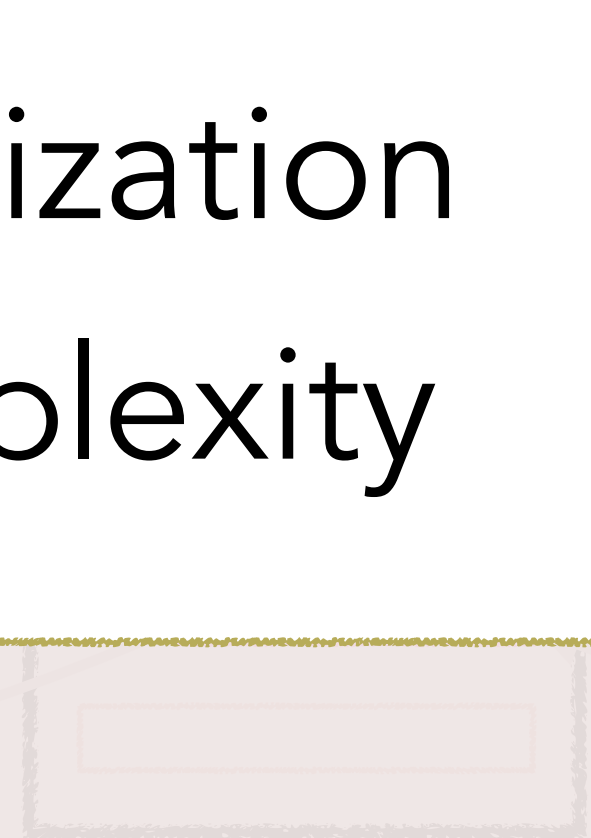
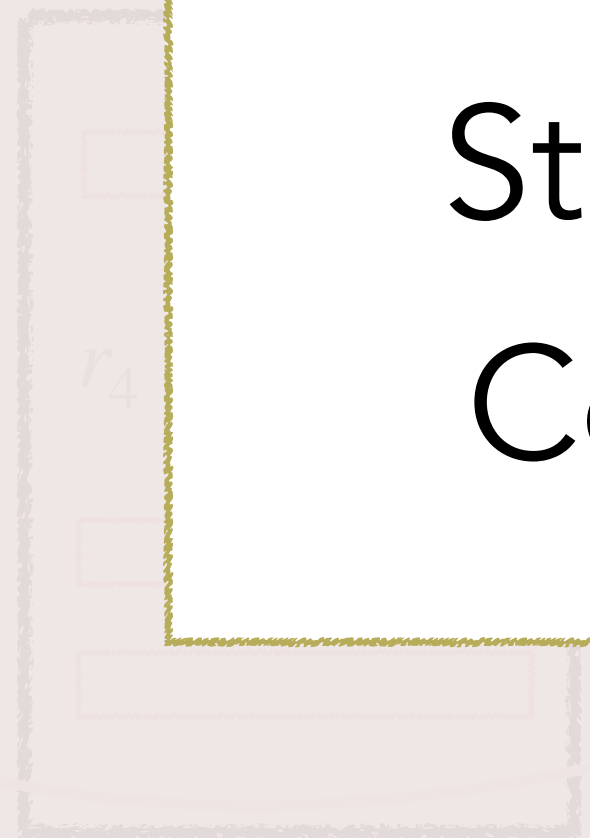
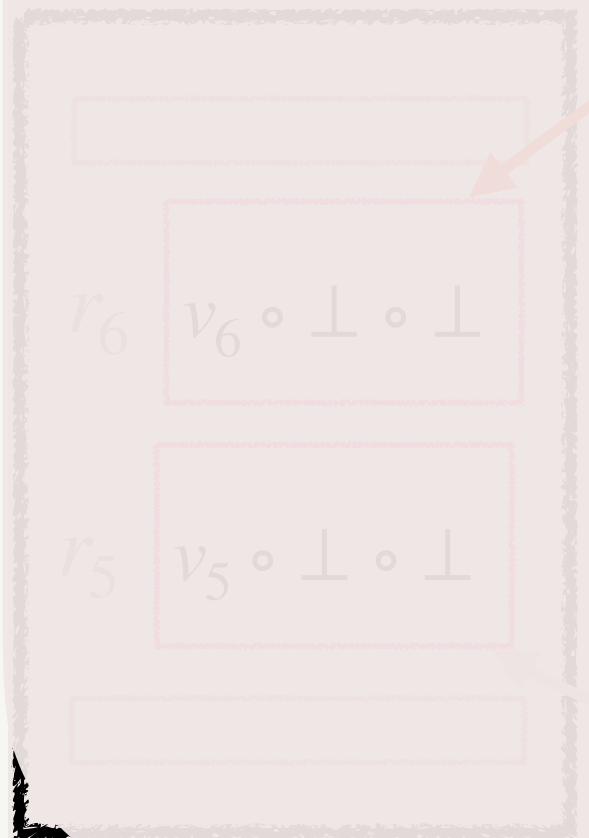




Written in parallel

Stabilization Complexity

logarithmic in number of values



- What are Multi-Maps (MMs)
- What are Encrypted Multi-Maps (EMMs)
- **How to store EMMs on Blockchains**
 - LSX
 - TRX
 - PAX
- Real World Deployment

LSX

A list-based EMM

LSX

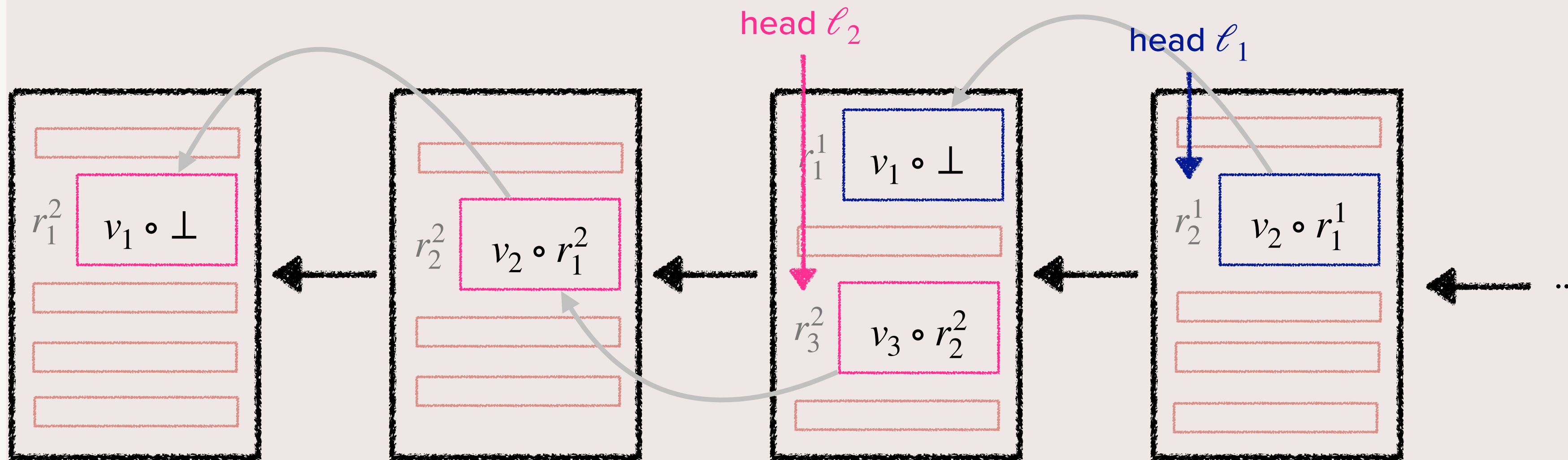
ℓ_1	(v_1, v_2)
ℓ_2	(v_1, v_2, v_3)

- Represent each label as separate list on BC

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- Represent each label as separate list on BC

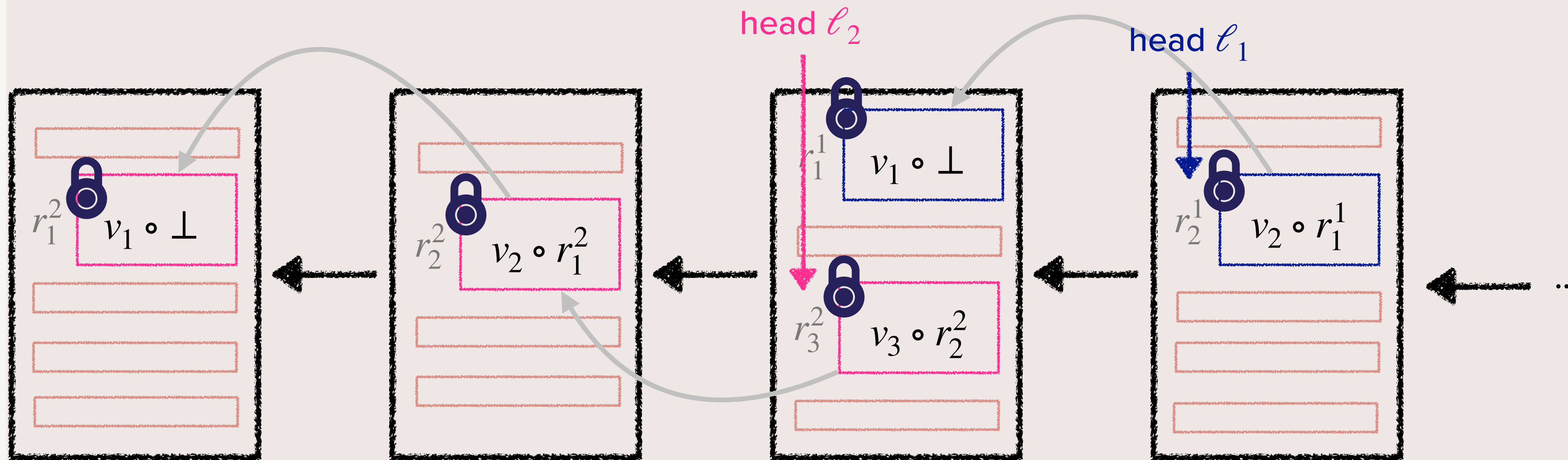
ℓ_1	(v_1, v_2)
ℓ_2	(v_1, v_2, v_3)



LSX

- Represent each label as separate list on BC
- Encrypt each value before storing on BC

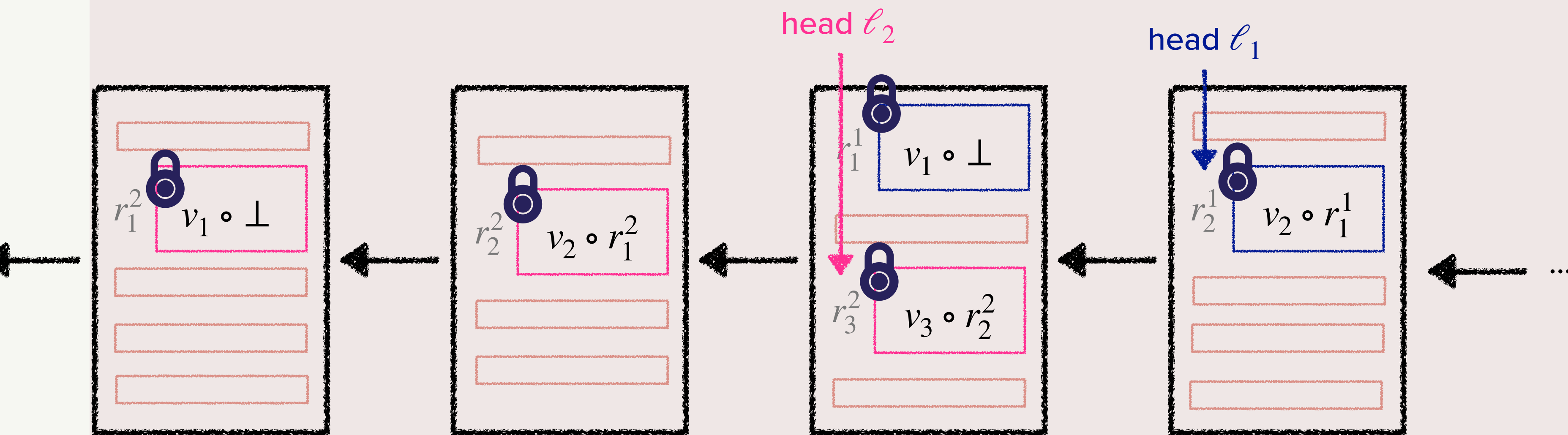
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ℓ_2	(v_1, v_2, v_3)



LSX

- Represent each label as separate list on BC
- Encrypt each value before storing on BC

ℓ_1	(v_1, v_2)
ℓ_2	(v_1, v_2, v_3)

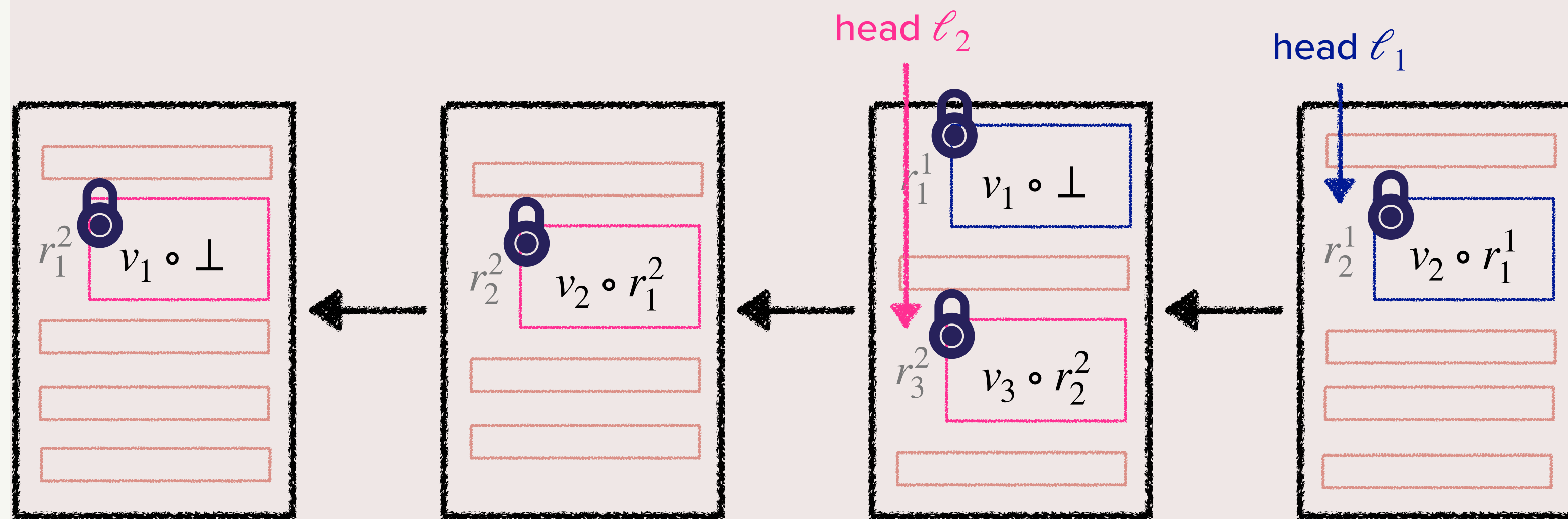


LSX

Add(ℓ_2, v_4)

Delete(ℓ_1, v_1)

Query(ℓ_1)



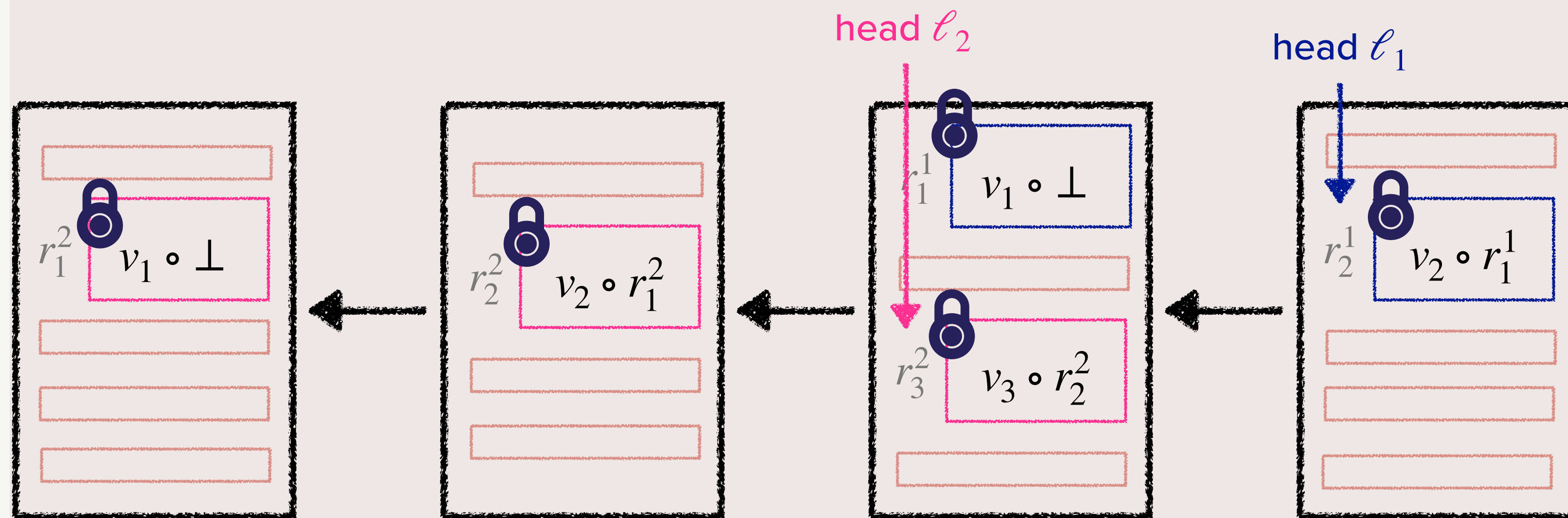
LSX

Add(ℓ_2, v_4)

- Append $\text{Enc}(v_4, r_3^2)$ at head of ℓ_2
- Update the head

Delete(ℓ_1, v_1)

Query(ℓ_1)



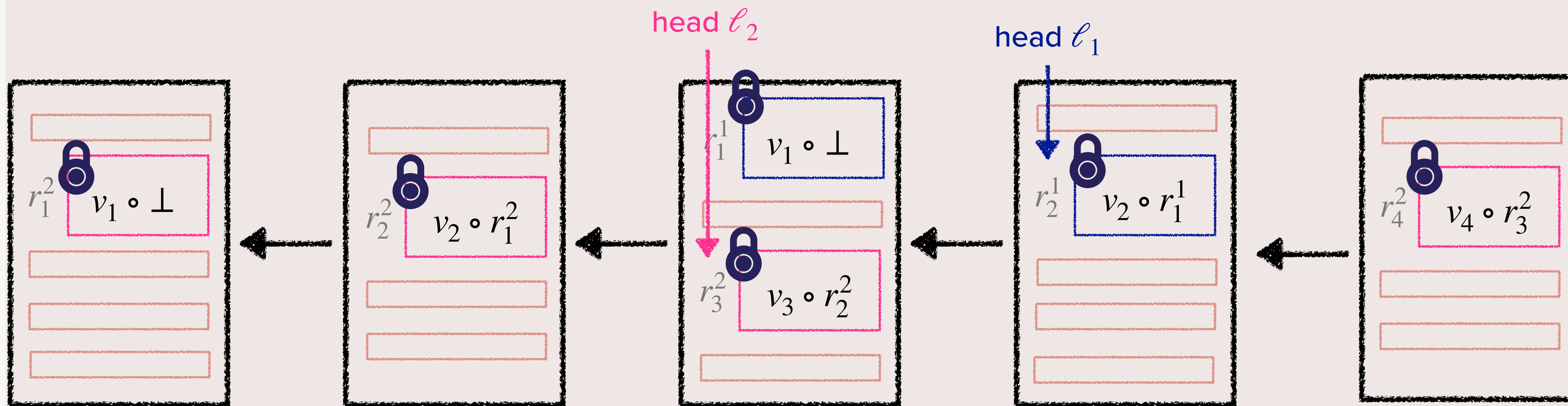
LSX

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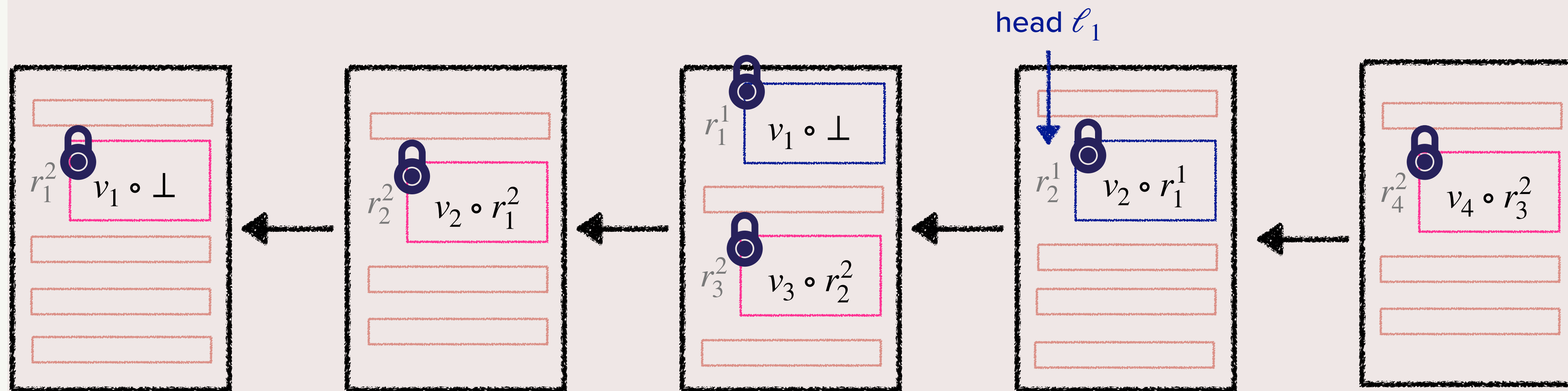
LSX

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Query(ℓ_1)



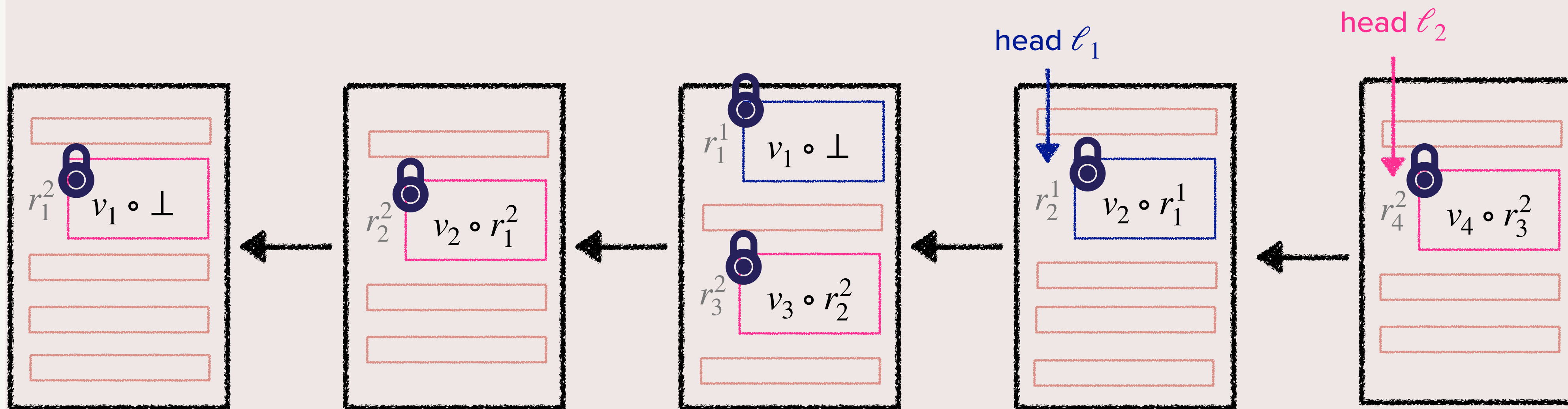
LSX

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- Update the head

Delete(ℓ_1, v_1)

Query(ℓ_1)



LSX

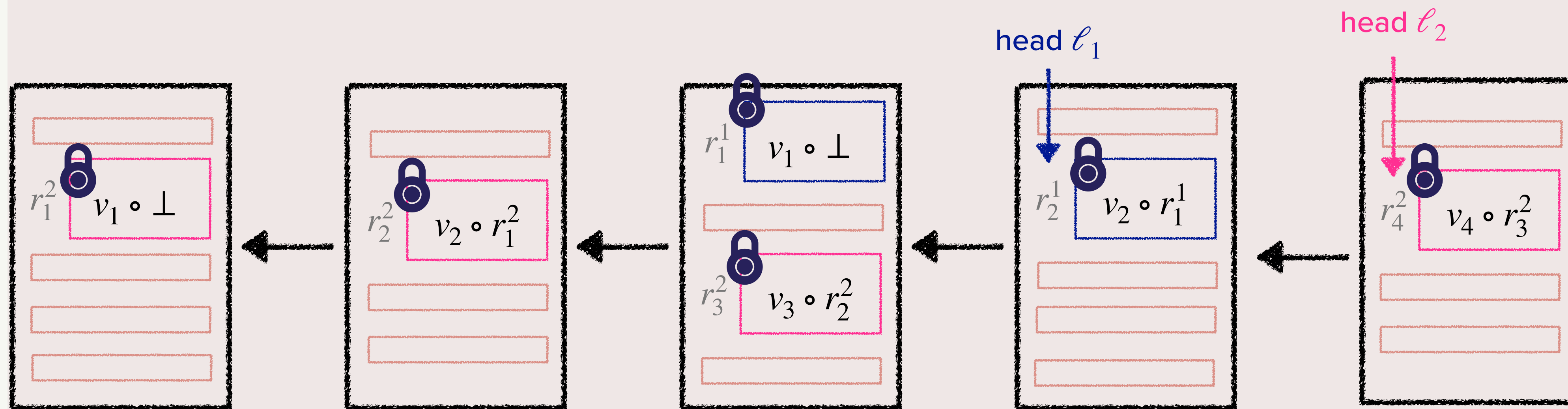
Add(ℓ_2, v_4)

- Append $\text{Enc}(v_4, r_3^2)$ at head of ℓ_2
- Update the head

Delete(ℓ_1, v_1)

- Same as Add
- Append a DEL flag to the value

Query(ℓ_1)



LSX

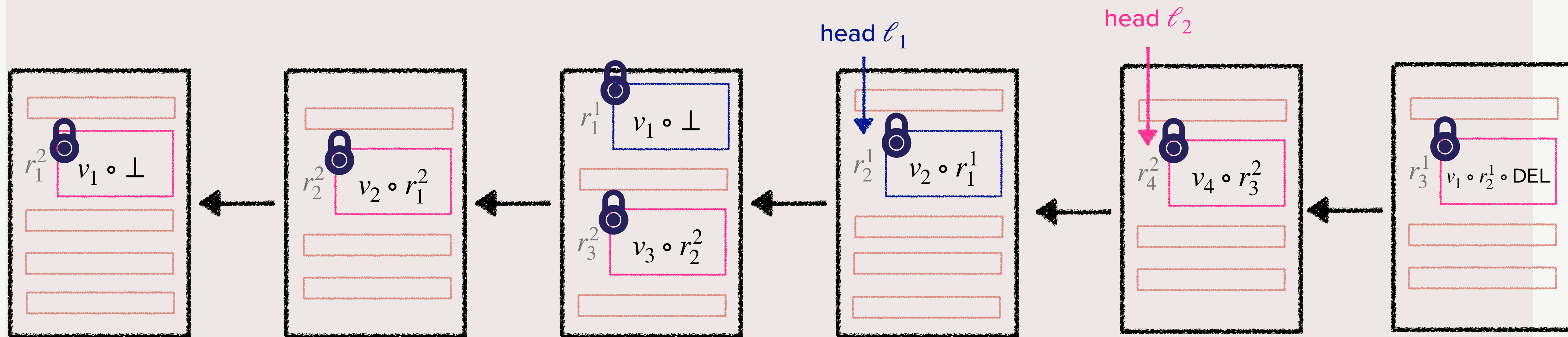
Add(ℓ_2, v_4)

- Append $\text{Enc}(v_4, r_3^2)$ at head of ℓ_2
- Update the head

Delete(ℓ_1, v_1)

- Same as Add
- Append a DEL flag to the value

Query(ℓ_1)



LSX

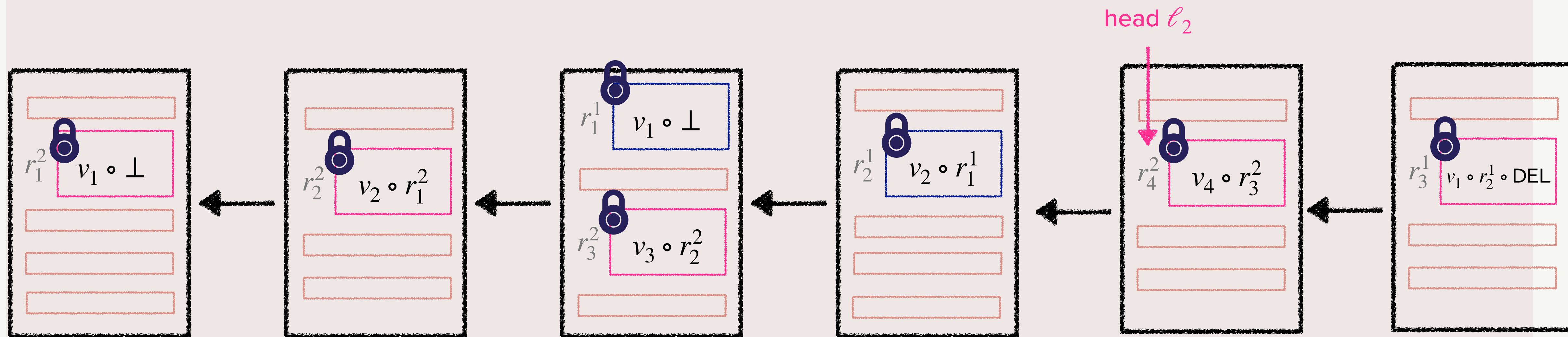
Add(ℓ_2, v_4)

- Append $\text{Enc}(v_4, r_3^2)$ at head of ℓ_2
- Update the head

Delete(ℓ_1, v_1)

- Same as Add
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Query(ℓ_1)



LSX

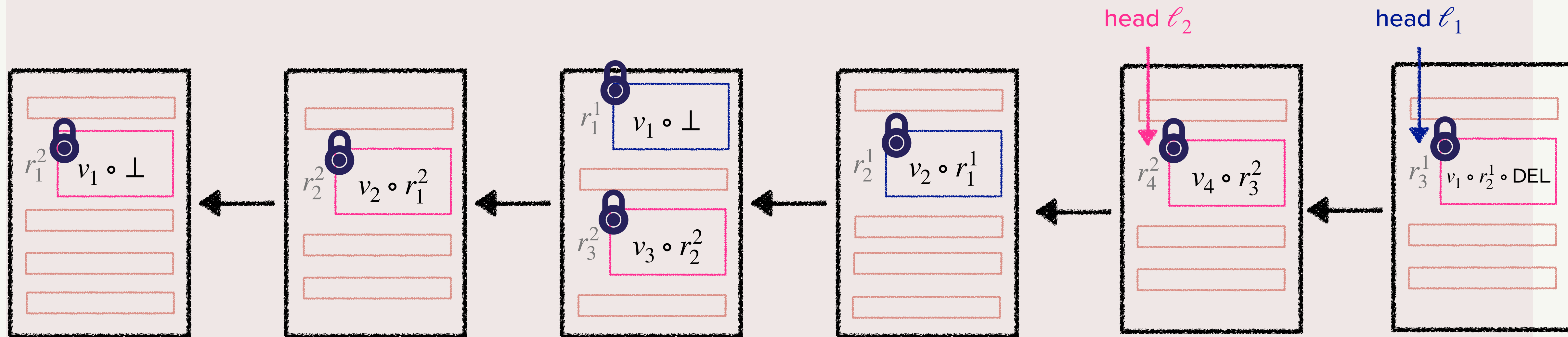
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- Update the head

Delete(ℓ_1, v_1)

- Same as Add
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Query(ℓ_1)



LSX

Add(ℓ_2, v_4)

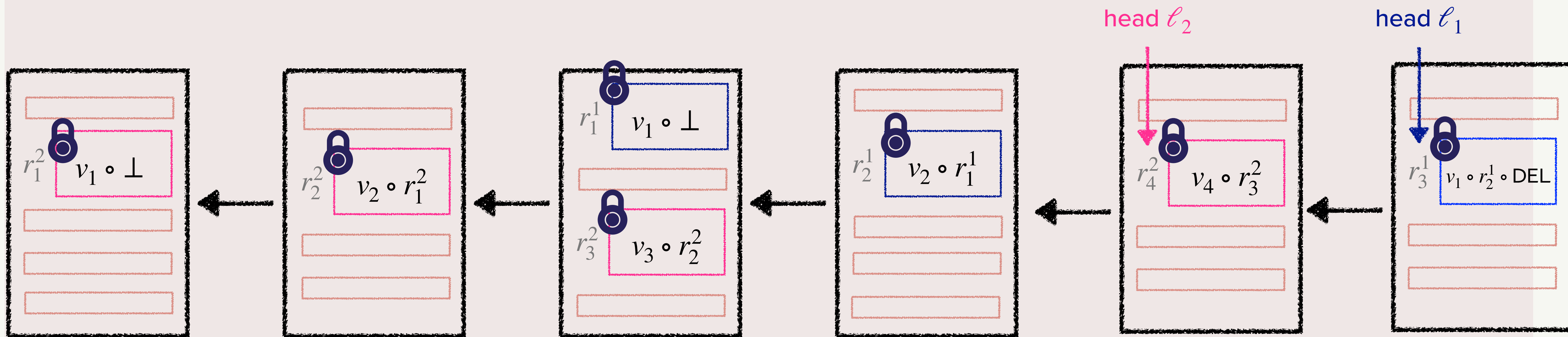
- Append $\text{Enc}(v_4, r_3^2)$ at head of ℓ_2
- Update the head

Delete(ℓ_1, v_1)

- Same as Add
- Append a DEL flag to the value

Query(ℓ_1)

- Read all values from the list
- Output un-deleted values



LSX

Add(ℓ_2, v_4)

- Append $\text{Enc}(v_4, r_3^2)$ at head of ℓ_2
- Update the head

Optimal: $O(|t|)$

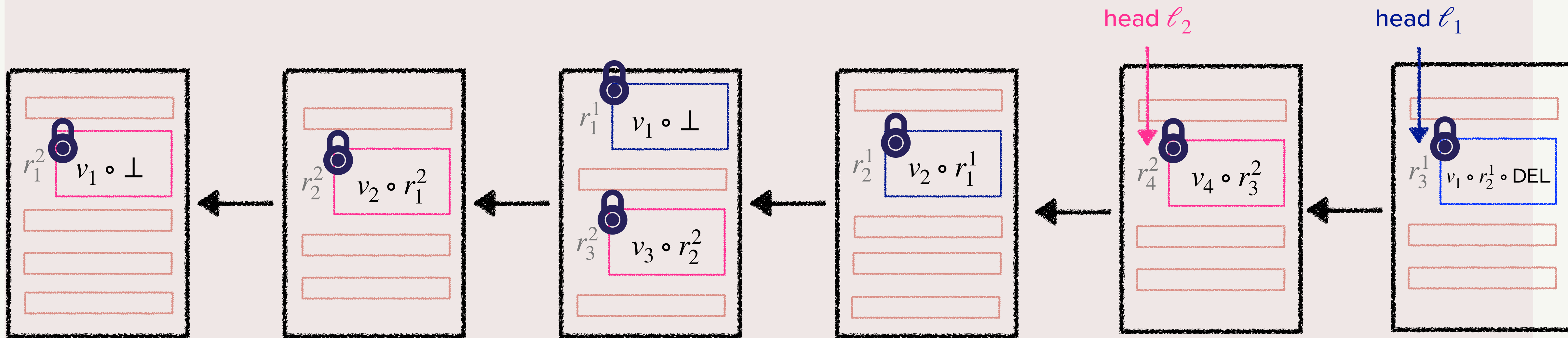
Delete(ℓ_1, v_1)

- Same as Add
- Append a DEL flag to the value

Optimal: $O(|t|)$

Query(ℓ_1)

- Read all values from the list
- Output un-deleted values



LSX

Add(ℓ_2, v_4)

- Append $\text{Enc}(v_4, r_3^2)$ at head of ℓ_2
- Update the head

Optimal: $O(|t|)$

Delete(ℓ_1, v_1)

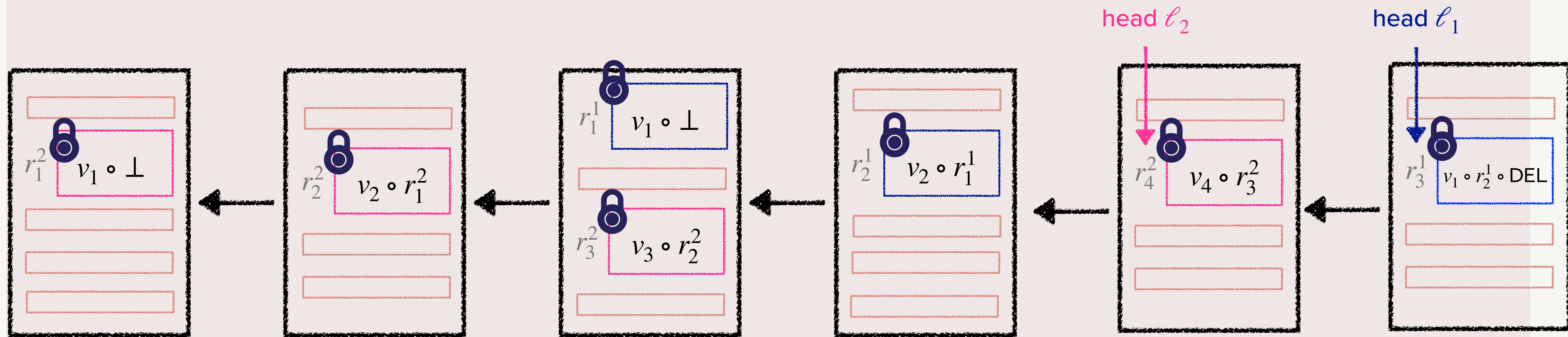
- Same as Add
- Append a DEL flag to the value

Optimal: $O(|t|)$

Query(ℓ_1)

- Read all values from the list
- Output un-deleted values

values ever added/
deleted



LSX

Add(ℓ_2, v_4)

- Append $\text{Enc}(v_4, r_3^2)$ at head of ℓ_2
- Update the head

time
Optimal: $O(|t|)$

stabilization

$O(|t|)$

Delete(ℓ_1, v_1)

- Same as Add
- Append a DEL flag to the value

time
Optimal: $O(|t|)$

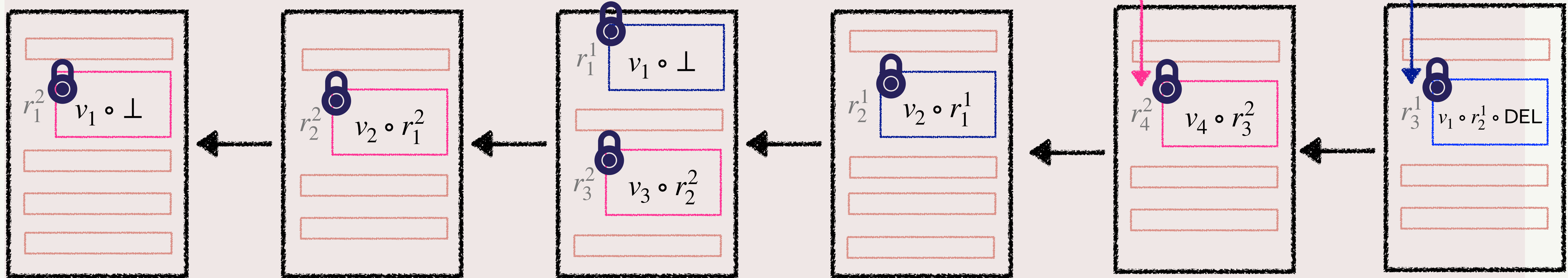
stabilization

$O(|t|)$

Query(ℓ_1)

- Read all values from the list
- Output un-deleted values

values ever added/
deleted



LSX

Add(ℓ_2, v_4)

- Append $\text{Enc}(v_4, r_3^2)$ at head of ℓ_2
- Update the head

time
Optimal: $O(|t|)$

stabilization
 $O(|t|)$

Delete(ℓ_1, v_1)

- Same as Add
- Append a DEL flag to the value

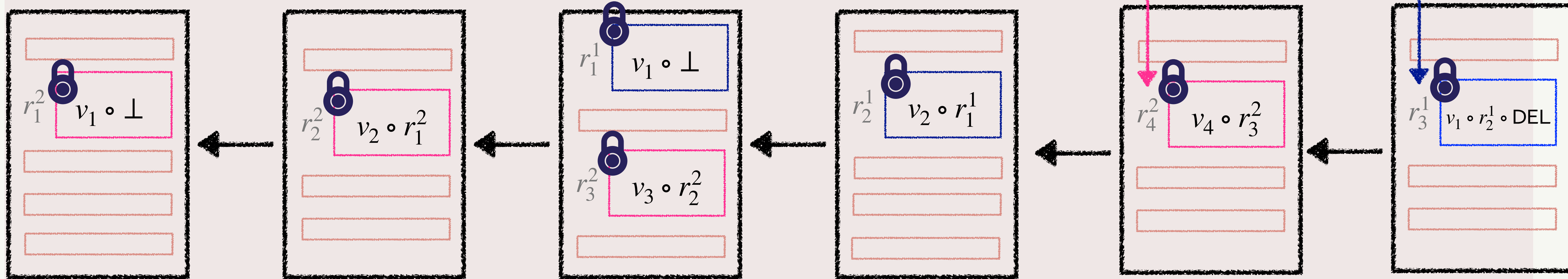
time
Optimal: $O(|t|)$

stabilization
 $O(|t|)$

Query(ℓ_1)

- Read all values from the list
- Output un-deleted values

values ever added/
deleted



LSX



TRX

A tree-based EMM

Add(ℓ_2, v_4)

- Append Enc(v_4, r_3^2) at head of ℓ_2
- Update the head

Delete(ℓ_1, v_1)

- Same as Add, but to the value

Query(ℓ_1)

- Read all values from the list
- Output un-deleted values

time

Optimal: $O(|t|)$

time

Optimal: $O(|t|)$

time

values ever added/
deleted

stabilization

~~$O(|t|)$~~

stabilization

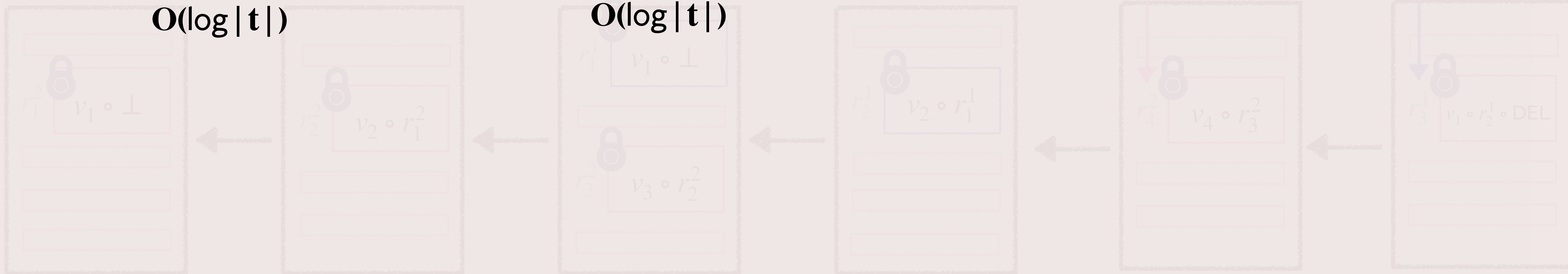
~~$O(|t|)$~~

$O(\log |t|)$

$O(\log |t|)$

head ℓ_2

head ℓ_1



TRX

A tree-based EMM

Add(ℓ_2, v_4)

- Append Enc(v_4, r_3^2) at head of ℓ_2
- Update the head

time

Optimal: $O(|t|)$

stabilization

~~$O(|t|)$~~

$O(\log |t|)$

Delete(ℓ_1, v_1)

- Same as Add, but to the value

time

Optimal: $O(|t|)$

stabilization

~~$O(|t|)$~~

$O(\log |t|)$

Query(ℓ_1)

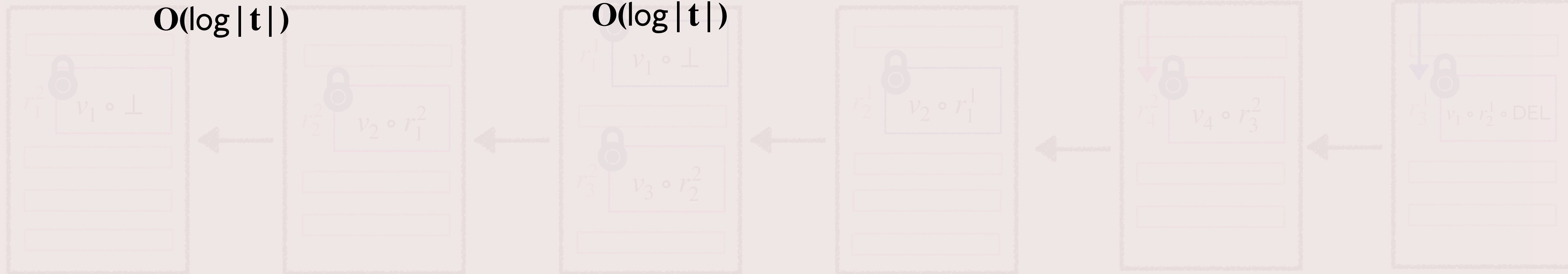
- Read all values from the list
- Output un-deleted values

time

values ever added/
deleted

head ℓ_2

head ℓ_1



PAX

A patched EMM

Add(ℓ_2, v_4)

time

Optimal: $O(|t|)$

stabilization

$O(|t|)$

Delete(ℓ_1, v_1)

time

Optimal: $O(|t|)$

stabilization

$O(|t|)$

Query(ℓ_1)

time

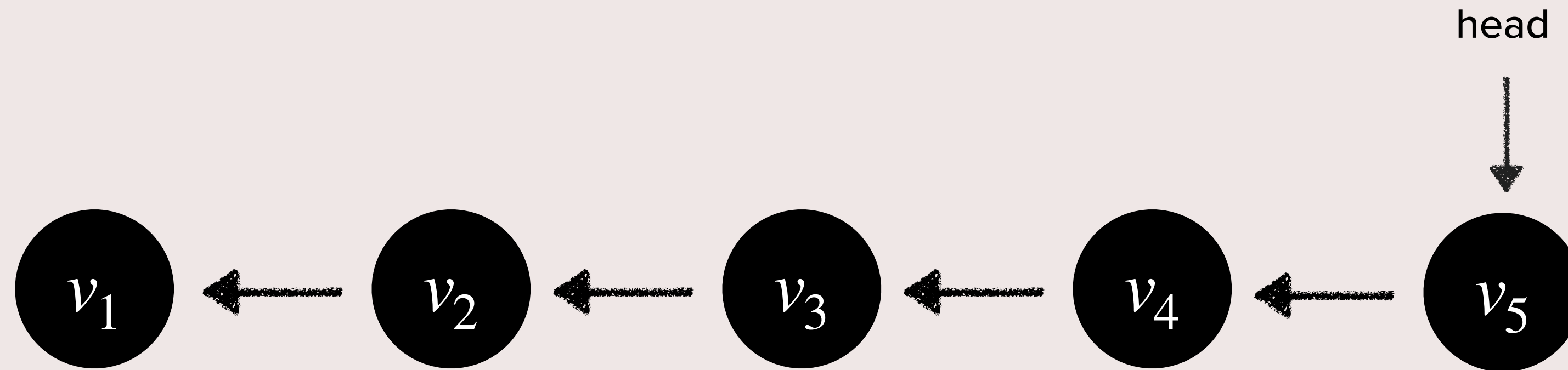
values ever added/
deleted

PAX

Query(ℓ_1)

time

values ever added/
deleted

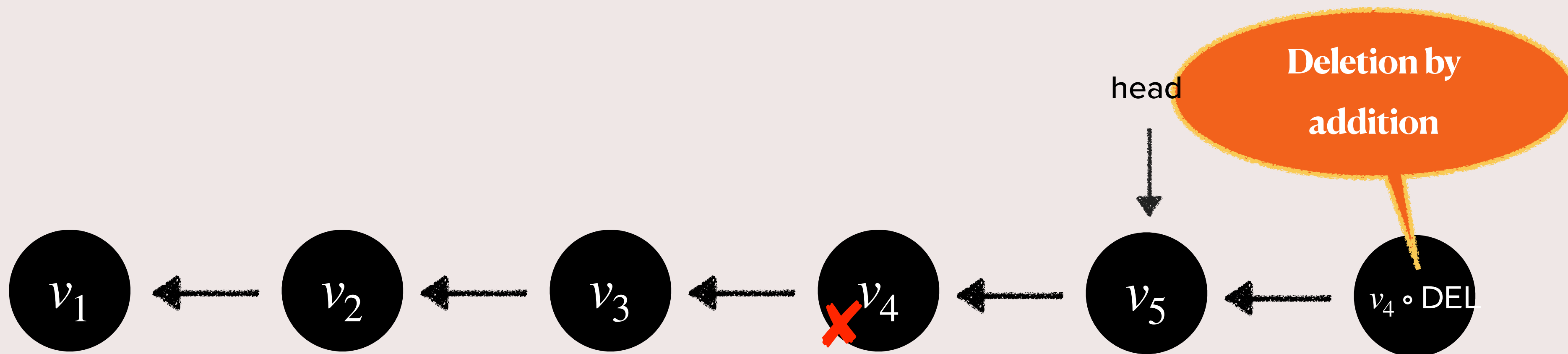


PAX

Query(ℓ_1)

values ever added/
deleted

time

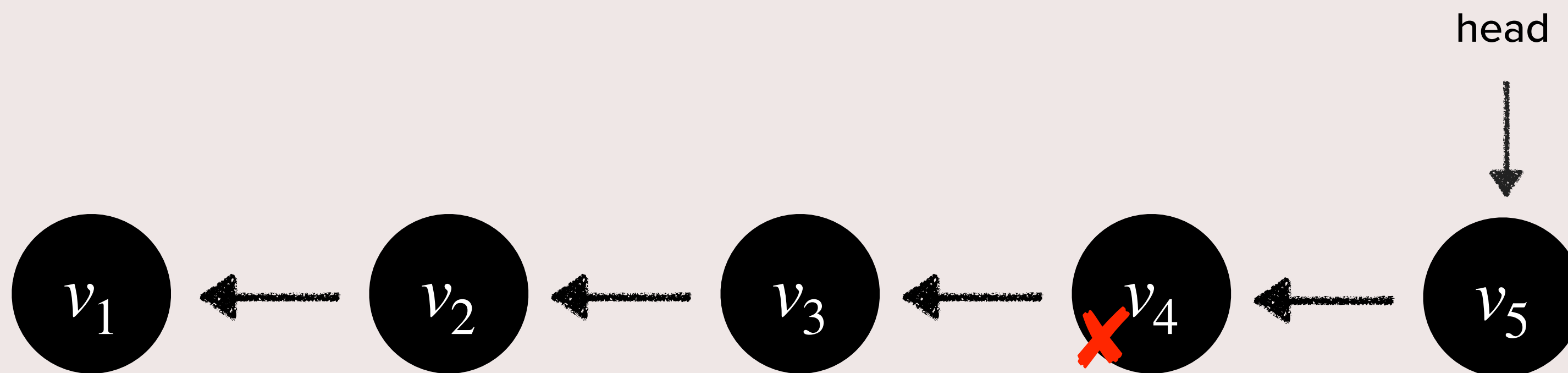


PAX

Query(ℓ_1)

time

values ever added/
deleted

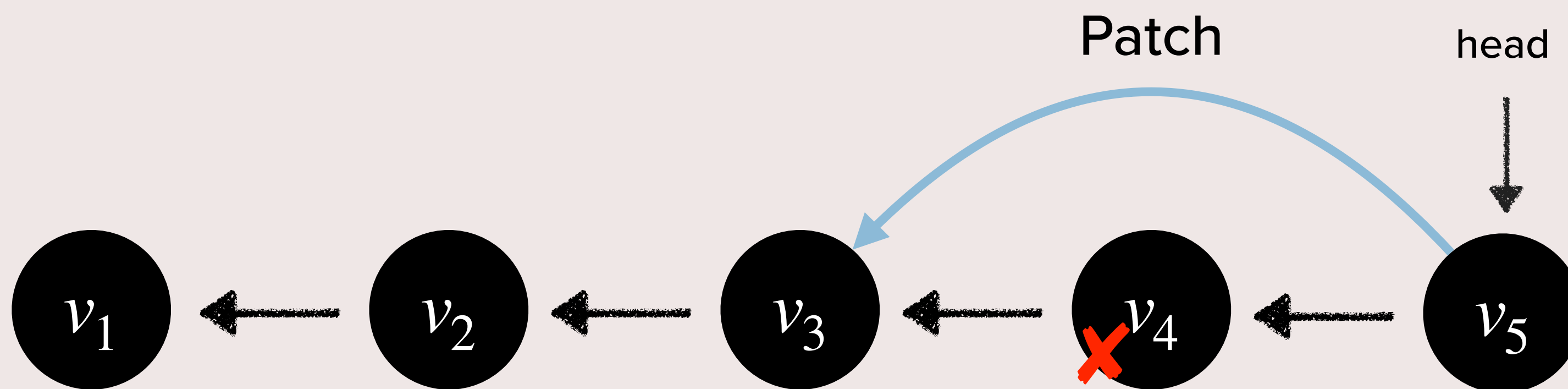


PAX

Query(ℓ_1)

values ever added/
deleted

time

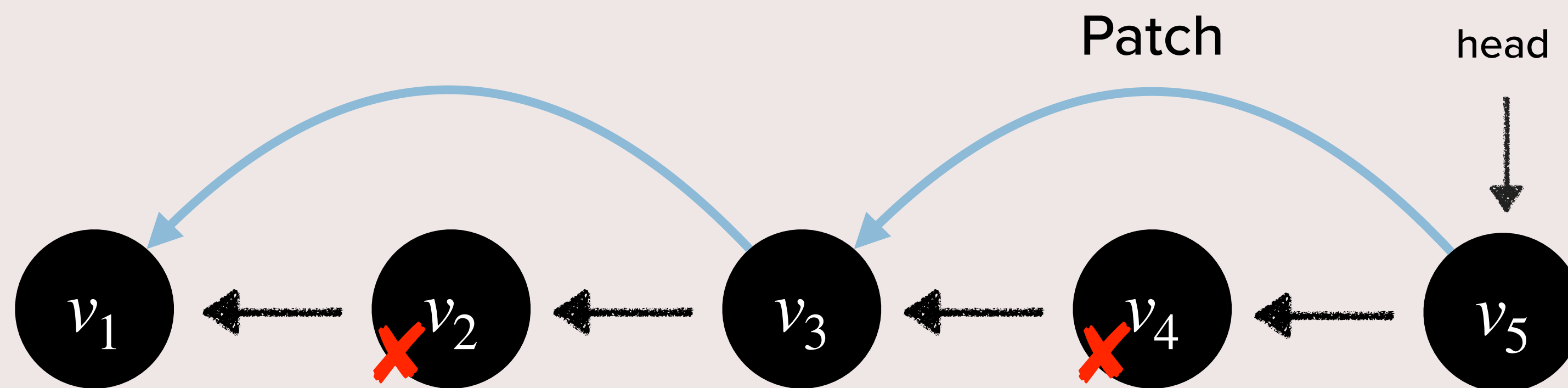


PAX

Query(ℓ_1)

values ever added/
deleted

time

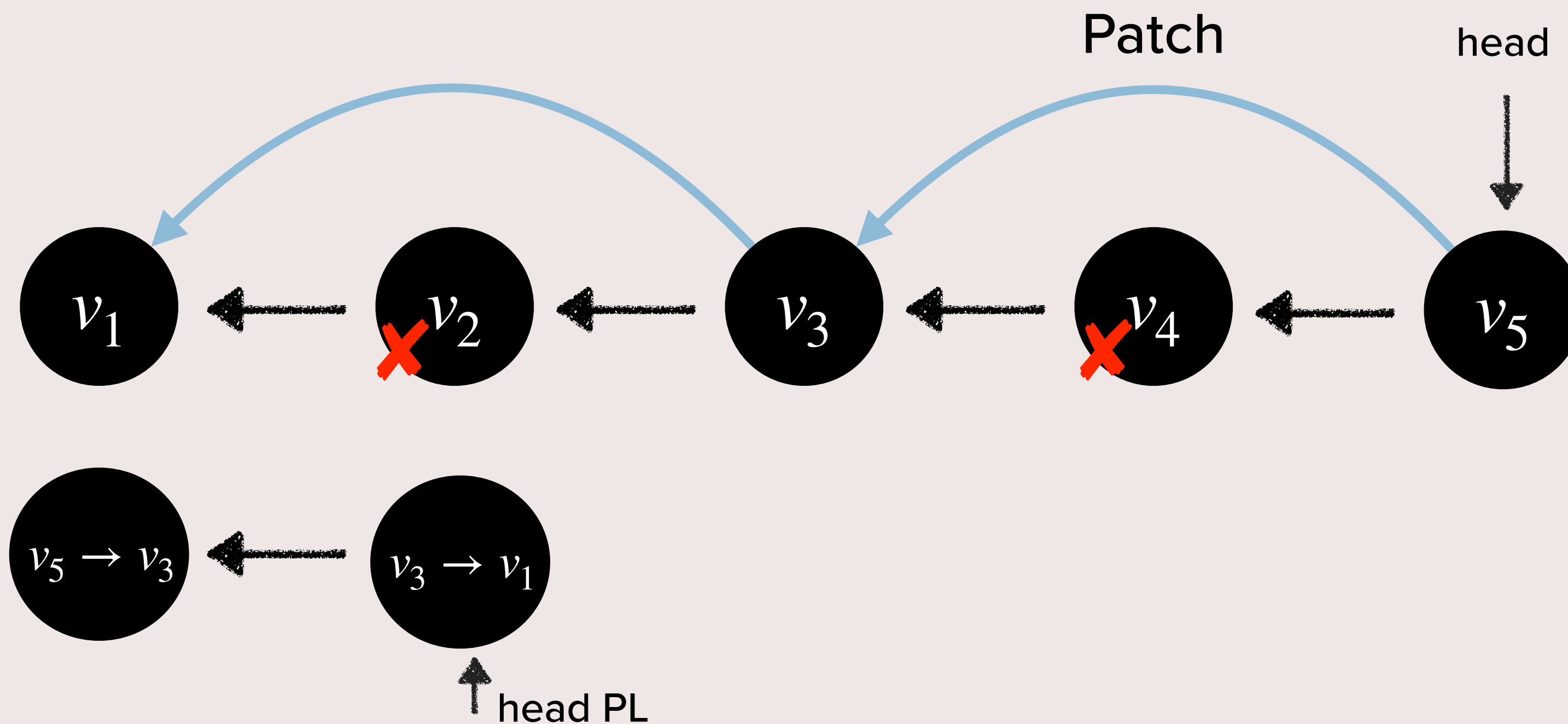


PAX

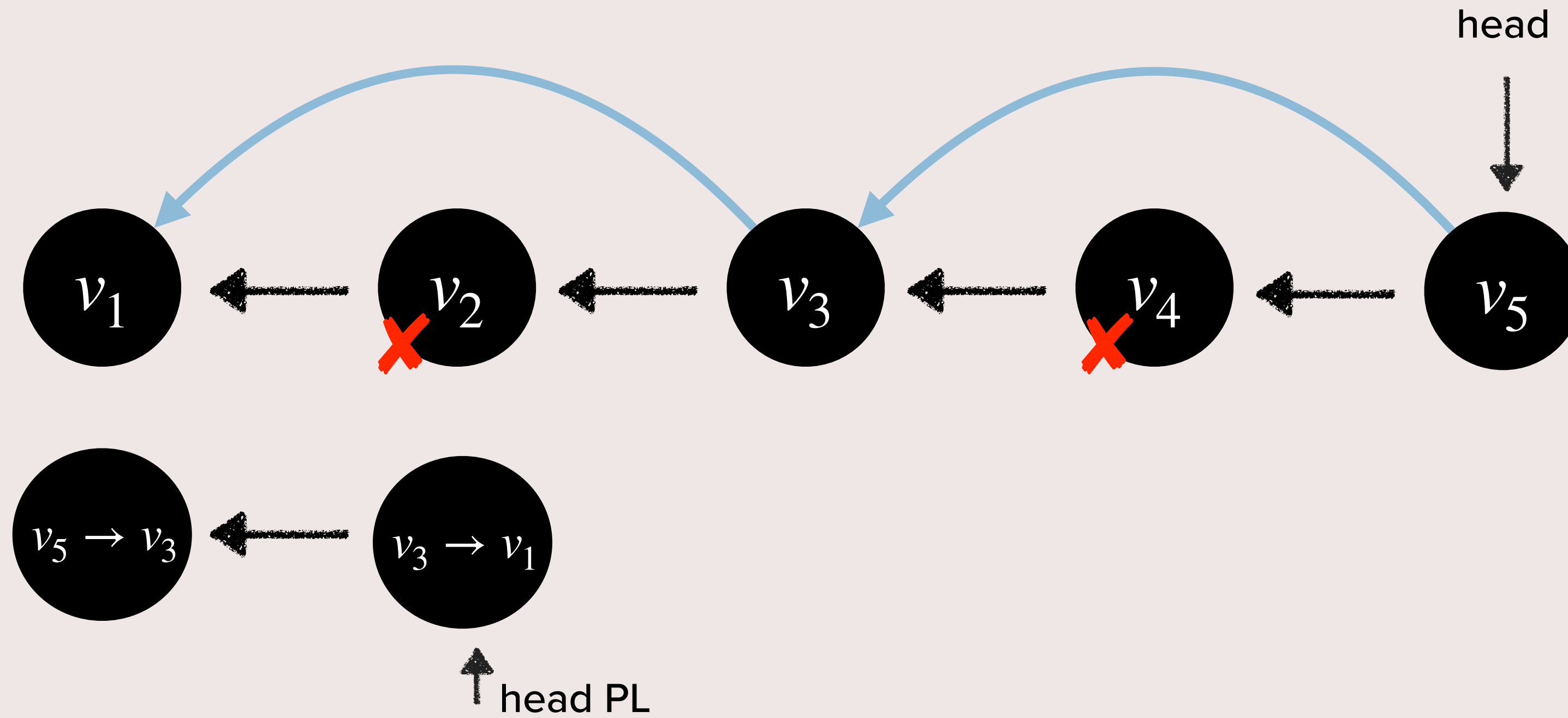
Query(ℓ_1)

values ever added/
deleted

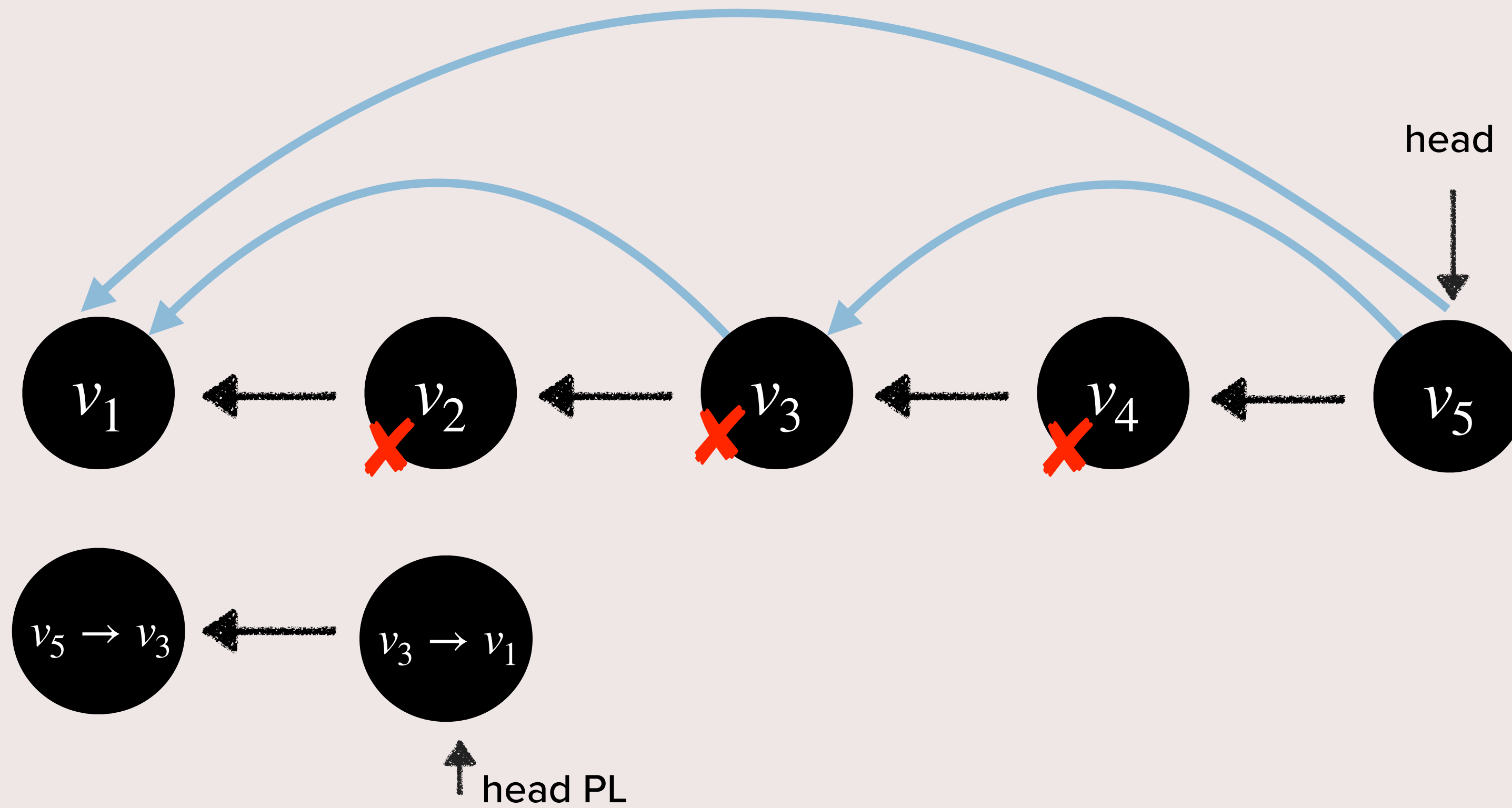
time



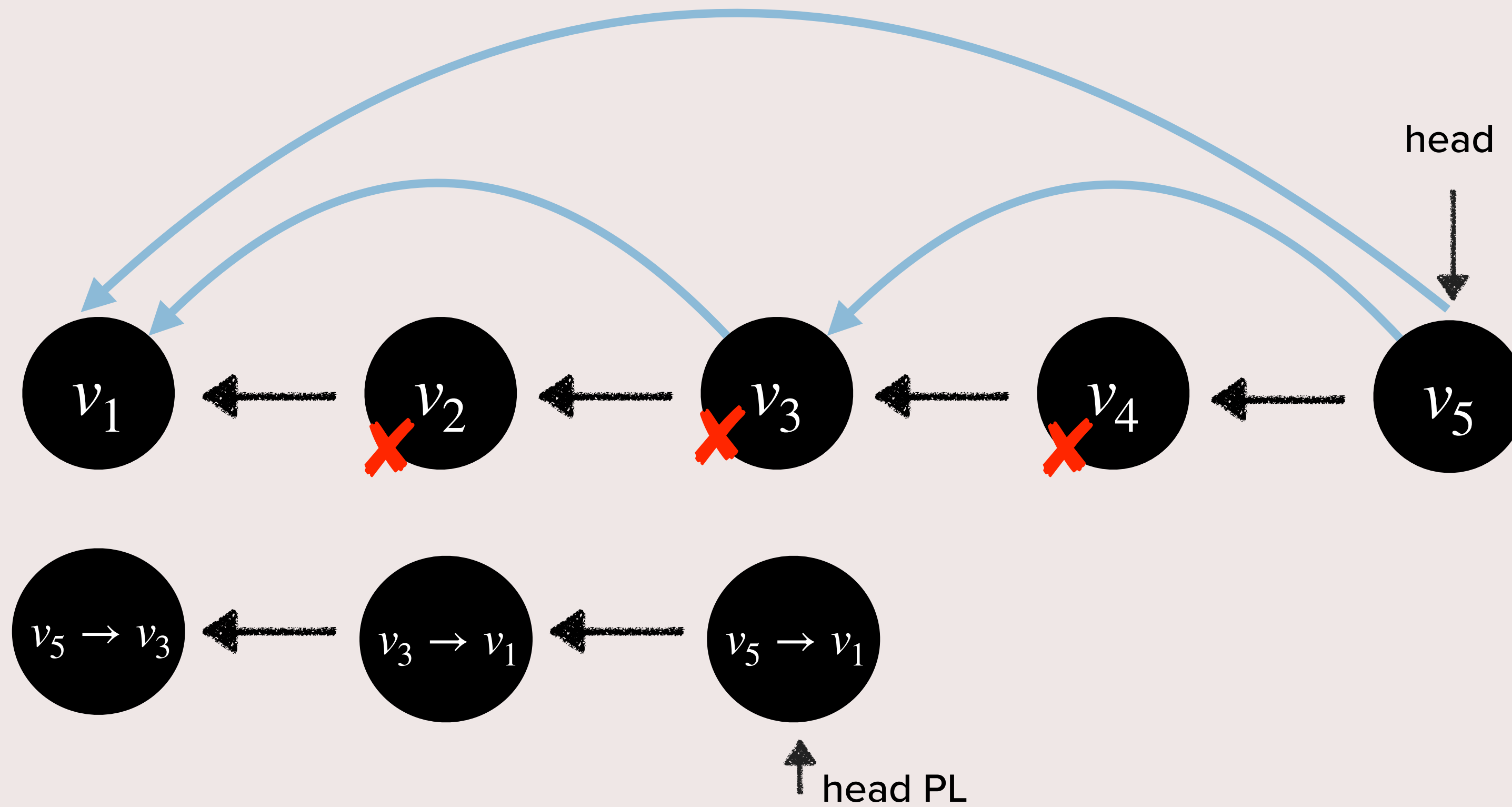
Let's delete v_3



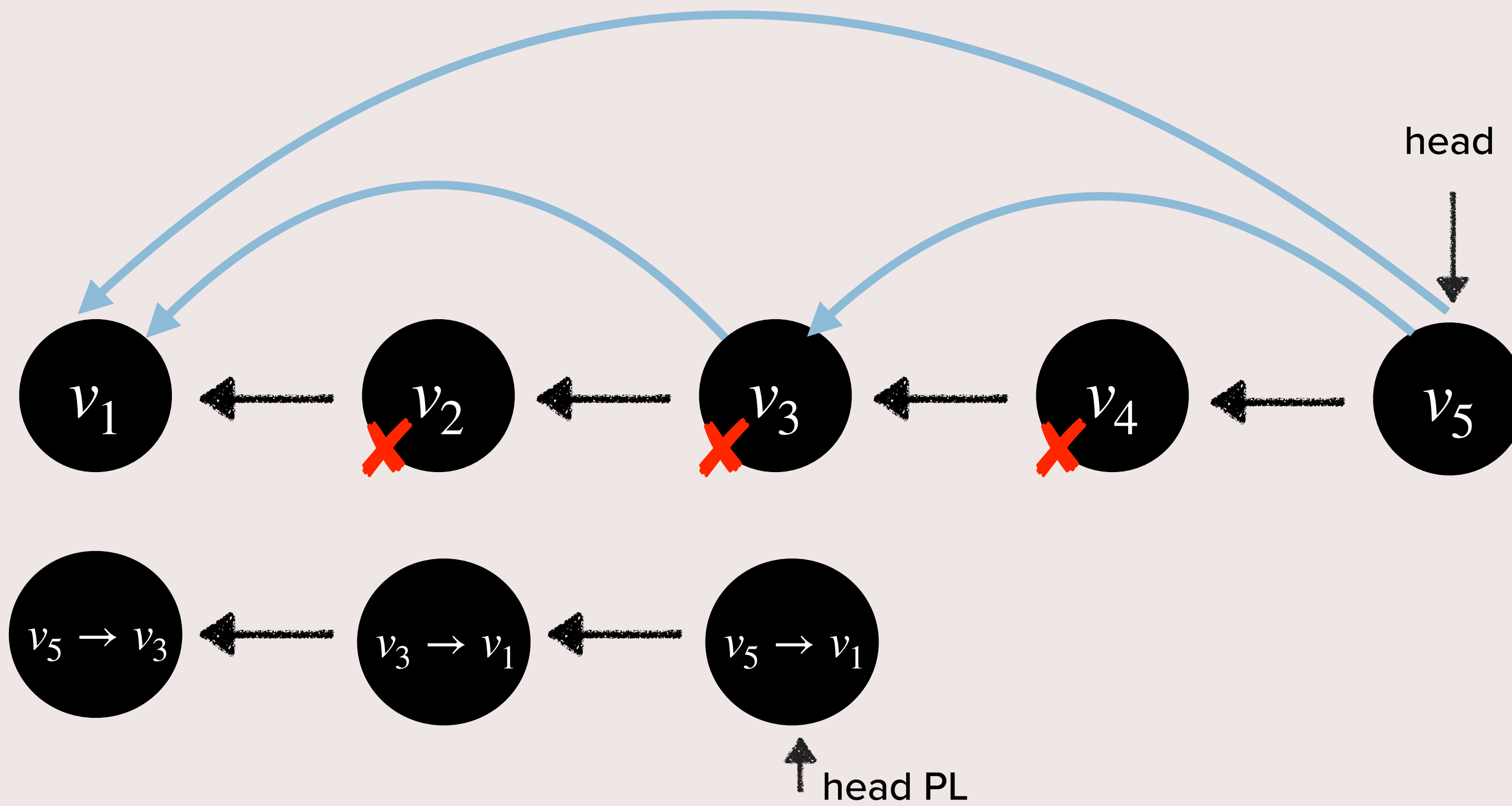
Let's delete v_3



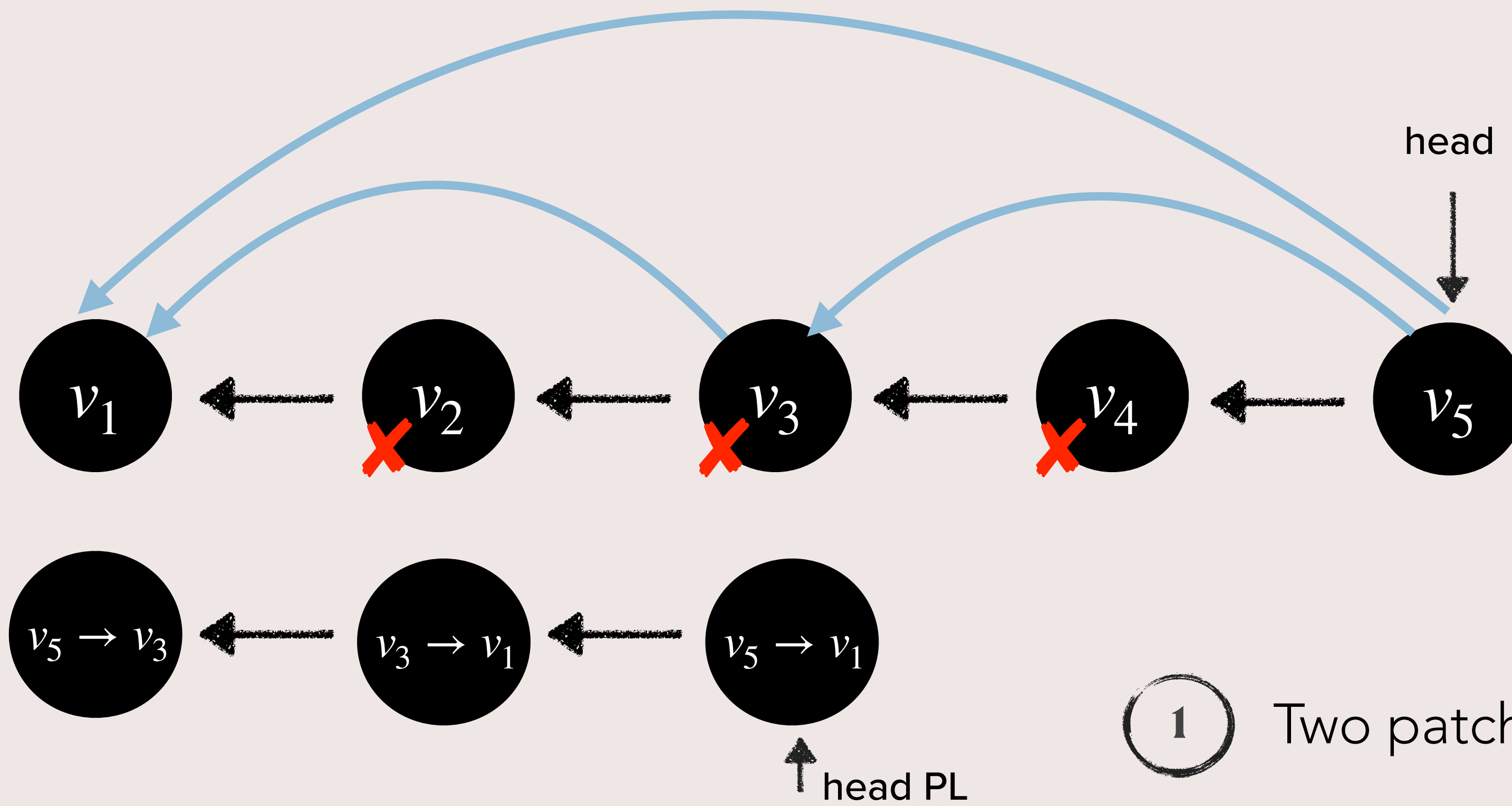
Let's delete v_3



Let's delete v_3



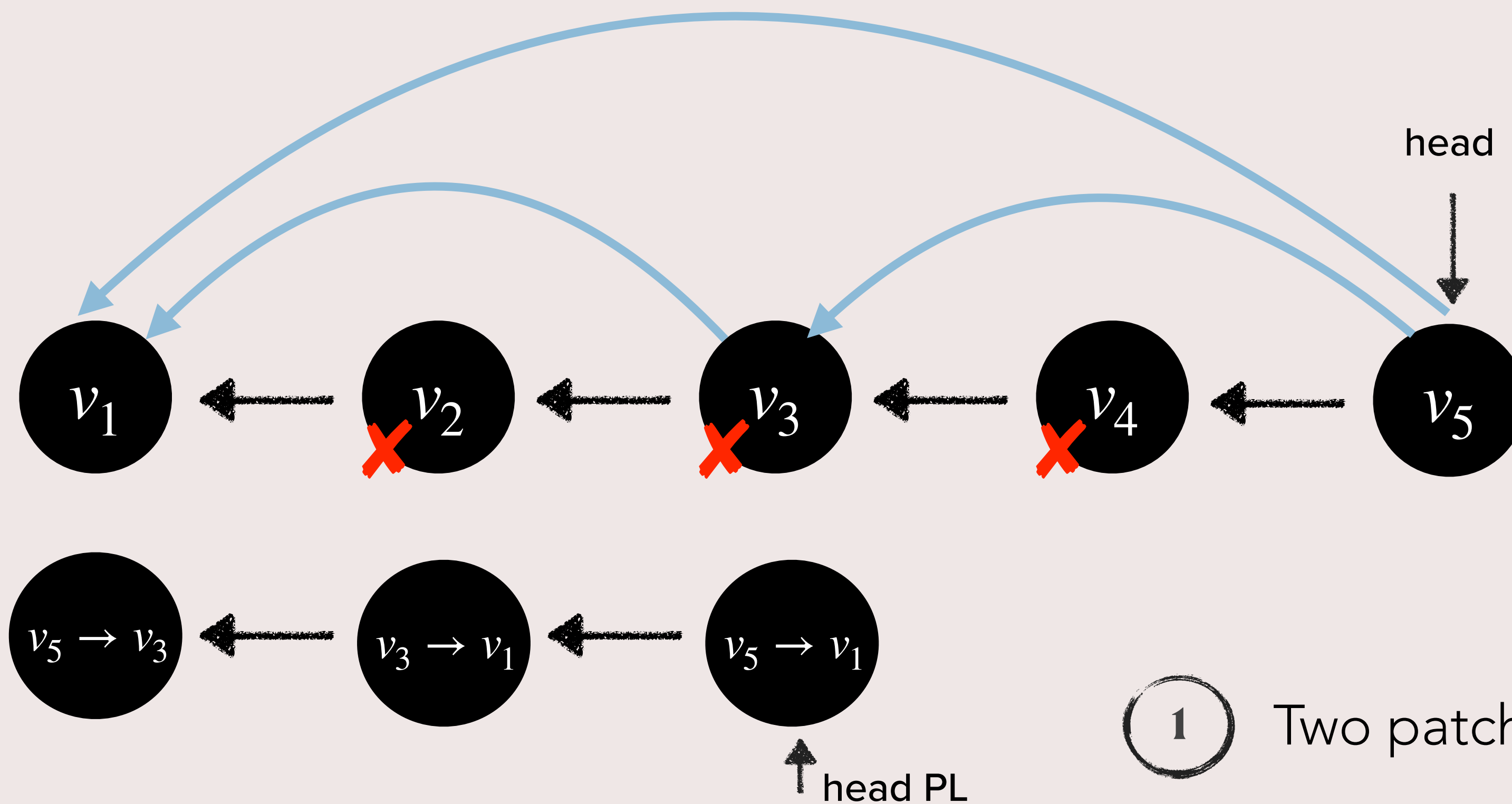
Let's delete v_3



① Two patches from v_5

Bad for correctness

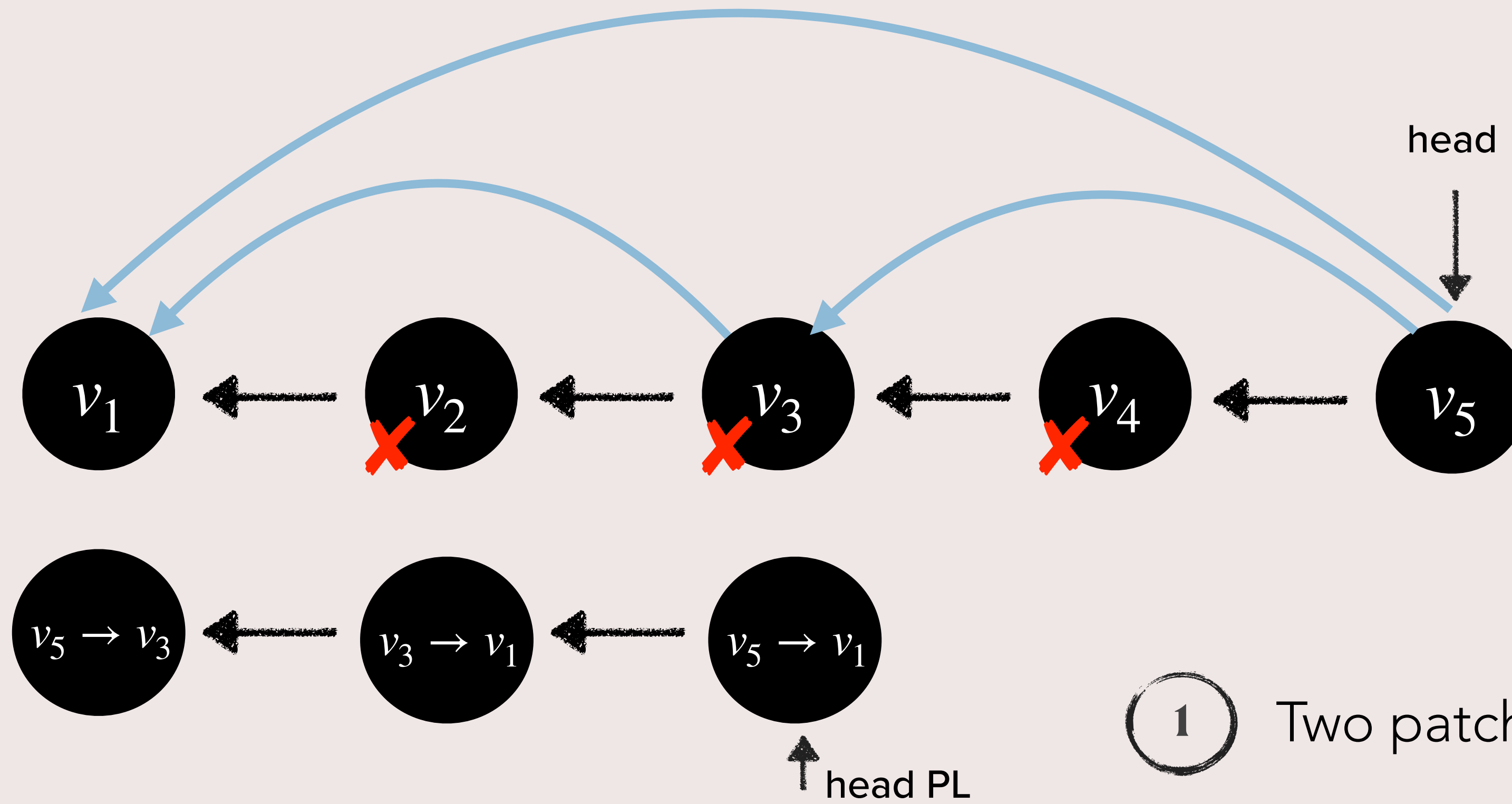
Let's delete v_3



① Two patches from v_5

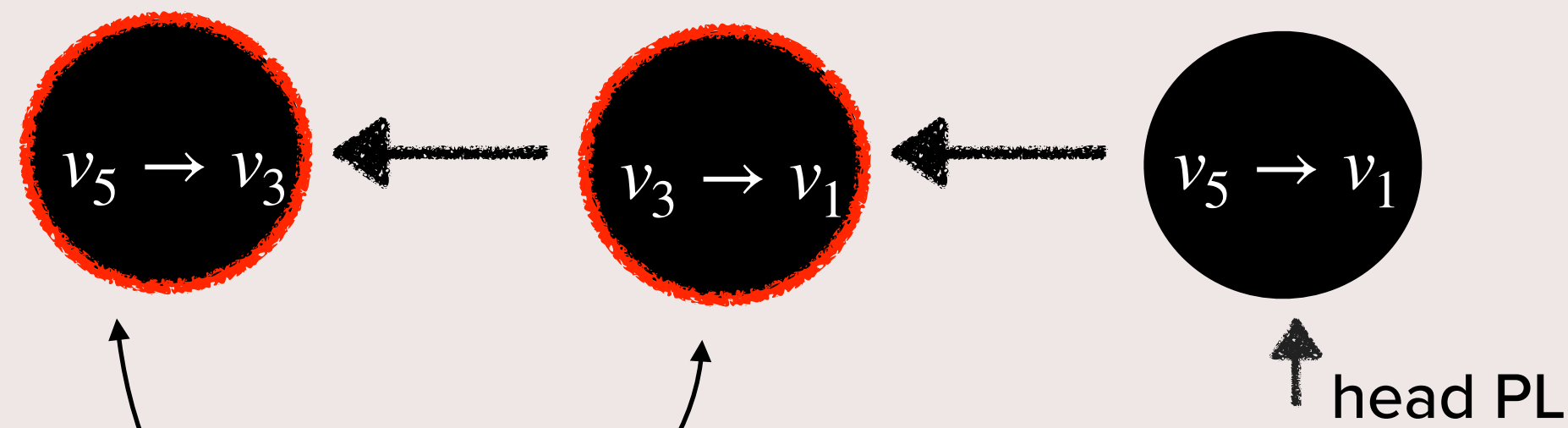
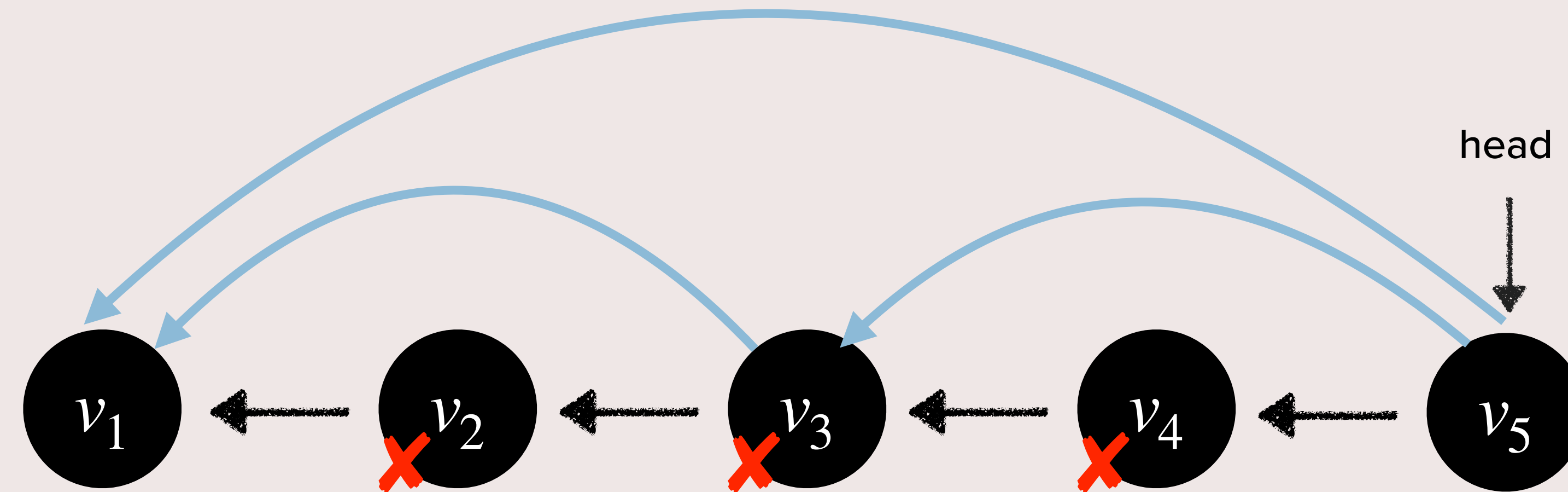
Bad for correctness

Let's delete v_3



- ① Two patches from v_5
Bad for correctness
- ② Size of PL = # values deleted
Bad for efficiency

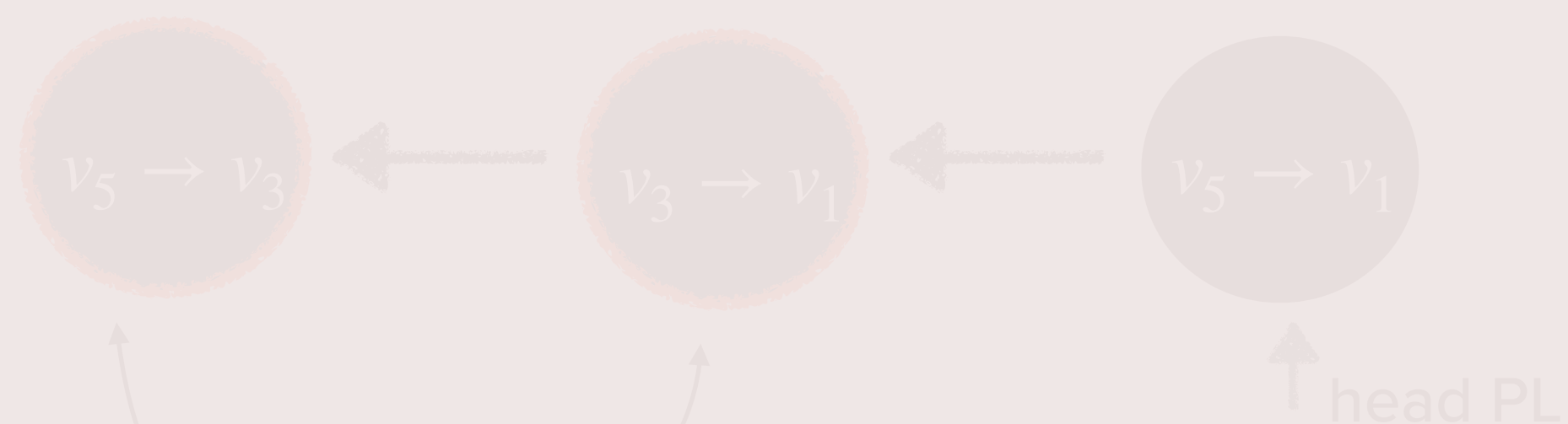
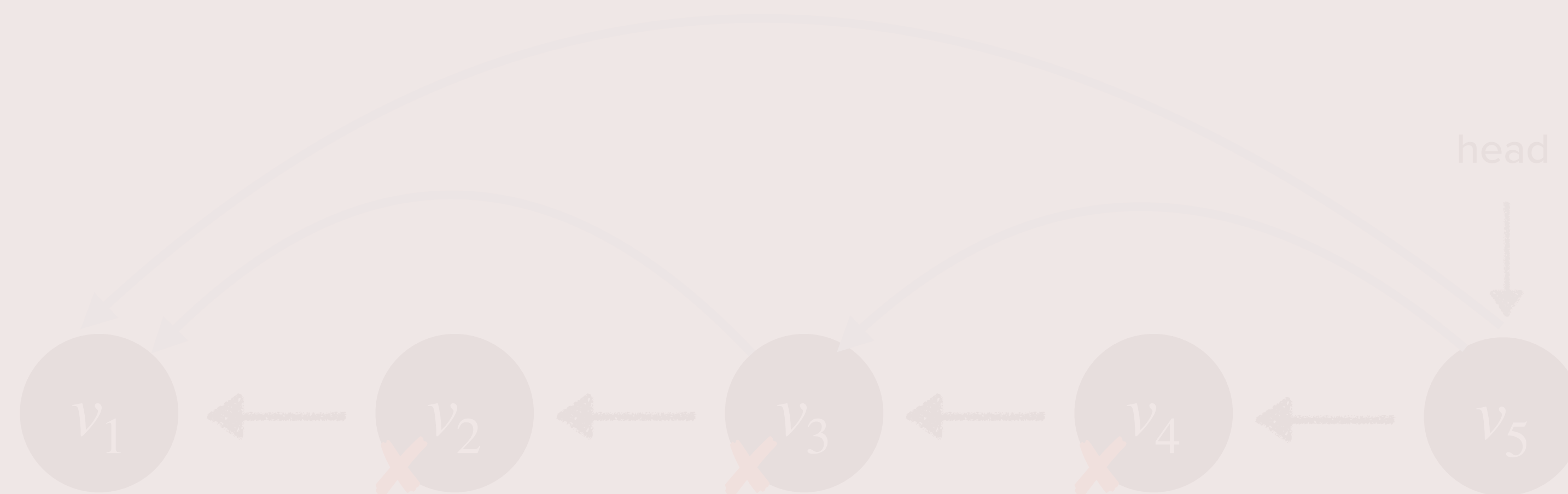
Let's delete v_3



Need to delete these two

- 1 Two patches from v_5
Bad for correctness
- 2 Size of PL = # values deleted
Bad for efficiency

Let's delete v_3



Need to delete these two

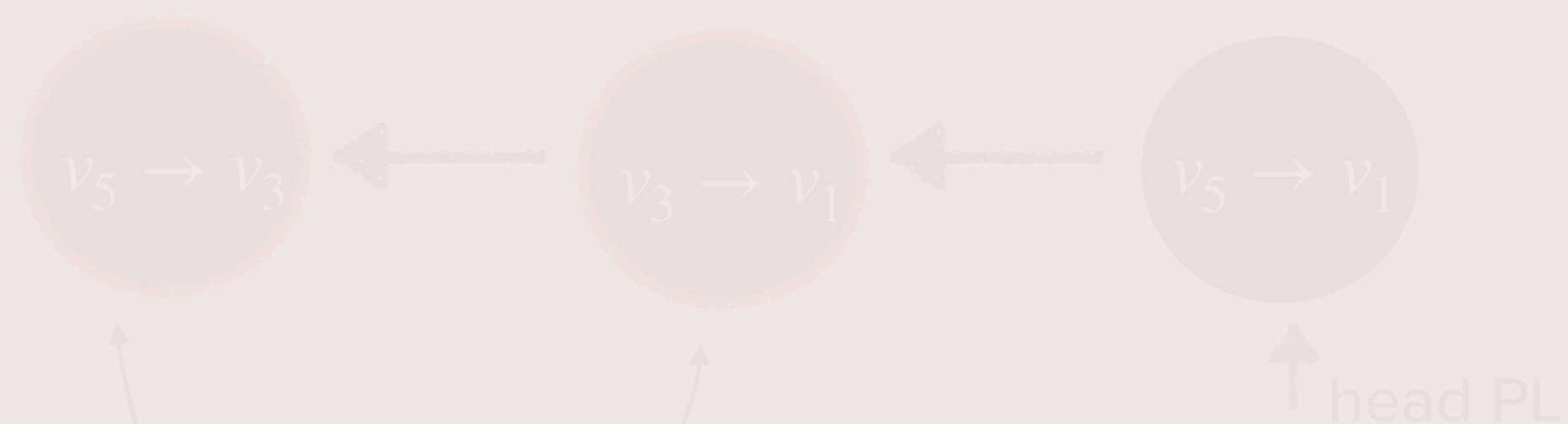
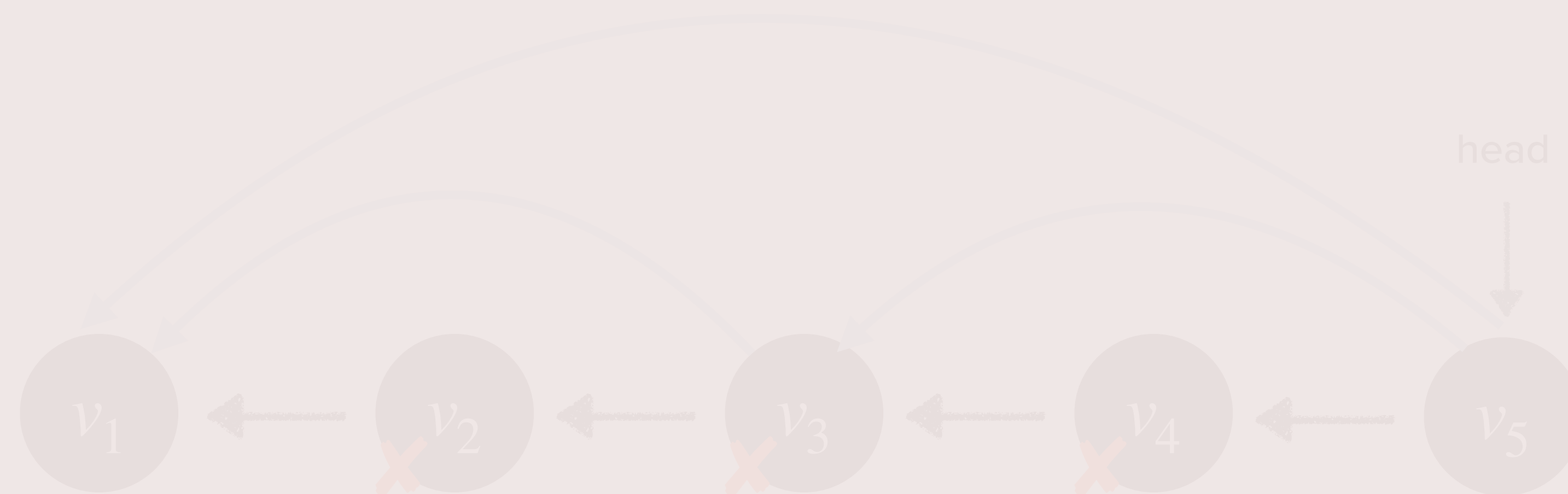
1 Two patches from v_5

Bad for correctness

2 Size of PL = #   deleted

Bad for efficiency

Let's delete v_3



Need to delete these two

1 Two patches from v_5

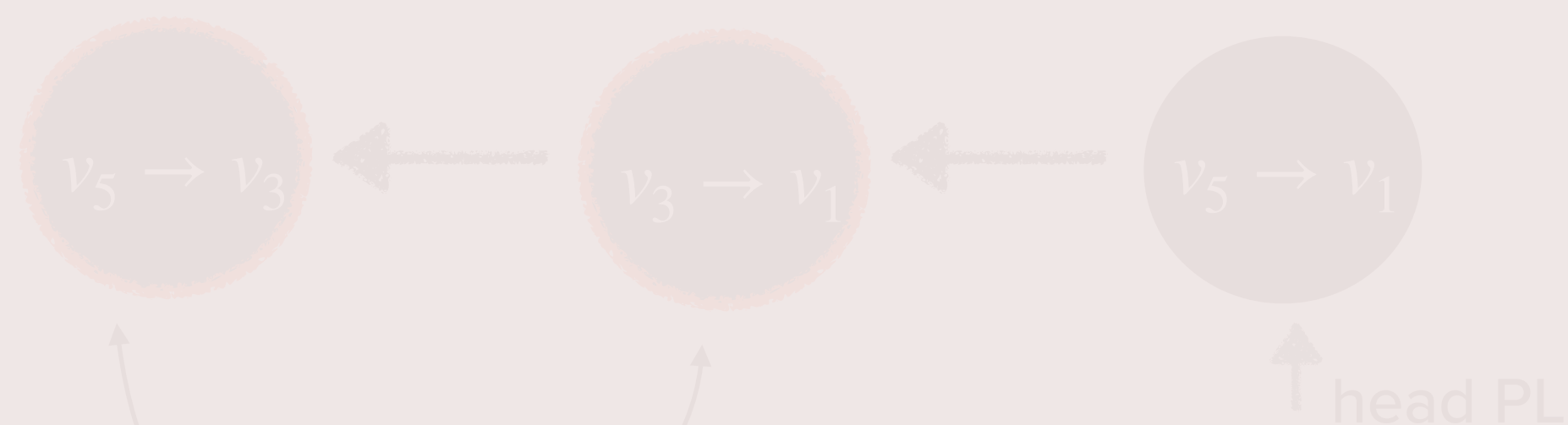
Bad for correctness

2 Size of PL = #   nodes deleted

Bad for efficiency

Let's delete v_3

Copy On Write



Need to delete these two

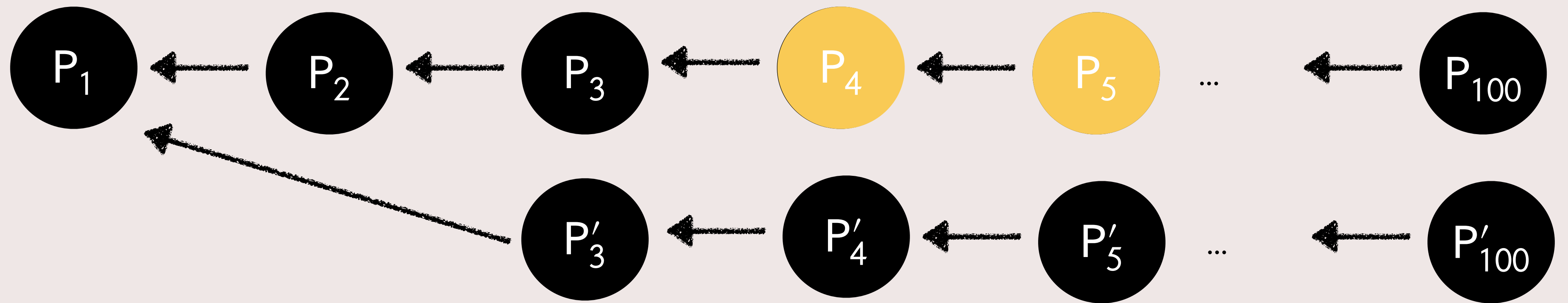
1 Two patches from v_5

Bad for correctness

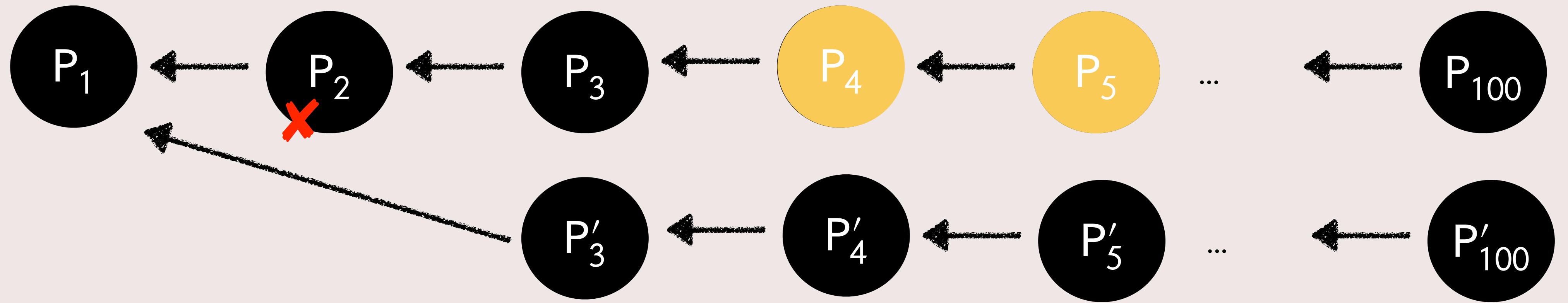
2 Size of PL = #   v_i s created

Bad for efficiency

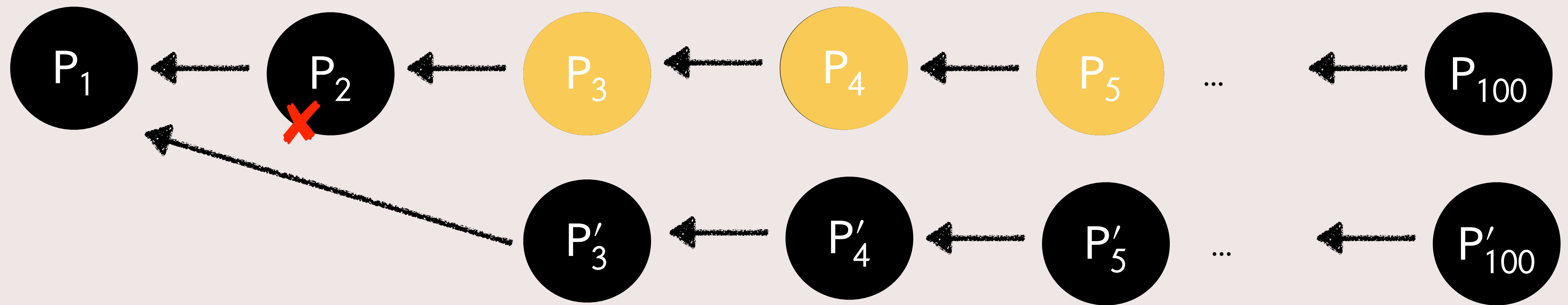
PAX



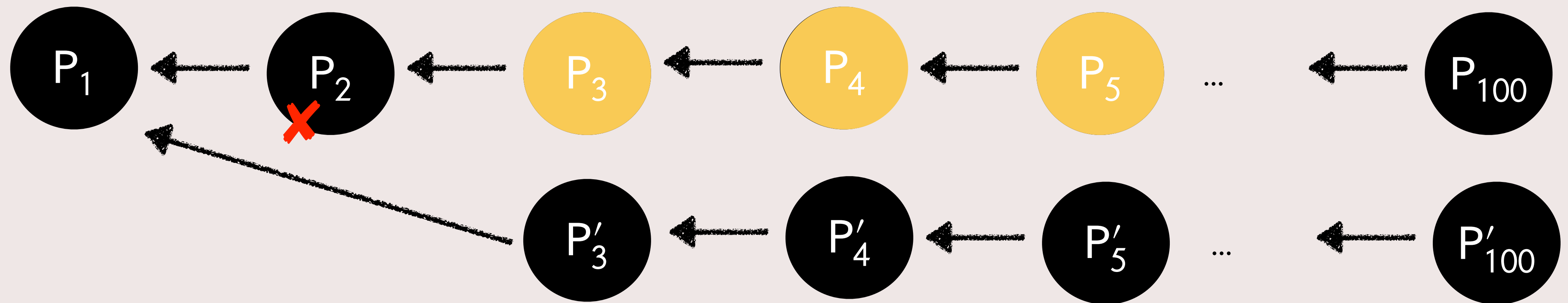
PAX



PAX

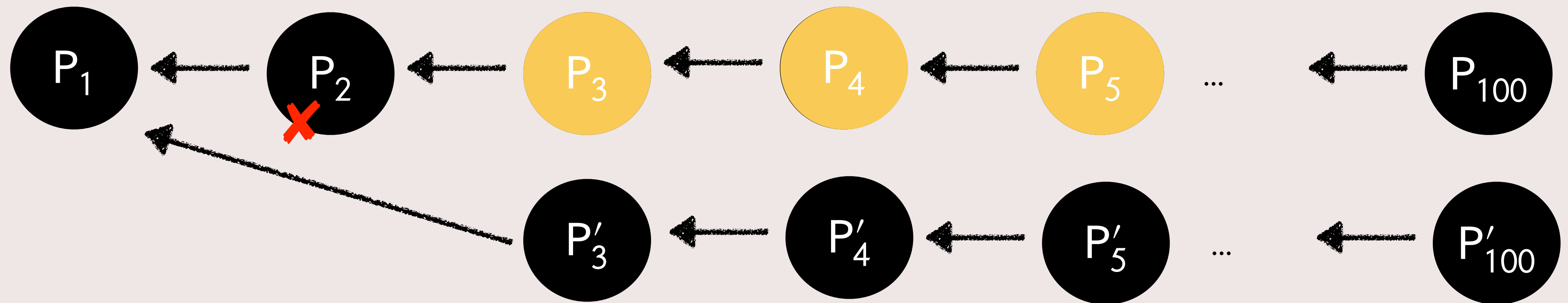


PAX

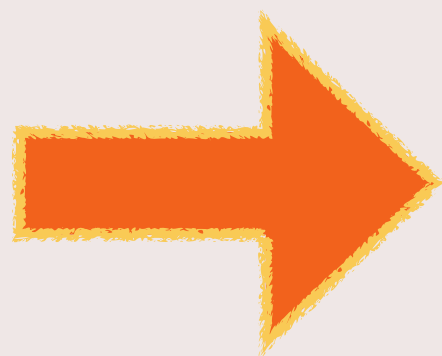


Expensive!

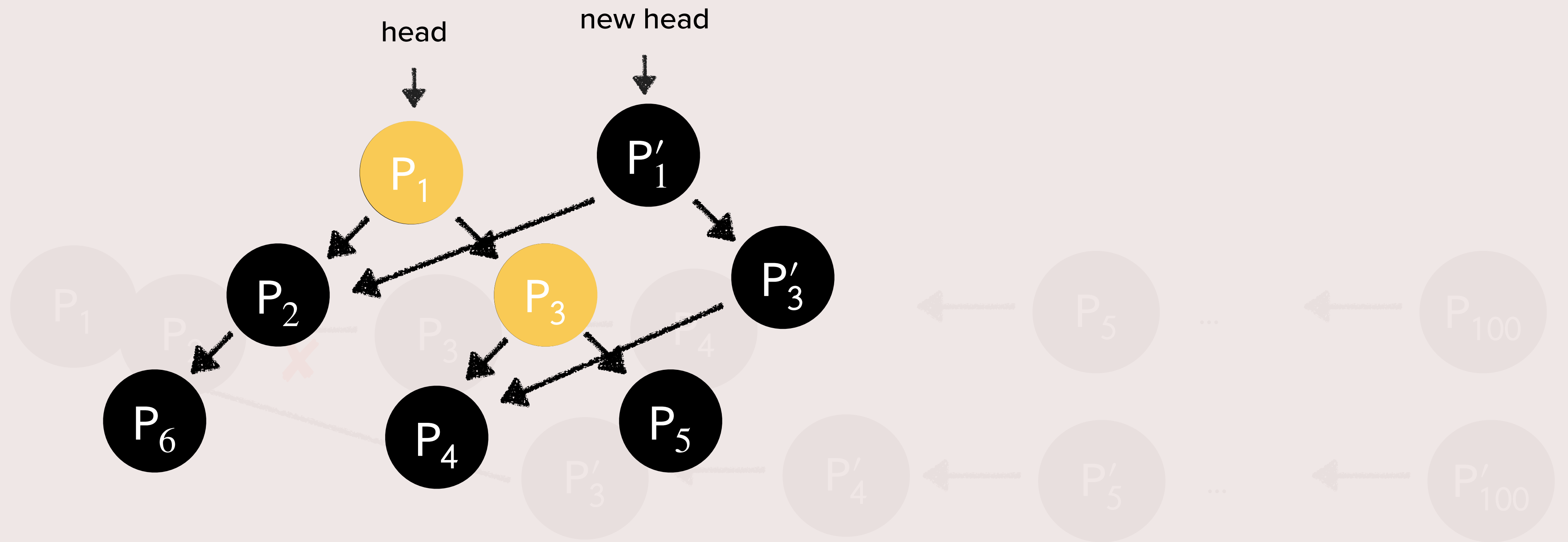
PAX



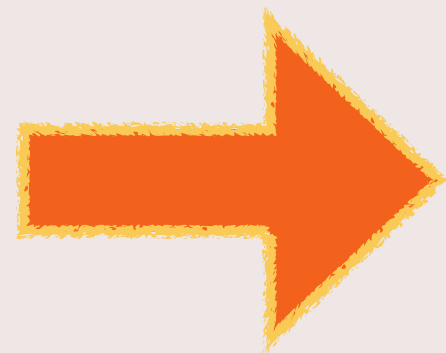
Expensive!



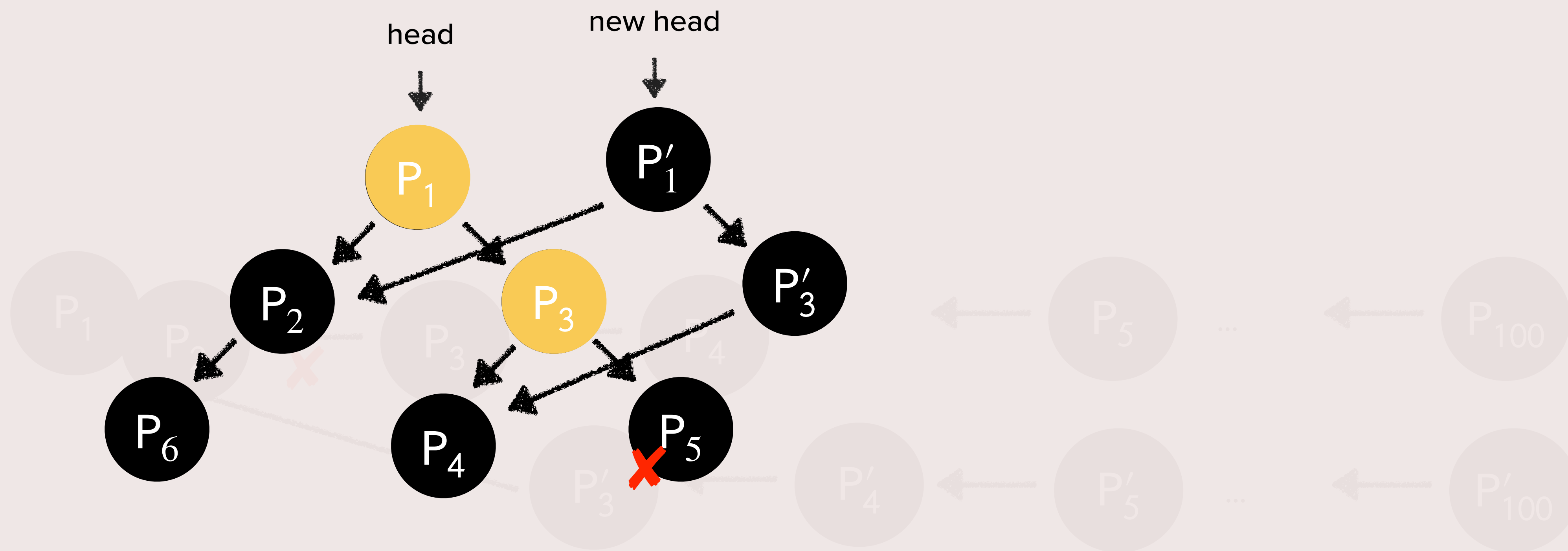
Organize patches in a BST



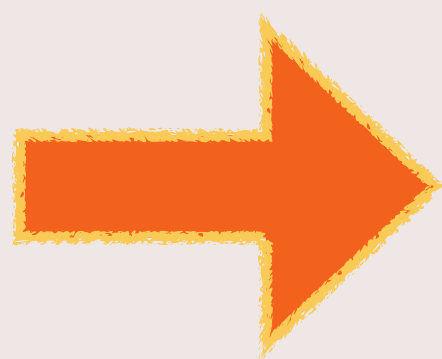
Expensive!



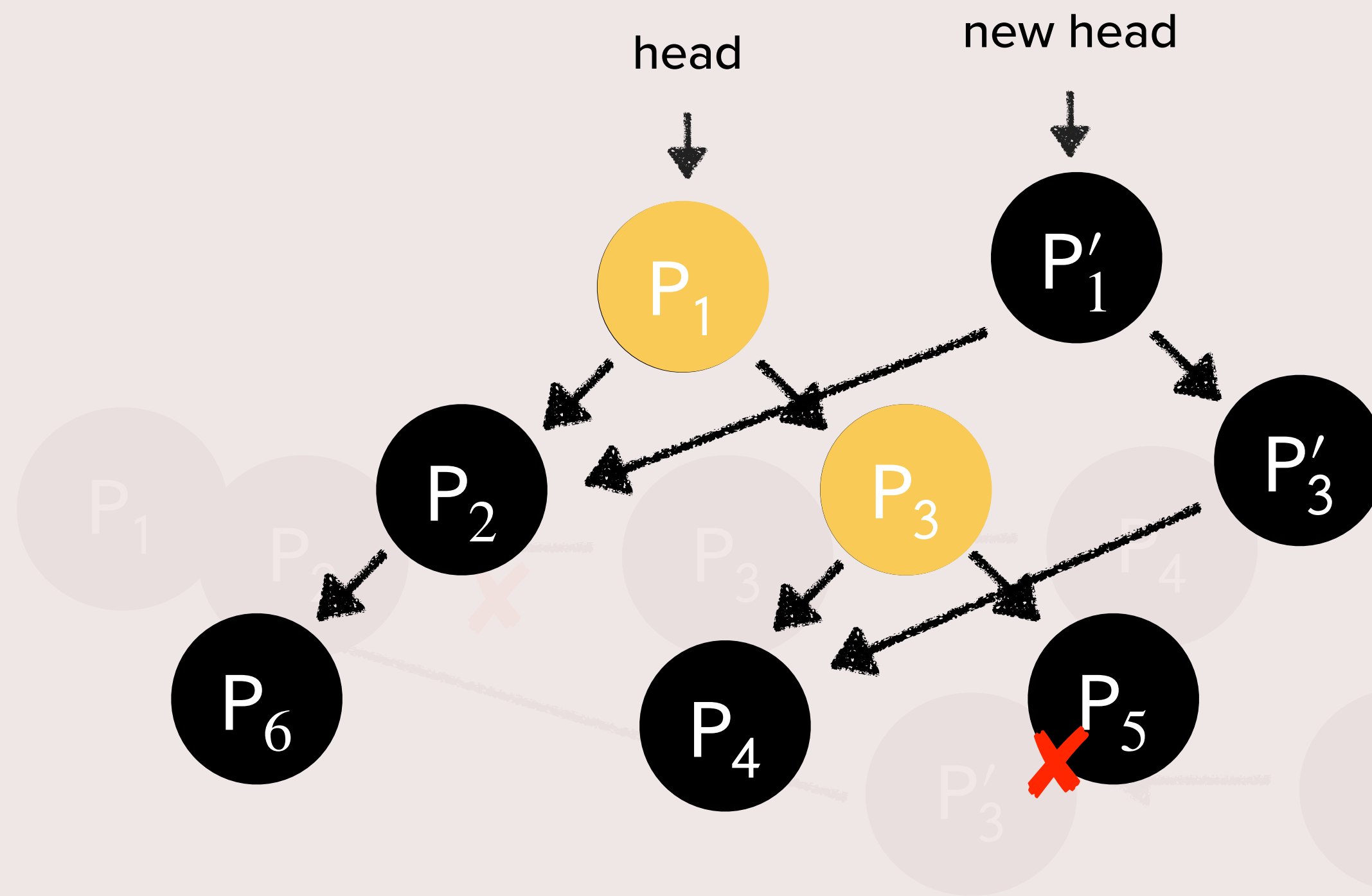
Organize patches in a BST



Expensive!



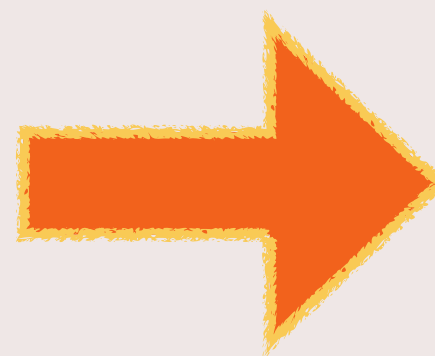
Organize patches in a BST



Show

nodes in BST
 \leq # values in multi-map

Expensive!



Organize patches in a BST

PAX

Add

time

stabilization

time LSX

stabilization LSX

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

Delete

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

Query

$O(\# \text{ values ever added/deleted})$

PAX

Add

time
 $O(|t|)$

stabilization

time LSX
 $O(|t|)$

stabilization LSX
 $O(|t|)$

Delete

$O(|t|)$

$O(|t|)$

Query

$O(\# \text{ values ever added/deleted})$

PAX

Add

time
 $O(|\mathbf{t}|)$

stabilization

time LSX
 $O(|\mathbf{t}|)$

stabilization LSX
 $O(|\mathbf{t}|)$

Delete

$$O(|\mathbf{t}| \log(\text{size of MM}))$$

$$O(|\mathbf{t}|)$$

$$O(|\mathbf{t}|)$$

Query

$$O(\# \text{ values ever added/deleted})$$

PAX

Add

time
 $O(|t|)$

stabilization

time LSX
 $O(|t|)$

stabilization LSX
 $O(|t|)$

Delete

$$O(|t| \log(\text{size of MM}))$$

$$O(|t|)$$

$$O(|t|)$$

Query

$$O(\text{size of MM})$$

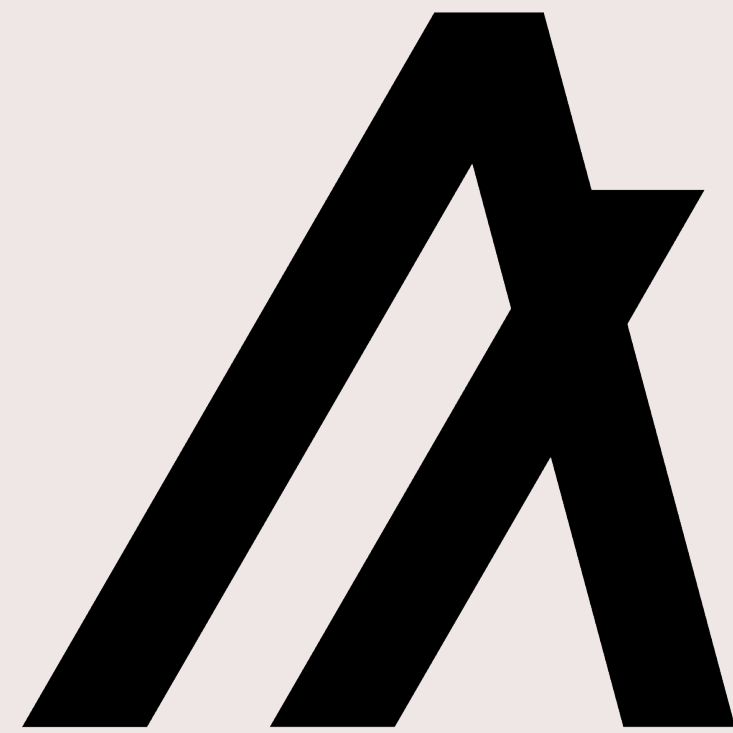
$$O(\# \text{ values ever added/deleted})$$

PAX

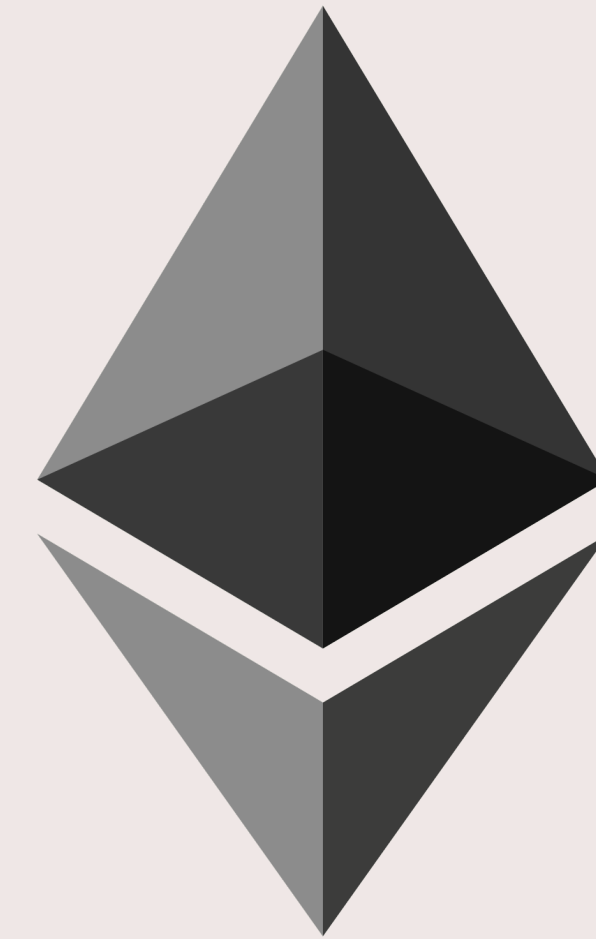
	<i>time</i>	<i>stabilization</i>	<i>time LSX</i>	<i>stabilization LSX</i>
Add	$O(\mathbf{t})$	$O(\mathbf{t})$	$O(\mathbf{t})$	$O(\mathbf{t})$
Delete	$O(\mathbf{t} \log(\text{size of MM}))$	$O(\mathbf{t})$	$O(\mathbf{t})$	$O(\mathbf{t})$
Query	$O(\text{size of MM})$		$O(\# \text{ values ever added/deleted})$	

- What are Multi-Maps (MMs)
- What are Encrypted Multi-Maps (EMMs)
- How to store EMMs on Blockchains
 - LSX
 - TRX
 - PAX
- **Real World Deployment**

Real World Deployments

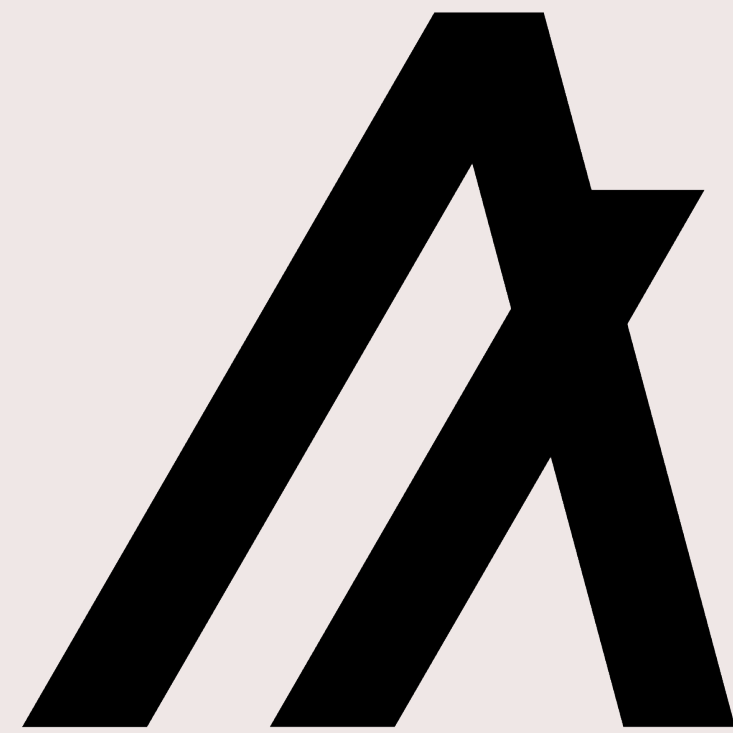


Algorand

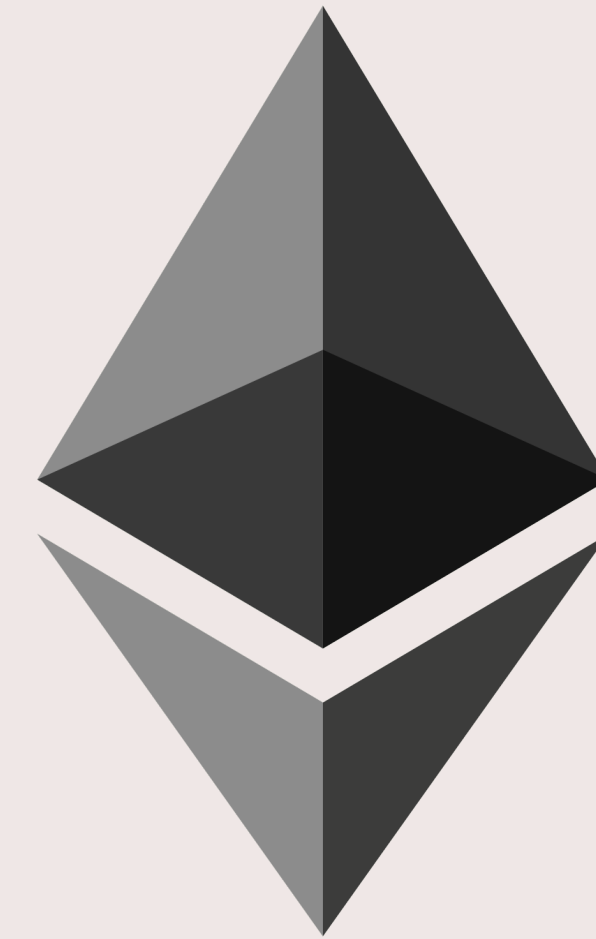


Ethereum

Real World Deployments



Algorand

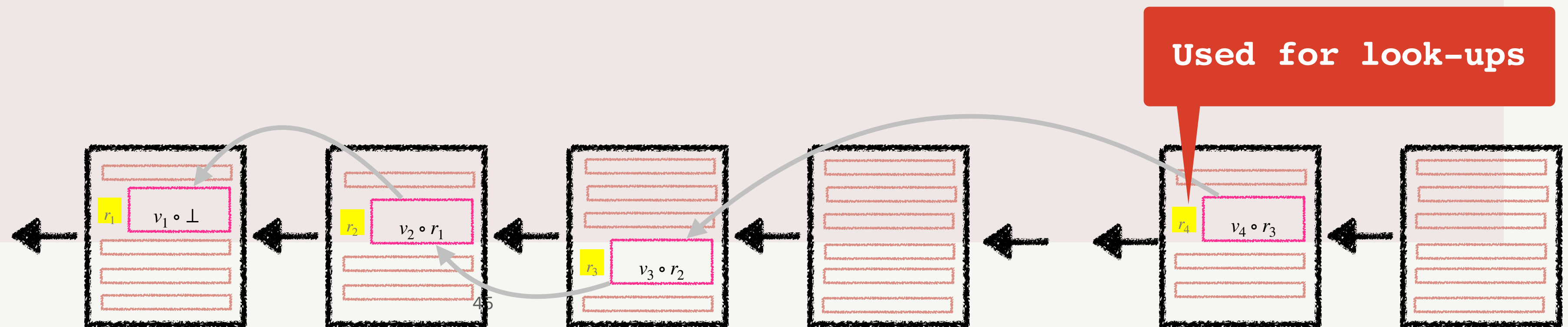


Ethereum

Some things to think about ...

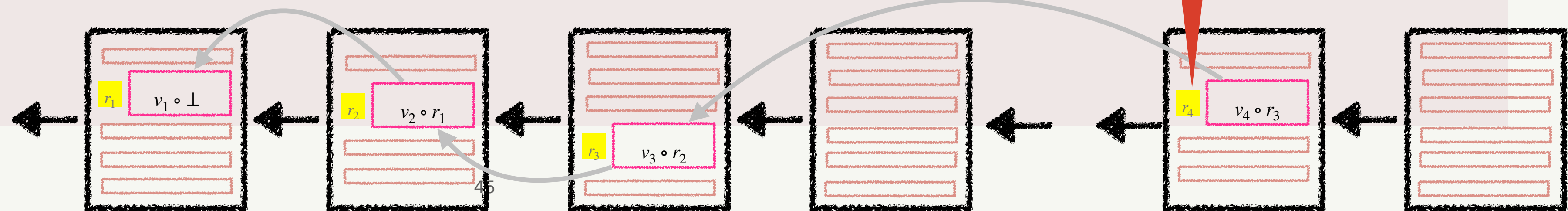
①

What should we use as addresses?



① What should we use as addresses?

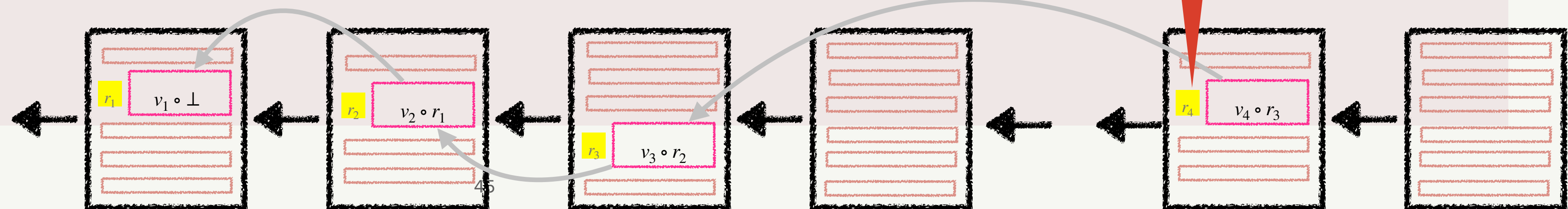
TX hashes



① What should we use as addresses?

TX hashes

- All writes can be sent in parallel
 - LSX = TRX
 - Stabilization complexity = $O(1)$

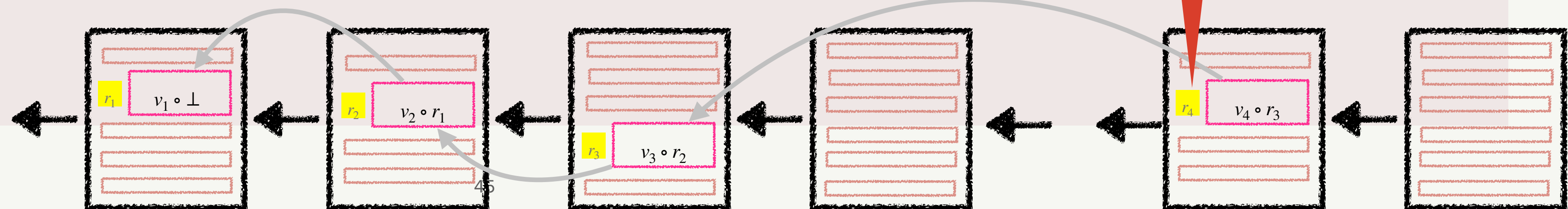


① What should we use as addresses?

TX hashes

- All writes can be sent in parallel
 - LSX = TRX
 - Stabilization complexity = $O(1)$

- Might require database indexing
- Many BCs do not support this



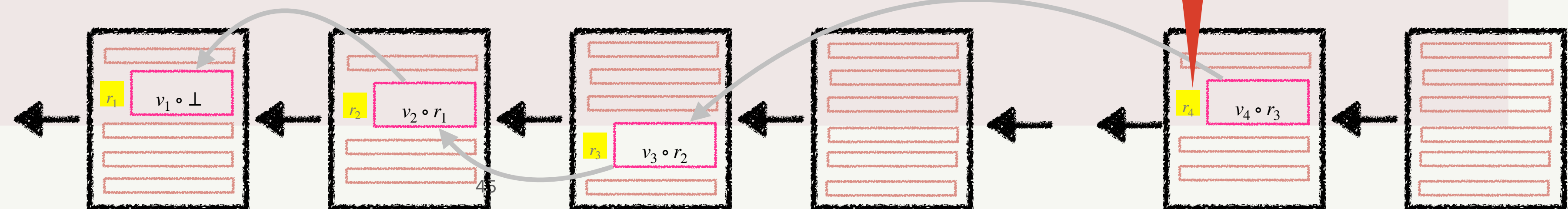
① What should we use as addresses?

TX hashes

Block numbers + TX hashes

- All writes can be sent in parallel
 - LSX = TRX
 - Stabilization complexity = $O(1)$

- Might require database indexing
- Many BCs do not support this



① What should we use as addresses?

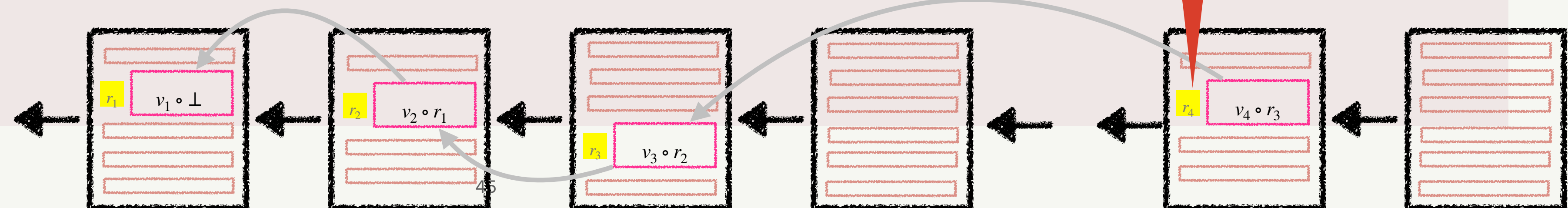
TX hashes

- + All writes can be sent in parallel
 - LSX = TRX
 - Stabilization complexity = $O(1)$

- Might require database indexing
- Many BCs do not support this

Block numbers + TX hashes

- + BCs support fast lookup by block numbers



① What should we use as addresses?

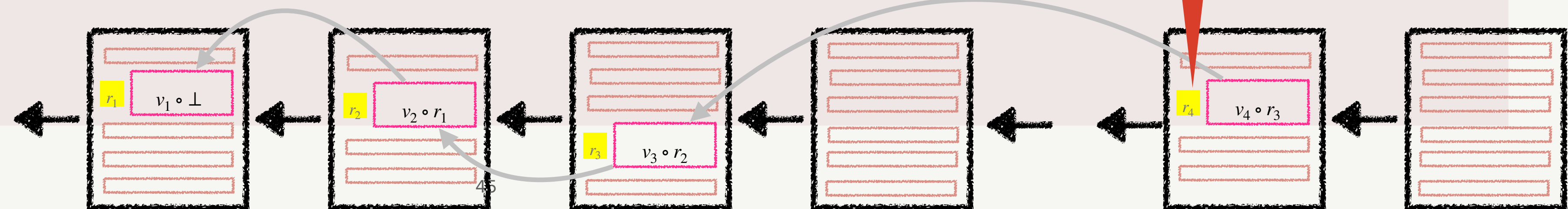
TX hashes

- + All writes can be sent in parallel
 - LSX = TRX
 - Stabilization complexity = $O(1)$

- Might require database indexing
- Many BCs do not support this

Block numbers + TX hashes

- + BCs support fast lookup by block numbers
- Higher bandwidth required



① What should we use as addresses?

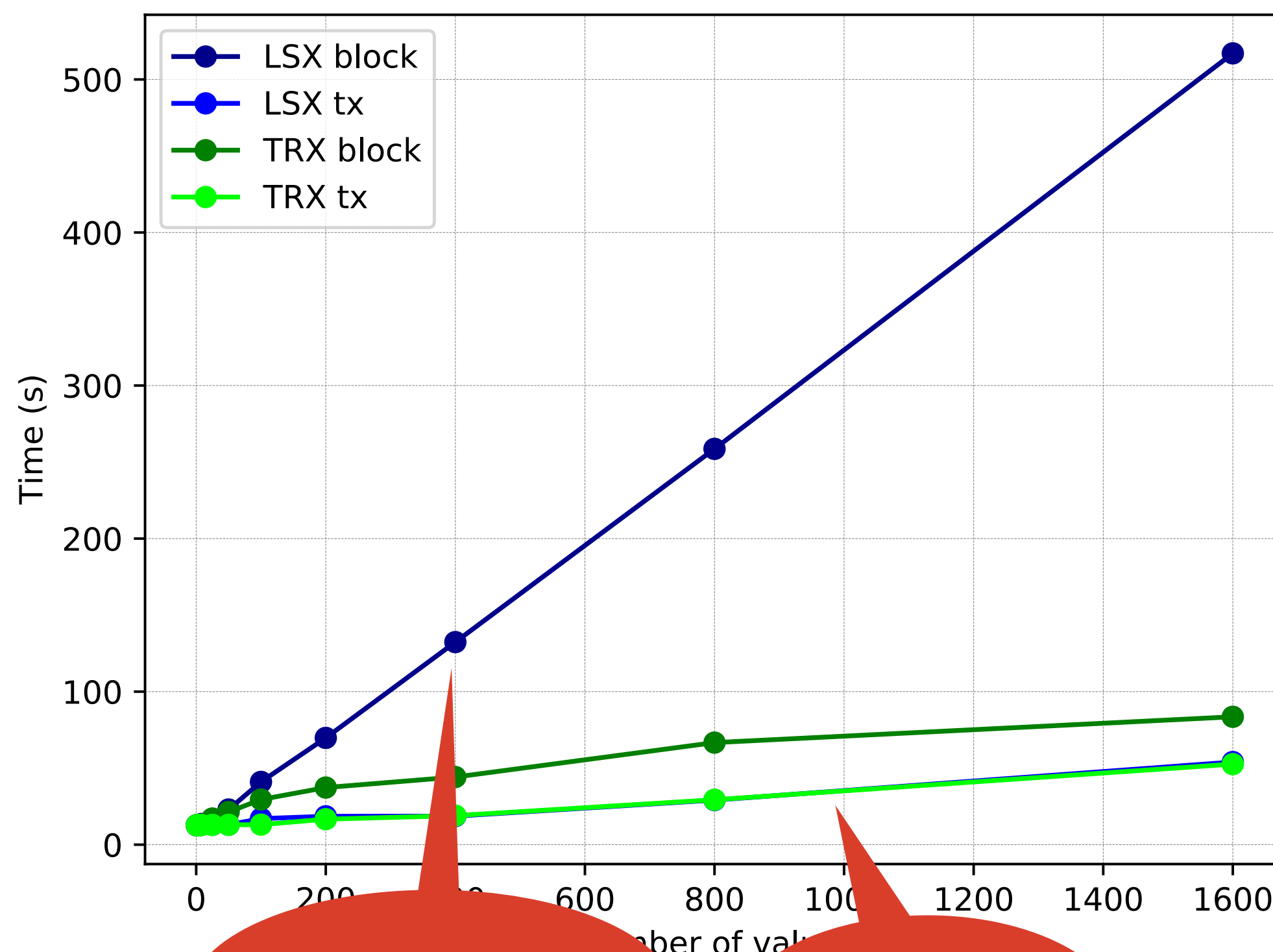
Add on Algorand

• LSX = TRX

• Stabilization con

• Might require data

• Many BCs do not s



LSX (block)

LSX (tx)

Used for look-ups



① What should we use as addresses?

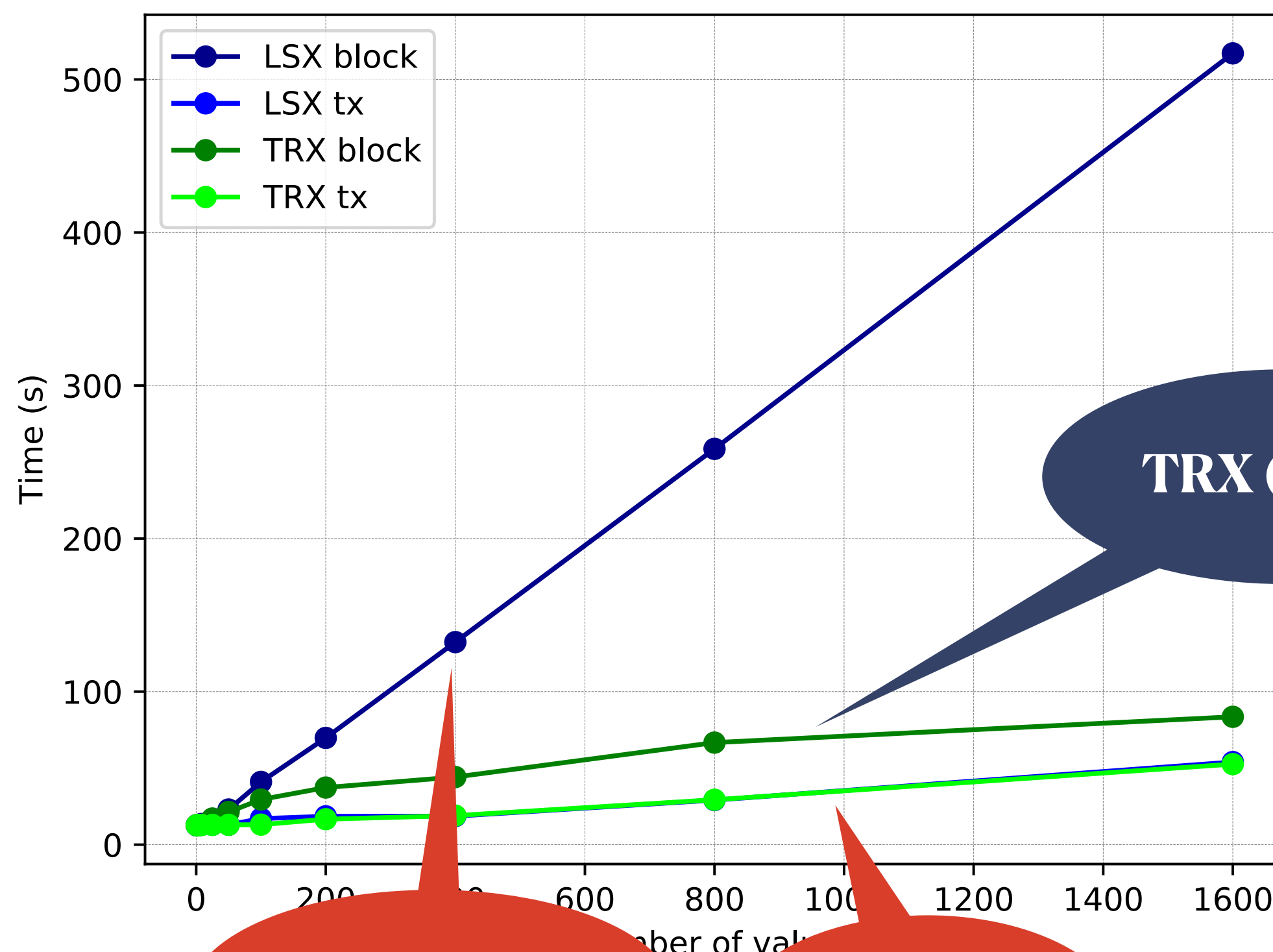
Add on Algorand

• LSX = TRX

• Stabilization con

• Might require data

• Many BCs do not s



LSX (block)

LSX (tx)

TRX (block)

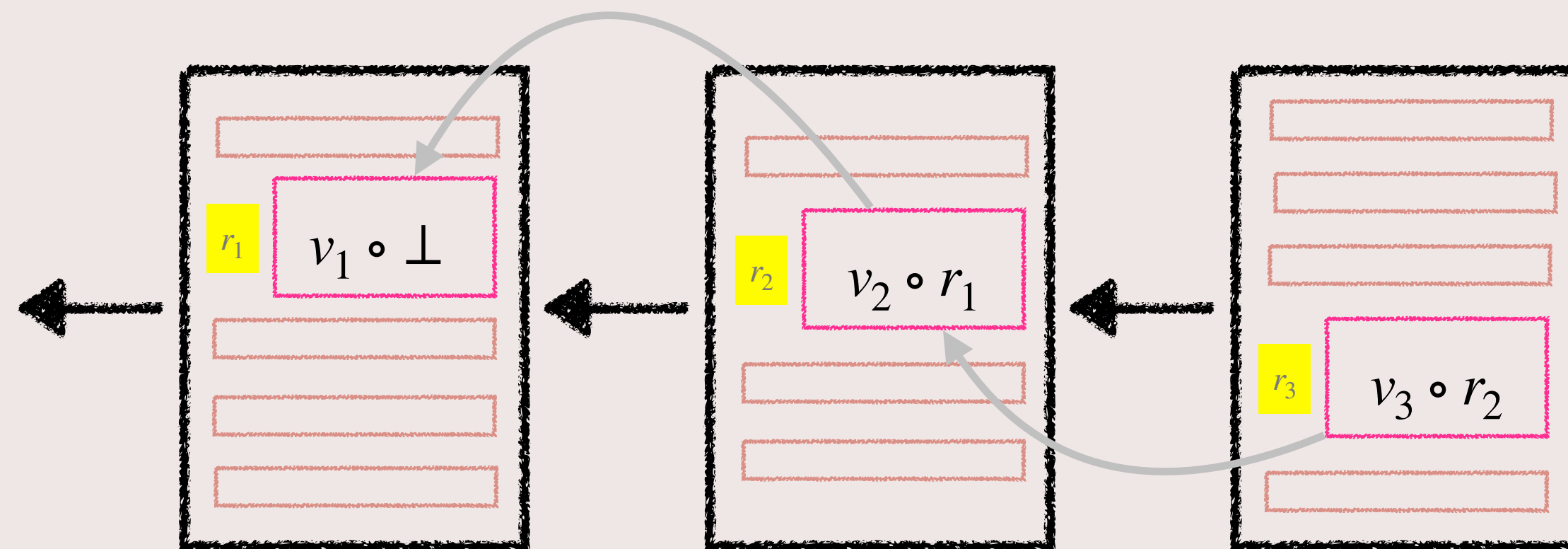
TRX (tx)

Used for look-ups



② Packing

Saves time & money

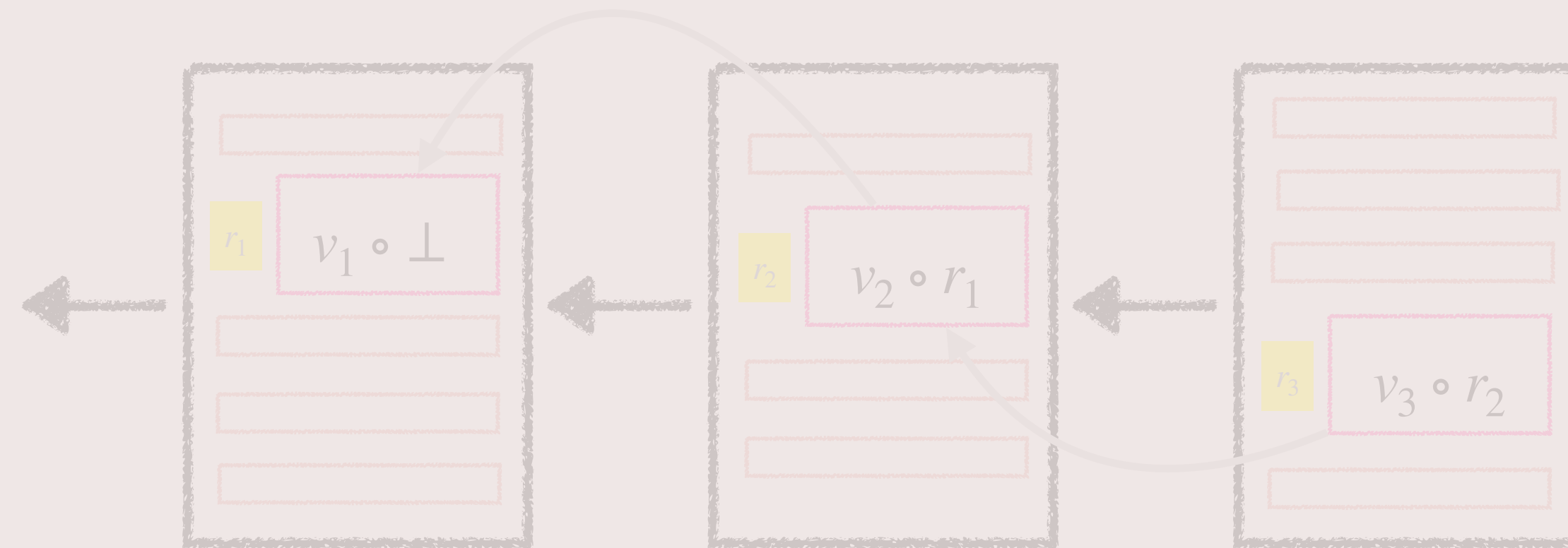


$v_1 \circ v_2 \circ v_3 \perp$

Store multiple
values in a tx

② Packing

PAX doesn't support packing



$v_1 \circ v_2 \circ v_3 \perp$

Store multiple
values in a tx

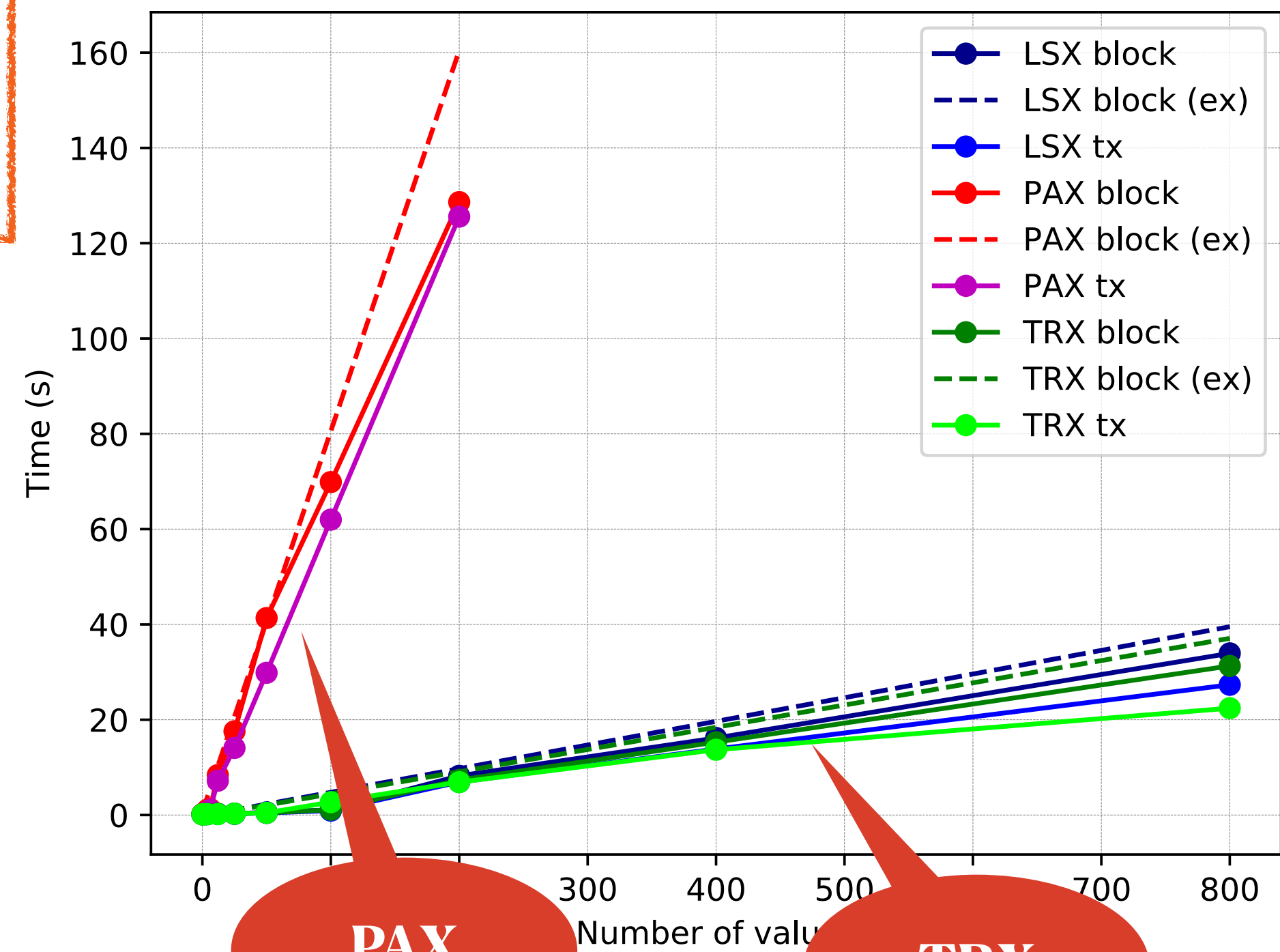
② Packing

PAX doesn't support packing

Query on Algorand

time PAX
 $O(\text{size of MM})$

time TRX
 $O(\text{\# values ever added/deleted})$



PAX

TRX

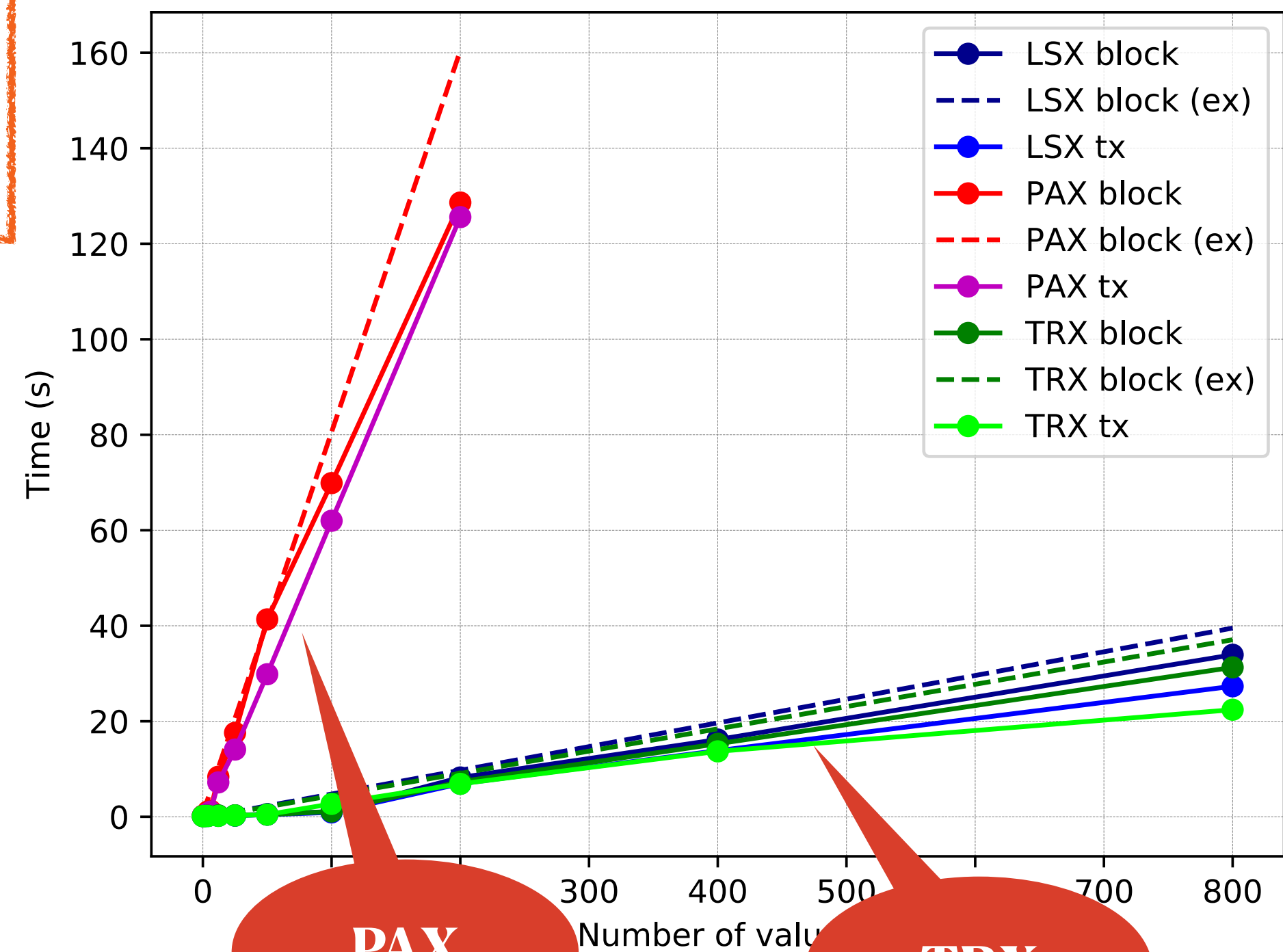
② Packing

PAX doesn't support packing ?

Query on Algorand

time PAX
 $O(\text{size of MM})$

time TRX
 $O(\text{\# values ever added/deleted})$



PAX

TRX

② Packing

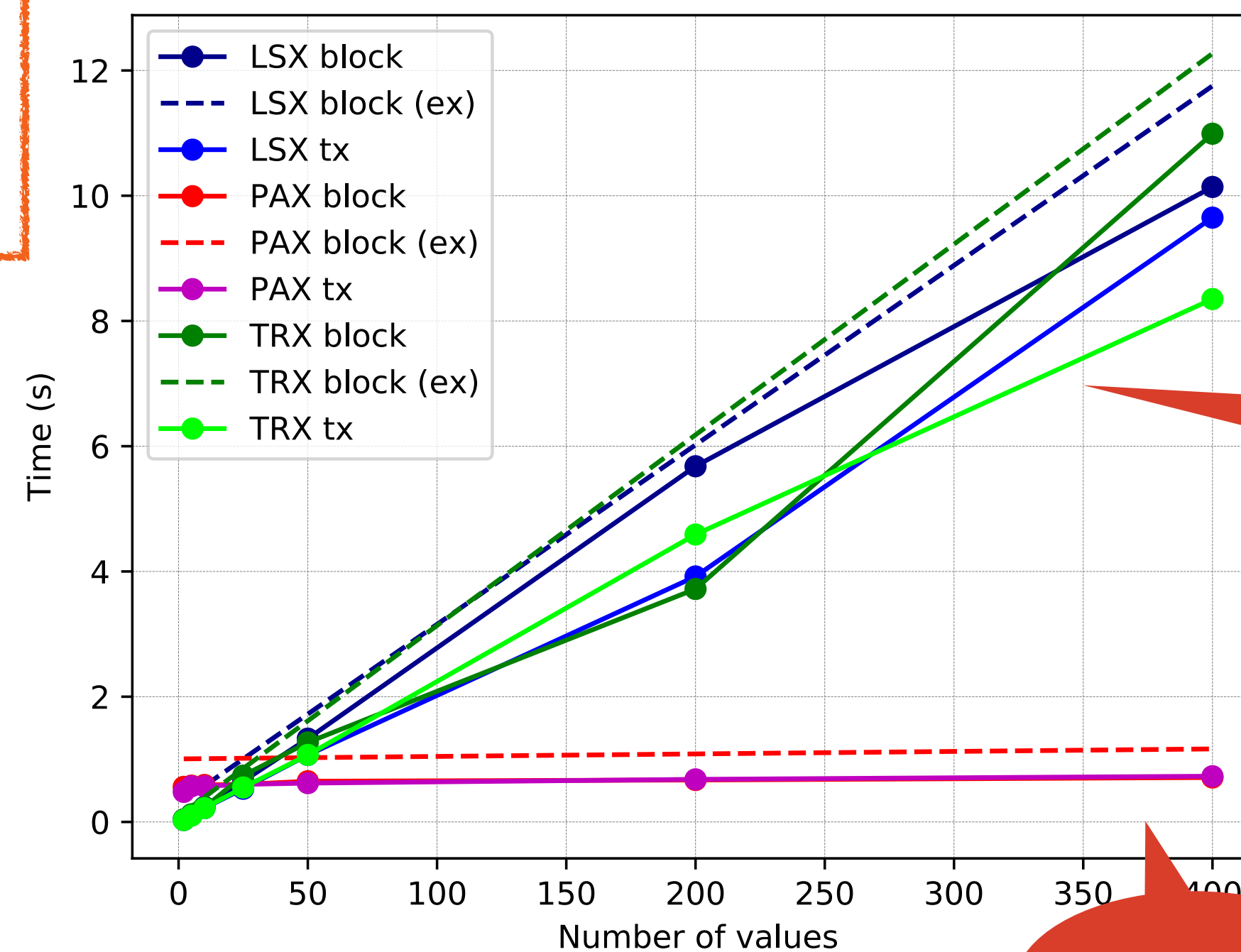
PAX doesn't support packing ?

Query on Algorand

(after most values have been deleted)

time PAX
 $O(\text{size of MM})$

time TRX
 $O(\# \text{ values ever added/deleted})$



TRX

PAX



